

# Photogrammetry and laser scanning course for beginners



CTU in Prague Faculty of Civil Engineering,  
Department of Geomatics

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## *Photogrammetry and laser scanning*

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Laboratory of photogrammetry

# Introduction



- **Photogrammetry** part of the field of geodesy and cartography, which deals with the determination of geometric and positional information from image records, most often from photographic images
- **RemoteSensing(RS)** deals with non-contact detection of surface cover types and their condition
- **Laser scanning** 3D scanning technology that uses laser measurements to determine the spatial coordinates of detailed points on an object.

# Introduction



**Photogrammetry, RS and laser scanning are methods that provide mass localized information for technology**

## **GIS**

- Basic sources of primary information about the territory supply:
- **geodetic methods** accuracy in the order of **mm - cm**
- **photogrammetry** accuracy in **mm, cm - dm**
- **RS** accuracy in the order of **m - km**



# History



## Al-Hassan bin Al-Haithm (965-1039)

\*

in 1032 he was the first to describe  
the "*camera obscura*" –*the central projection*  
*principle*

# History



- **Leonardo da Vinci (1452 1519) described the pinhole camera for the construction of central projections**
- **1605 Galileo Galilei invents the telescope**
- **1657 Schott Kasper builds the first portable box camera**
- **in 1777 the invention of the light sensitive compound , AgCl (C.H.Scheele )**
- **theories of reconstruction of acquired perspective images : Taylor (1715) and J.H.Lambert (1759)**
- **invention of photography : Niepce and Daquerre (1839)**
- **negative positive: Talbot 1841**
- **the title of the photo comes from J.Herschel**
- **the first aerial photographs were taken by the famous French photographer G.F.Tournachon called Nadar ) in 1858**

- the first phototeodolite was constructed according to the design of A. Laussedat ( 1859); used in France for mapping in 1861
- photogrammetry " dates back to 1858, when the German A.Meydenbauer used the term
- G . Eastman , 1884 paper film) and its introduction in 1889 (celluloid film , first roll film camera
- C . Pulfrich Zeiss Jena) in 1901 constructed the first device for stereoscopic measurement , the stereocomparator
- E .Orel , 1909 1911 constructed the first Autostereograph since 1909 in the Carl Zeiss Jena works as " Stereoautograph "
- Th . Scheimpflug constructed in 1911 the first rectifier for transforming an inclined image of flat terrain to the scale of a map
- W .Wright was the first to take pictures from a plane in 1903
- imaging from aircraft found its application with the advent of World War I.
- In 1935, the first Kodakchrome colour film was released

**- during the World War II. some new cameras and instruments were**

**constructed and methods of using photogrammetry were developed , but**

**mainly for military purposes**

**- further development of photogrammetry occurred again after 1945**

**analogue plotters**

**- space technology**

**- Seventies analytical plotters used computers**

**- Eighties development of digital technologies**

**- 1990s full transition to digital technology**



# History

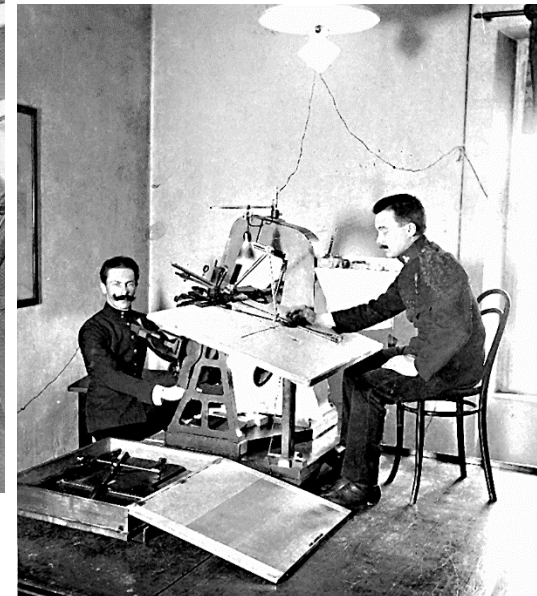
**Karel Kořistka (1825 1906 ) professor of mathematics and geodesy , the first rector of the Royal Czech Polytechnic Institute in Prague in the school year 1864 65. Pioneer of photogrammetry in the Czech lands**

**K.Kořistka**

**got acquainted with photogrammetry on a study trip in 1862**

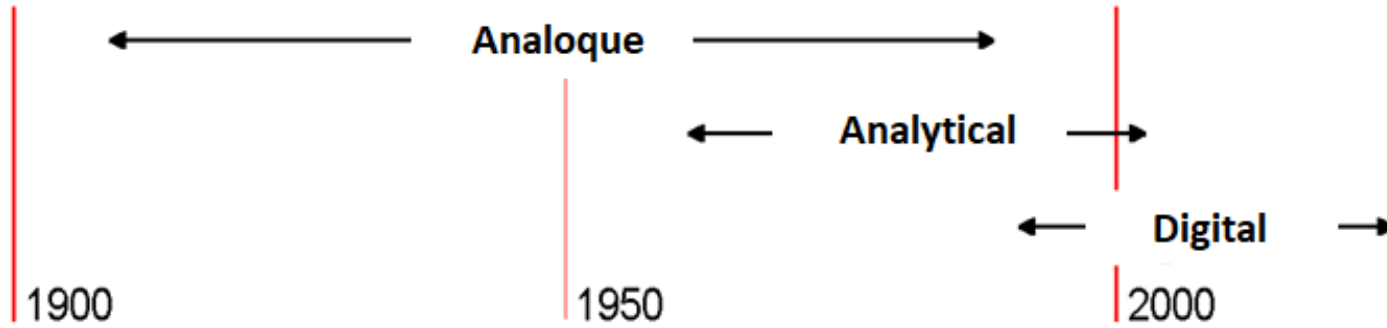
**directly with A.Laussead and after his return from this trip he used it in Prague**

World War I.



# *Photogrammetry subdivision*

## *Basic stages of development: technology*



### **Basic criteria for dividing photogrammetry**

**a) according to the position of the position**

**Terrestrial , air, satellite**

**b) by number and configuration of images**

**Single frame and multi frame : stereo or intersection**

**b) according to the processing technology**

**Analogue, analytical , digital**



# *Use of photogrammetry (in CZ, but it is typical)*



- **State map works in CZ, State Administration of Land Surveying and Cadastre (ČÚZK) topographic maps (1:10**
- **Military topographic maps (in CZ , Army of the Czech Republic)**
- **Information systems state administration , GIS information layers ) , digital models DMR and DMP)**
- **Monument care ( monument care workers , architects ) documentation , documents**
- **Construction design and construction companies ) documents , documentation , determination of deformations**
- **Environment (in CZ, administrations of National park, protected natural area , forestry maps (in CZ, Forest Management Institute ÚHÚL), vegetation delimitation**

# Next

**Come in:**

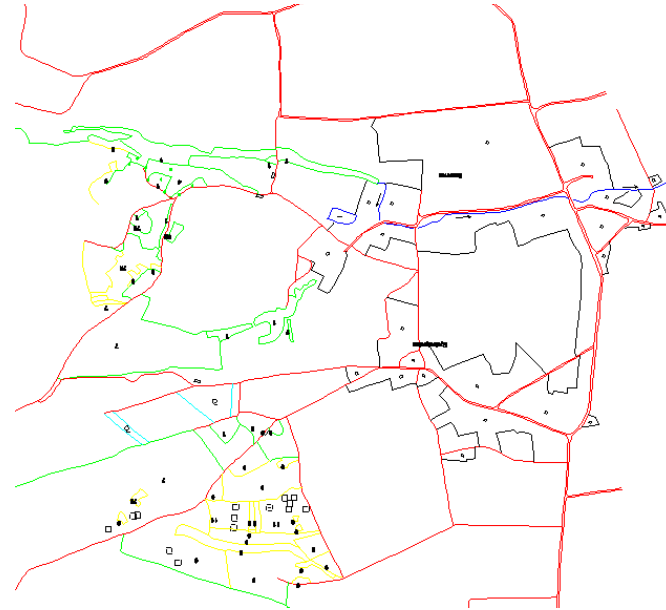
- **spatial planning 3D building models**
- **water management floods , Runoff profiles**
- **inventory and monitoring mines , quarries , landfills, landslides**
- **mechanical engineering precision control , deformation**
- **rehabilitation medicine , biomechanical applications etc.**



# *Use of photogrammetry in mapping*



**Original photogrammetric vertical image is similar to map**





# Reasons for using photogrammetry

⇒ minimising field work



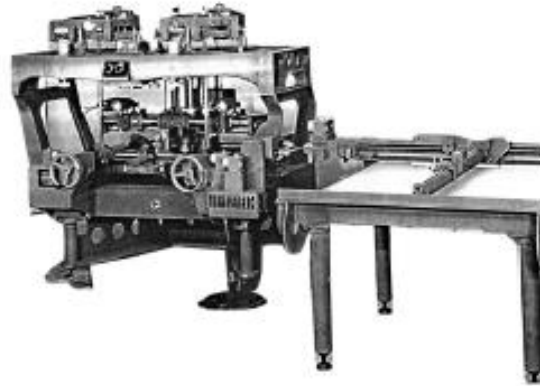
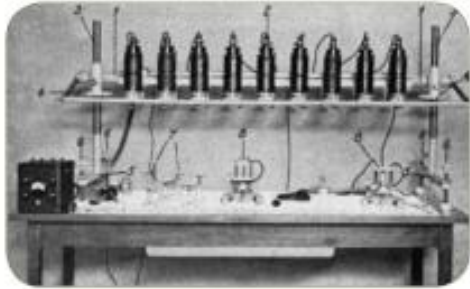
- economics



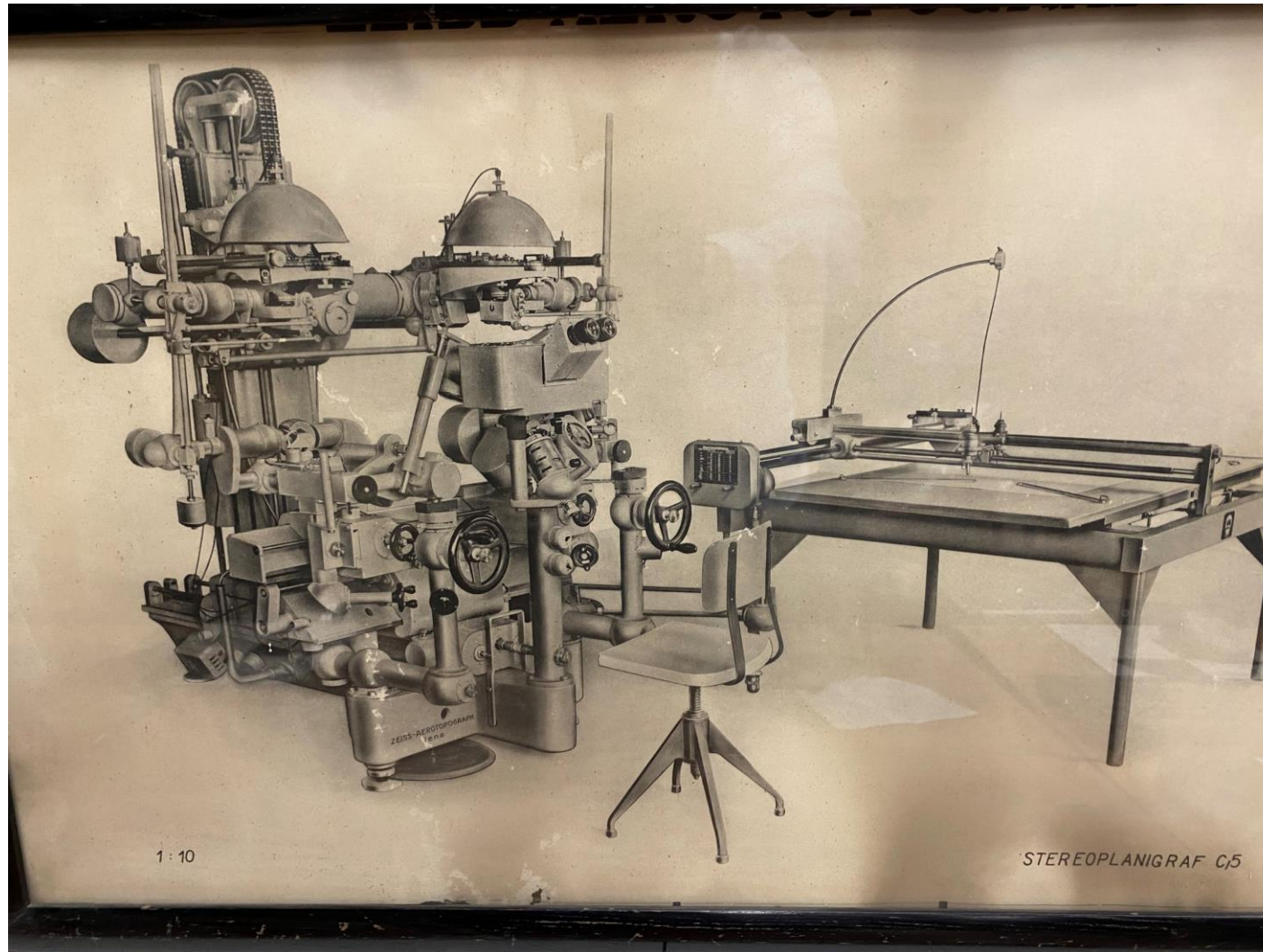
- speed

- overall time saving
- cost saving
- documentary value of the images time series
- higher resolution of the images compared to the map digital orthophoto

# From analogue photogrammetry to the digital technology



# Stereoplanigraph, 1930-1950





# DPW (digital photogrammetric Workstation (1990- today)

Stereo DWP



## Digital (automated) photogrammetry (after 2010)

Image correlation principle

Agisoft Photoscan-Metashape,

Zephyr 3D, pix4D, 123catch, aj.)

SfM+ MVS (structure from motion  
and multi view stereo)

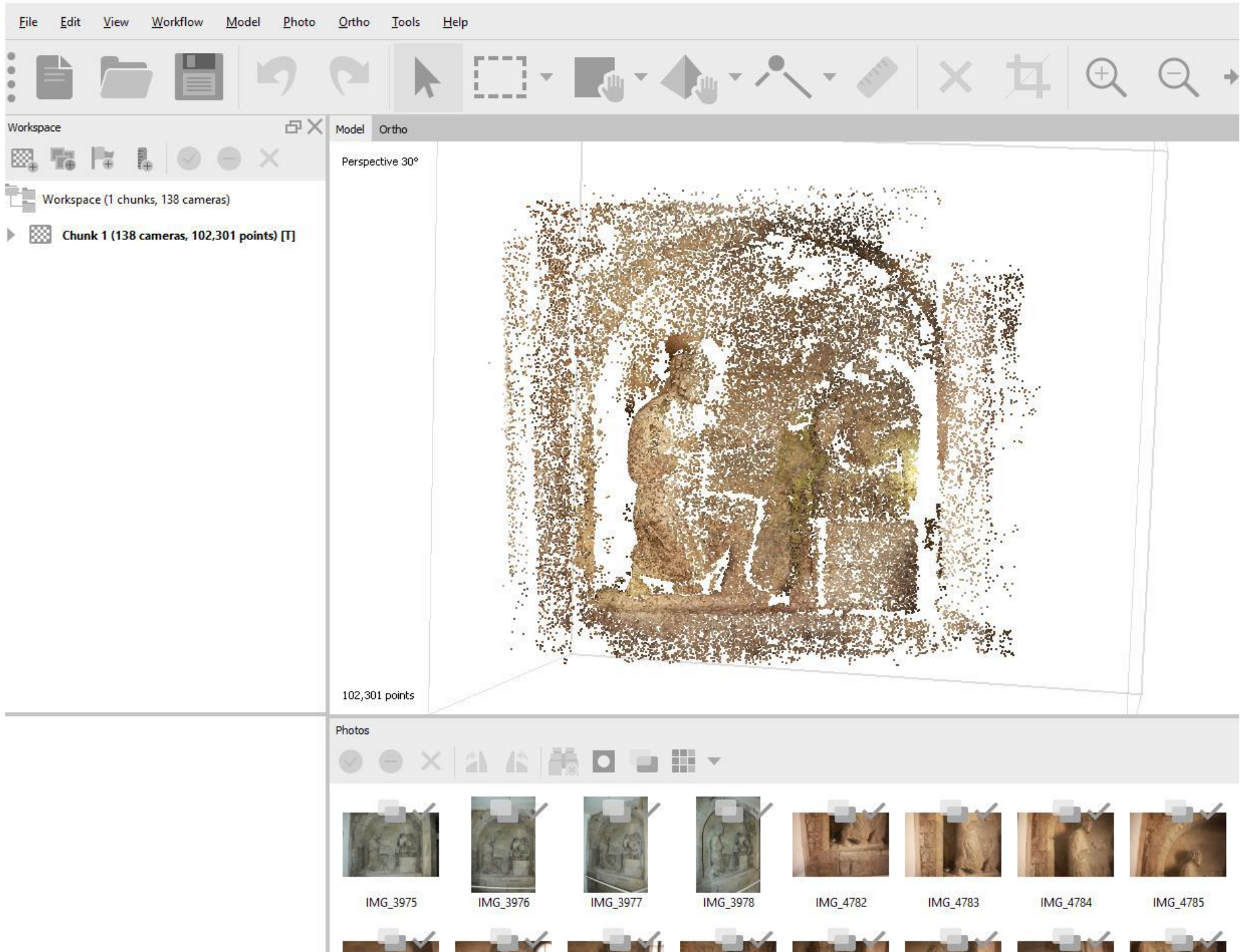


# Photogrammetry

terrestrial (hand – held)

aerial (aerial or using drones)

satellite







Workspace



Workspace (1 chunks, 138 cameras)

Chunk 1 (138 cameras, 102,301 points) [T]

Model Ortho

Perspective 30°

points: 57,778,176



Photos



IMG\_3975

IMG\_3976

IMG\_3977

IMG\_3978

IMG\_4782

IMG\_4783

IMG\_4784

IMG\_4785



Model Ortho

Perspective 30°



faces: 1,283,957 vertices: 1,232,169

# Case study –combined documentation of a historical object

- photogrammetry (terrestrial, drone)
- laser scanning
- mobile laser scanning
- VR

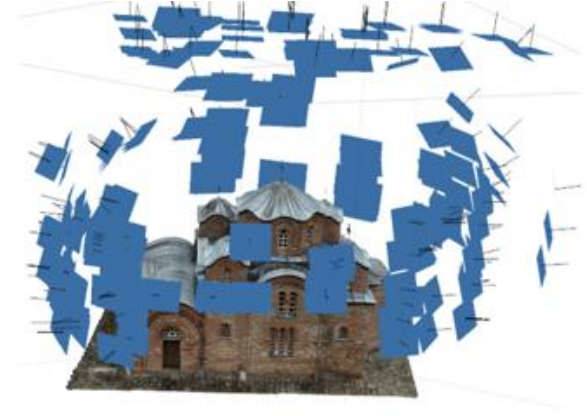
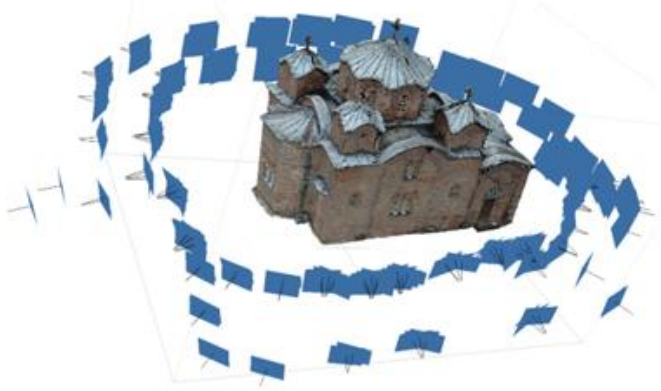
# Used instruments



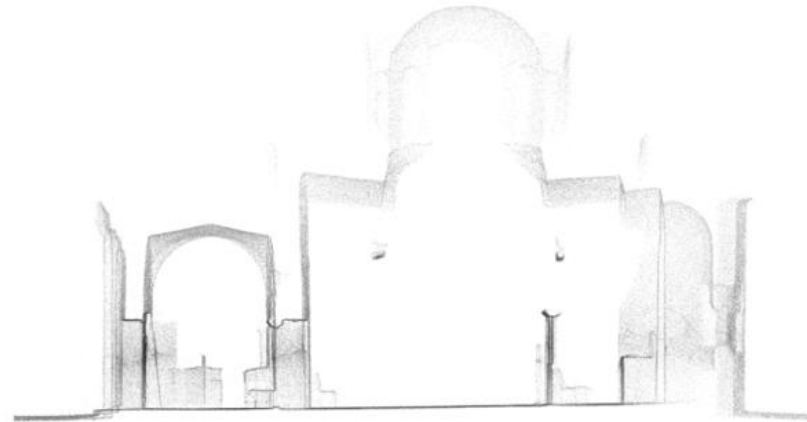
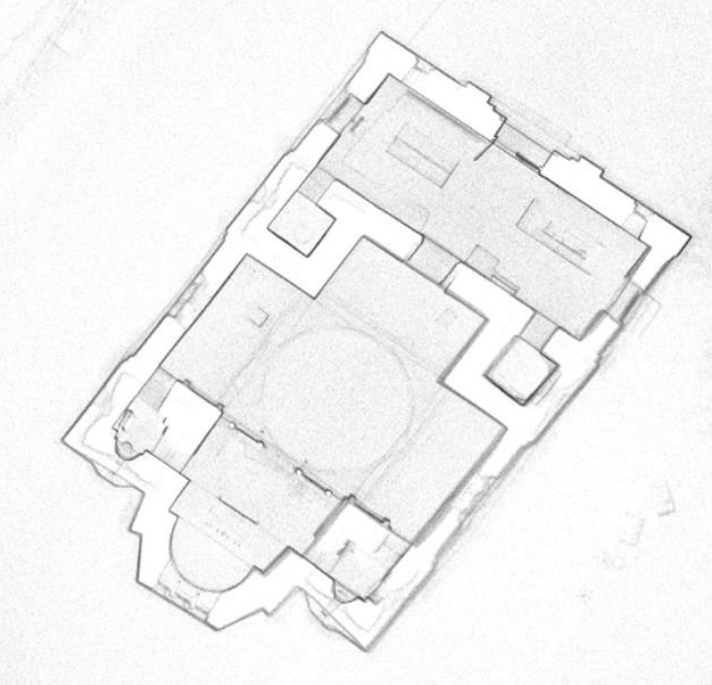
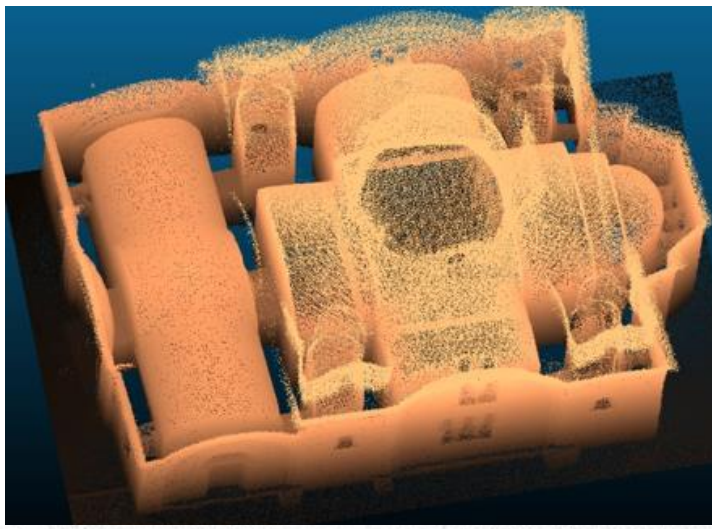




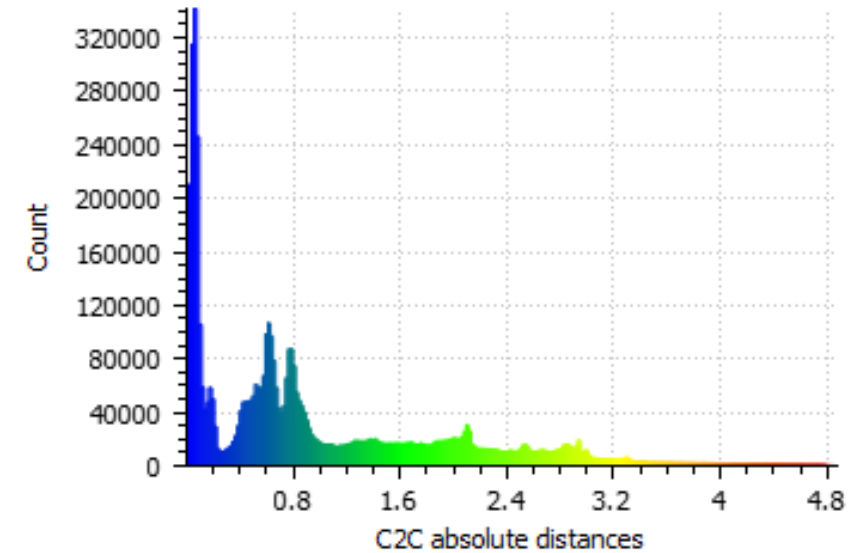
# Sv. Panteleimon, Skopje



# Point cloud from PLS ZEB REVO



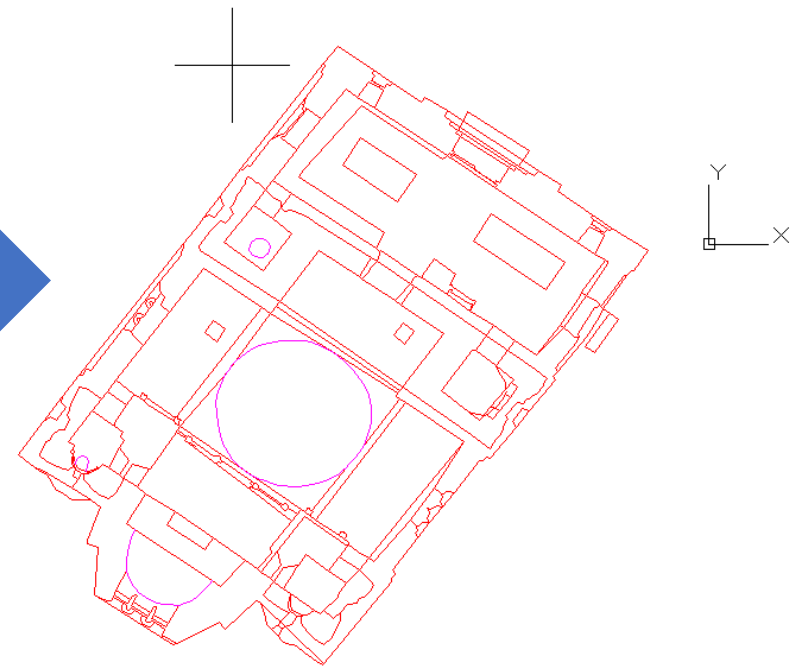
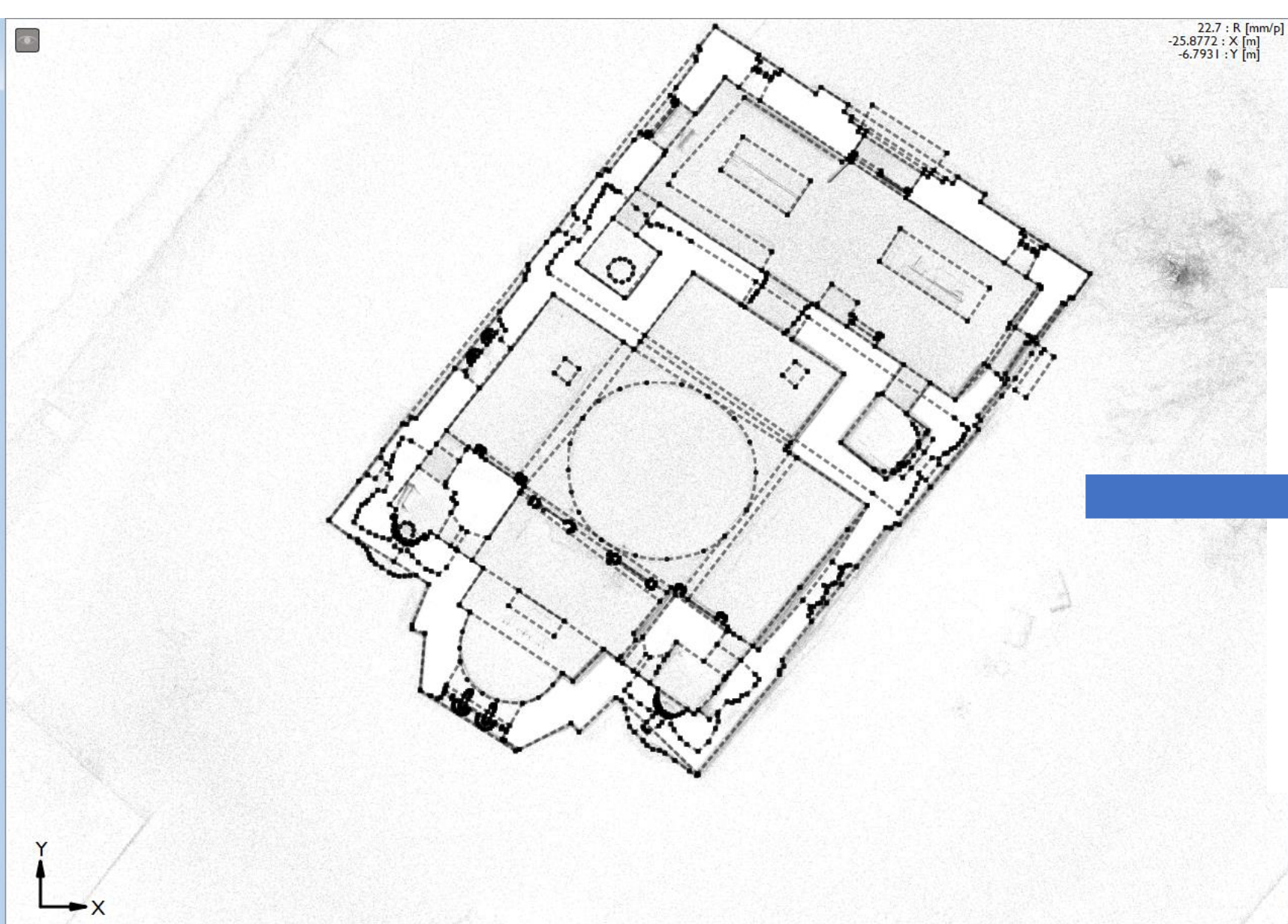
C2C absolute distances (5428106 values) [256 classes]

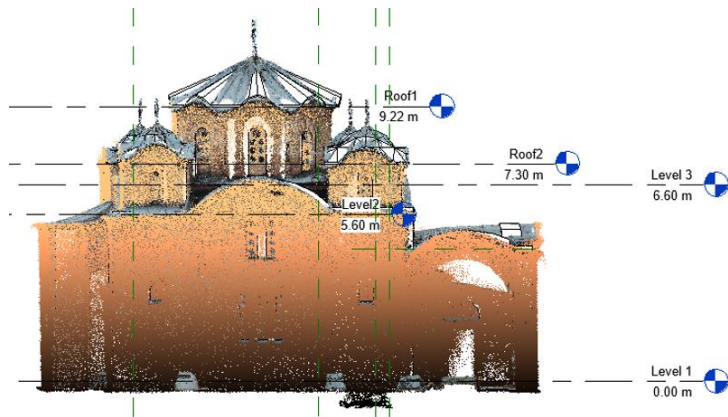


Differences between point cloud from combined terrestrial and aerial photogrammetry

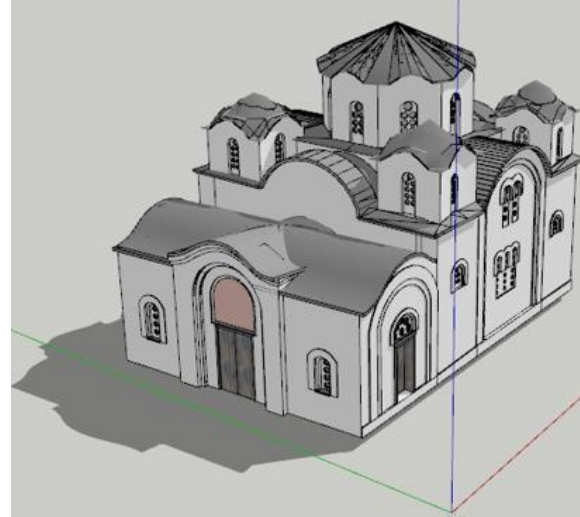
Device	Accuracy [mm] on 10 m	Range [m]	Acquiring points/sec	Data size [MB]	Time [minutes]
Nikon D3200	5-20	10	~30 photos/minute	~10/photo	~30 photos/minute
DJI Mavic Pro	5-30	30	~20 photos/minute	~4/photo	~20 photos/minute
ZEB-REVO	10-30	30	43000	100/min	slow walking
BLK360	4	30	360000	600/scan	6/scan



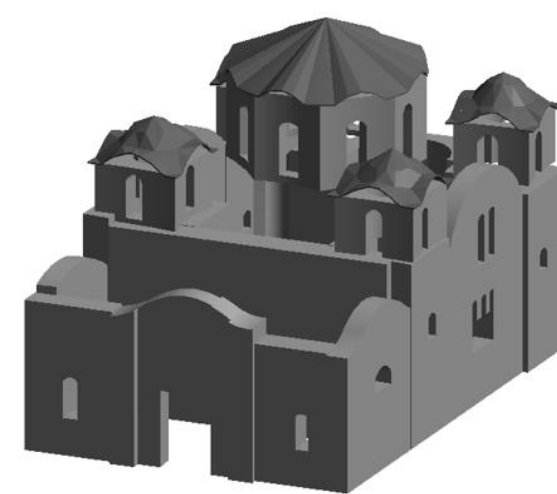




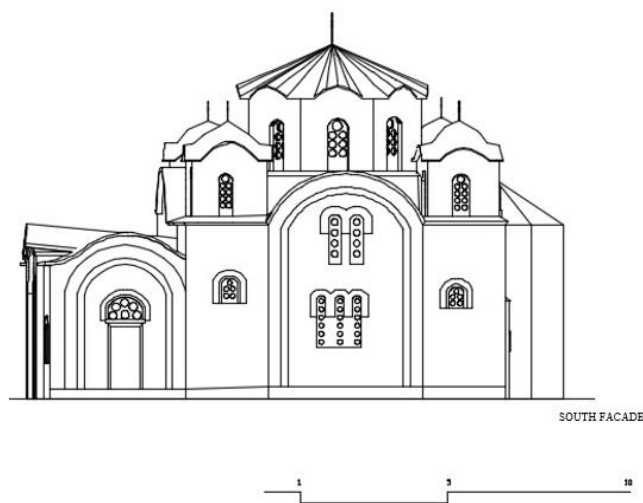
Defining of levels for creating of simplified model



Model from SketchUp



Model from Revit



Generated views from simplified models (SketchUp)



Generated VR model with texture (UnrealEngine)



VR model rendered in Lumion





Comparison of both 3D models: BIM geometrical basic model (grey), photogrammetrical model (blue)



# **Basics of photogrammetry**

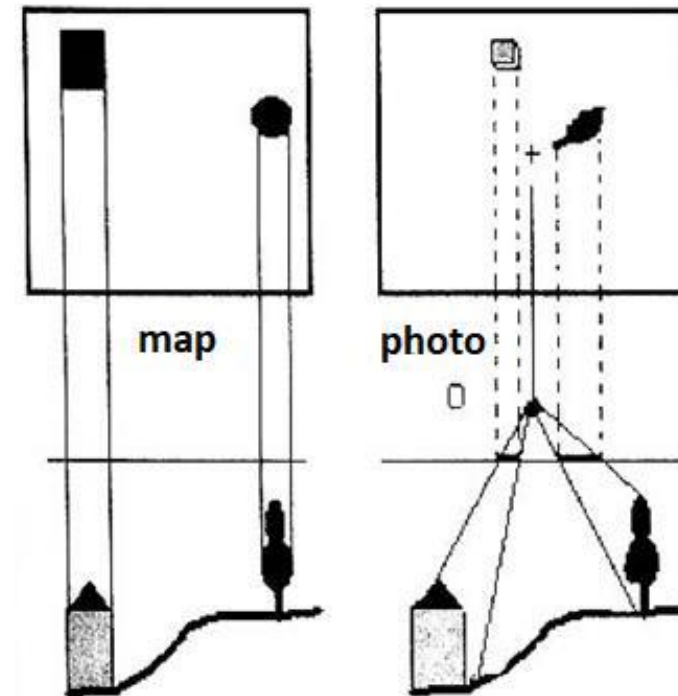
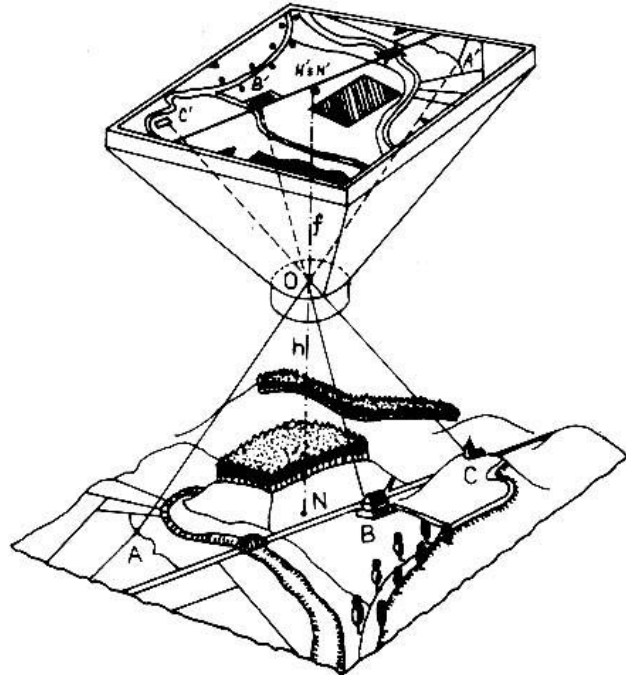
# *Basics of photogrammetry*



**Photographic image = central projection of the displayed object**

## **Input data:**

- image source of information necessary
- additional data geodetic coordinates of the ground control points , elements of internal and external orientation



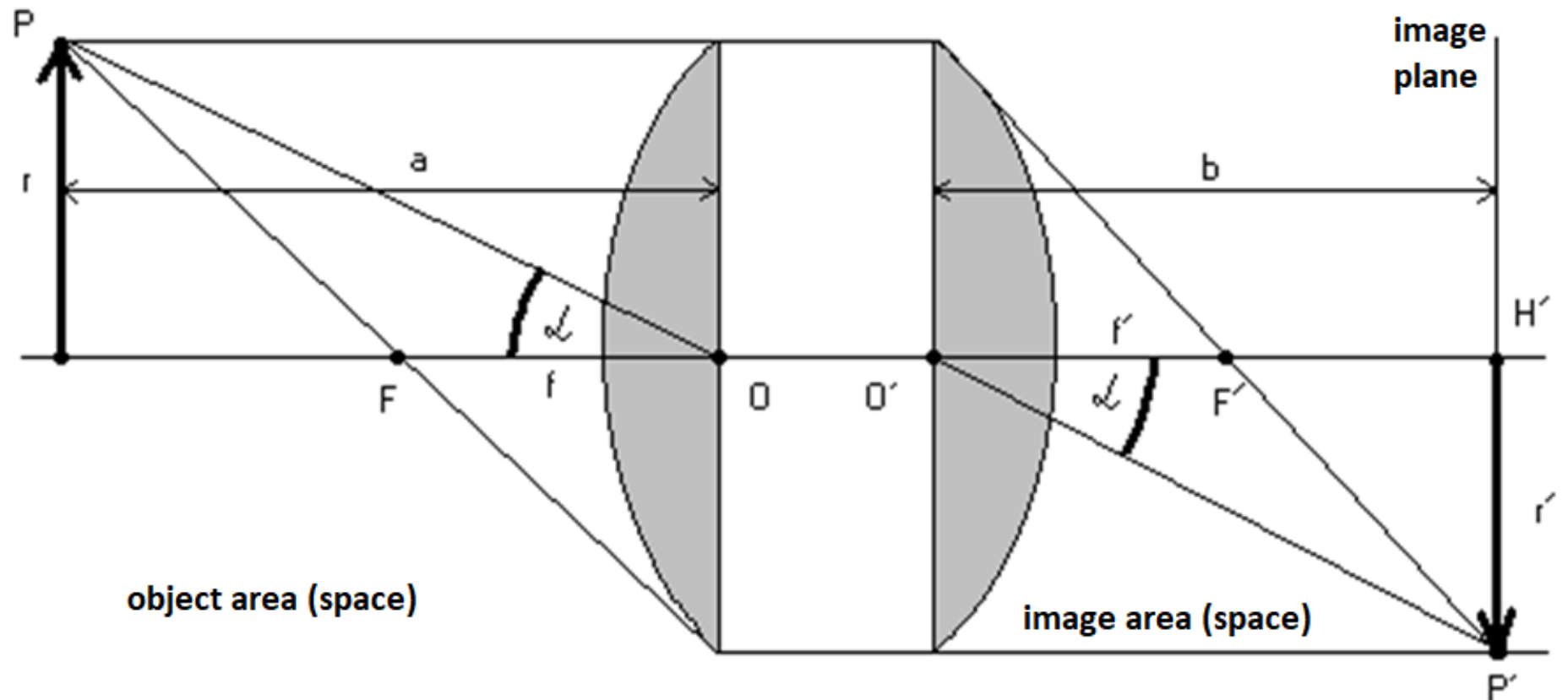


# Theory - optics



## *A real lens aperture*

- *reduces the number of rays that form an image*
- *$O$  Input pupila image of the aperture in the subject space*
- *$O'$  output pupila image of the aperture in the image space*
- *$f$  (camera lens ) constant distance  $O' H'$*



# Theory - optics

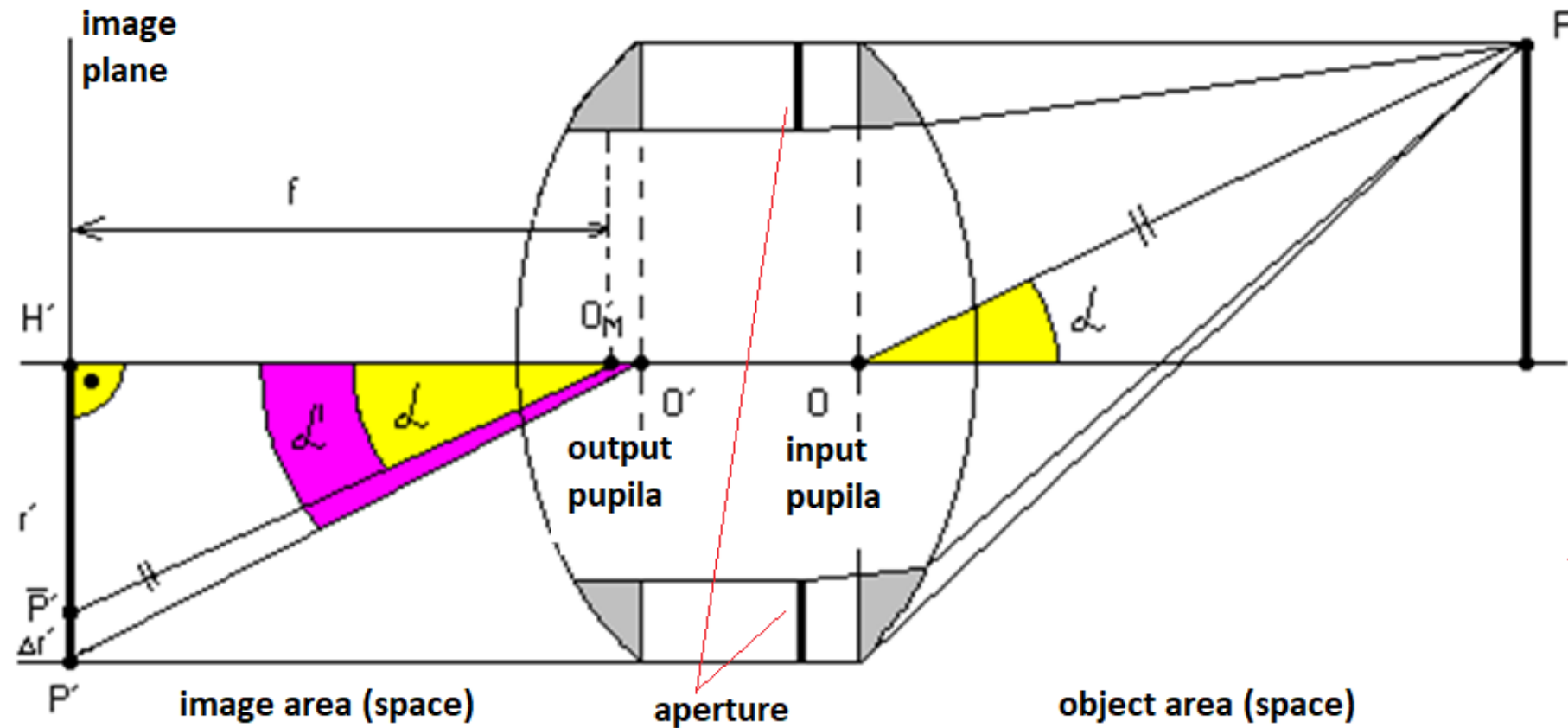
Real lens view

$$r' = f \cdot \tan \alpha + \Delta r'$$

$\Delta r'$  - effect of lens distortion



$$\alpha \neq \alpha'$$



# ***Summary of effects on the geometry of the lens view***



## **Aberrations**

**Optical defects can be sub divided into**

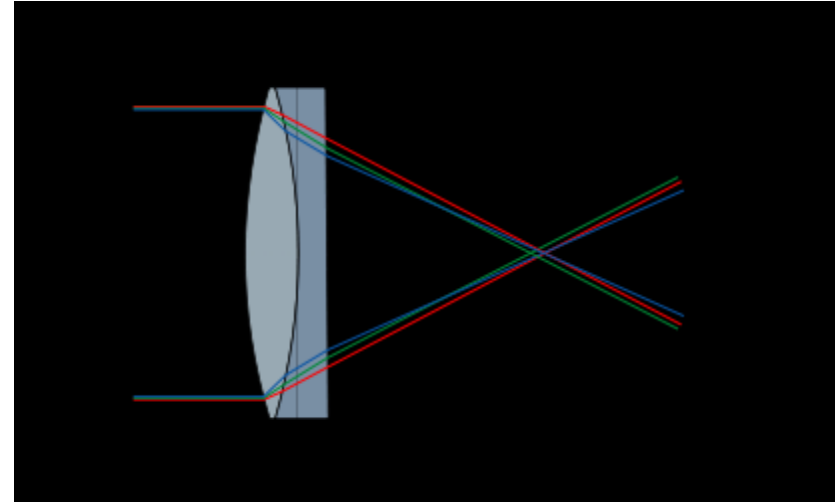
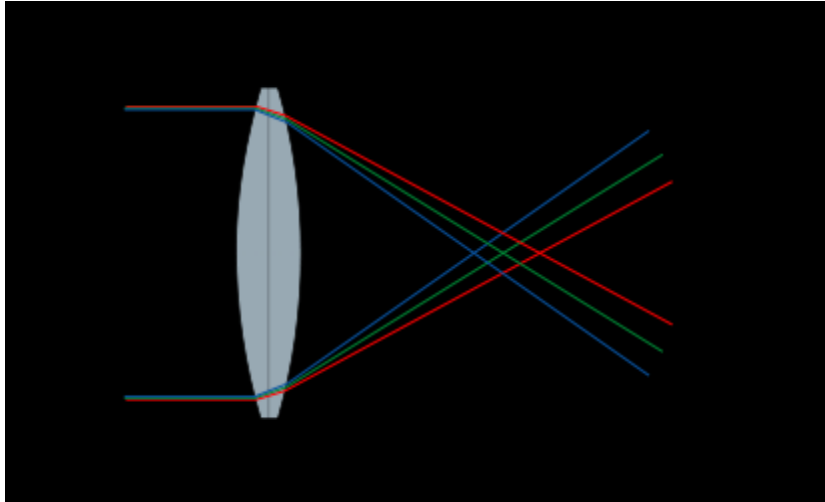
- a) monochrome**
- b) coloured**

**Furthermore,**

**- defects arising from**

- c) point imaging (spherical defect, astigmatism and coma)**
- d) imaging of the subject (field blurring and image distortion)**

# *Lens defects*



*Lens view chromatic colour defect (aberration )  
and its suppression*





# ***Coordinate systems***

Generally, three types of coordinate systems are used in the photogrammetry

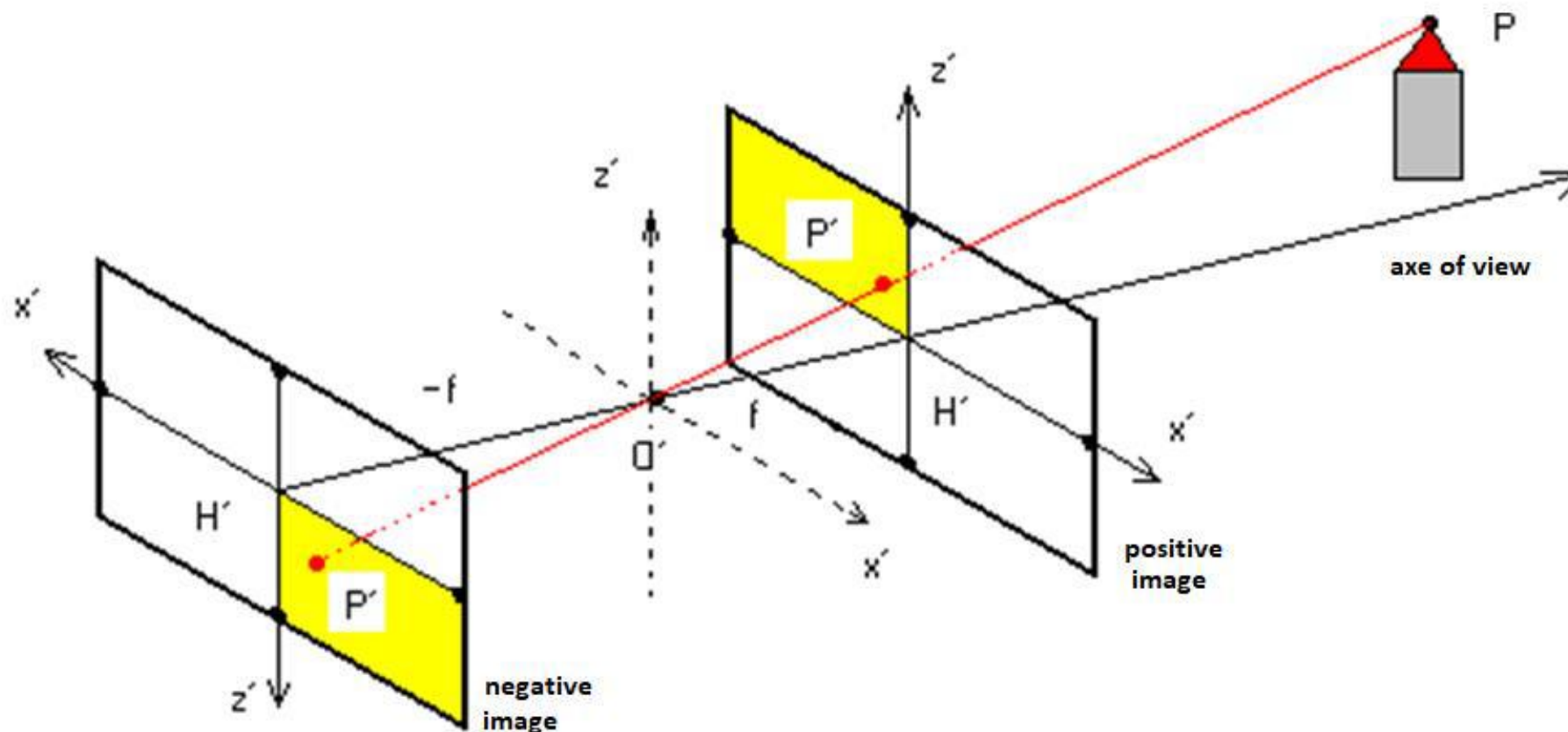
- a) main coordinate systems (system of geodetic coordinates)
- b) image coordinate system
- c) model coordinate system

auxiliary coordinate systems

- fictitious image coordinate system (3 image coordinates)
- the image coordinate system of an exactly vertical image



# *Elements of interior orientation*

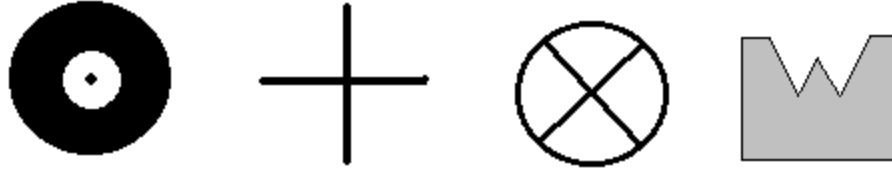


Camera constant , negative and positive, terrestrial configuration

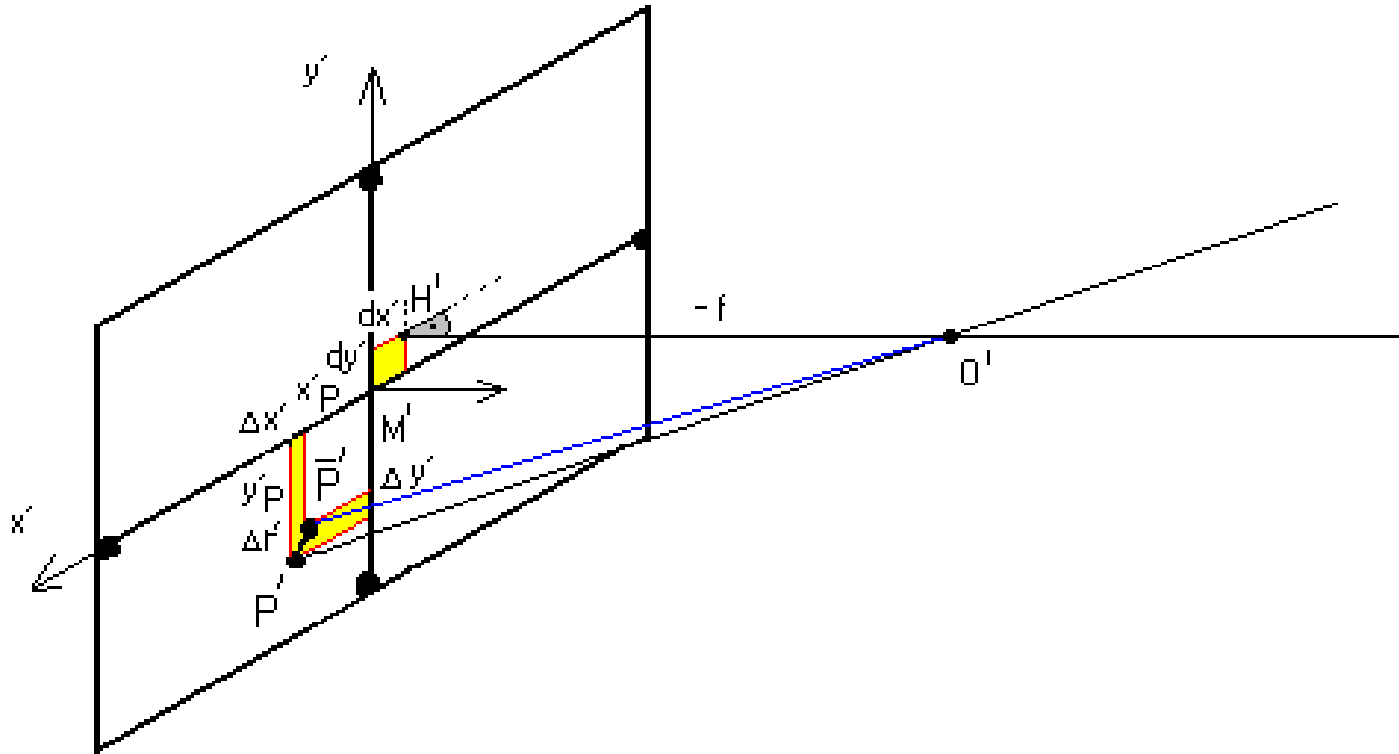
Elements of interior orientation :  $x_0'$ ,  $y_0'$ ,  $f$

(and known parametres of distortion)

# Elements of internal orientation



Different types of fiducial marks (on historical images or in historical cameras only)



*Definition of the elements of the internal orientation in the general configuration (image coordinates  $x'$ ,  $y'$ ); The axis of view is the perpendicular to the image plane passing through the object projection centre.*

# ***Coordinate systems and conversions***

# Elements of internal and external orientation

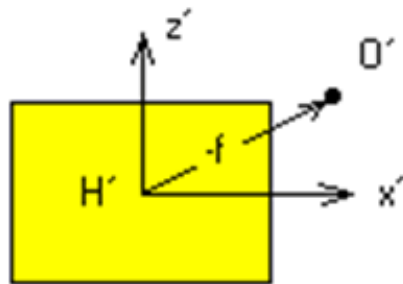
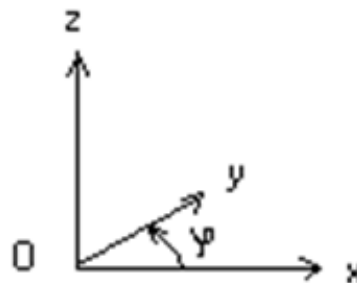
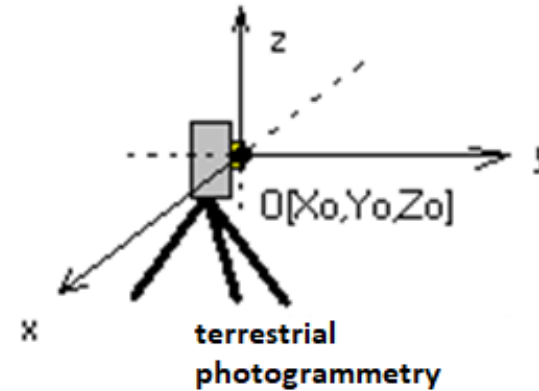


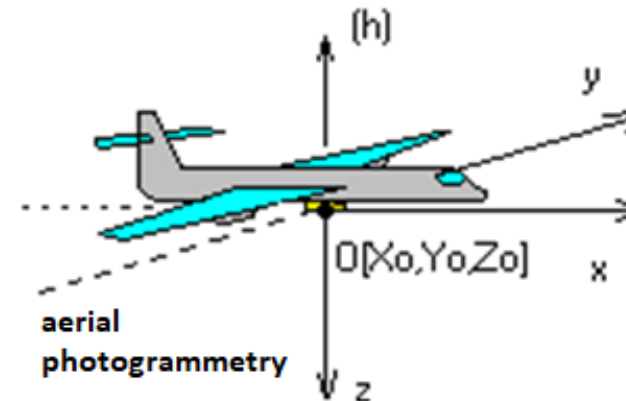
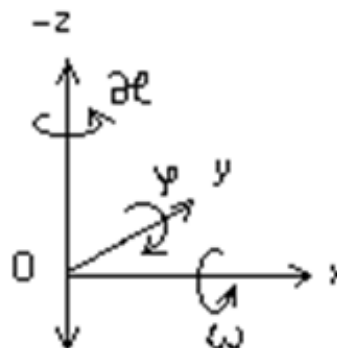
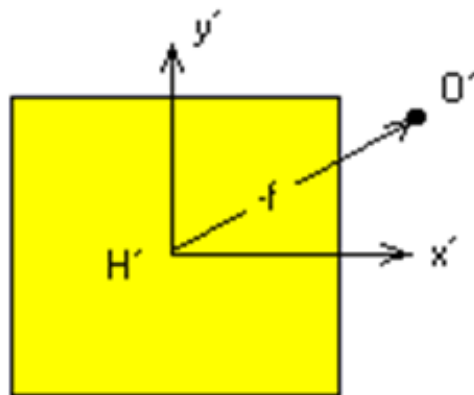
image coordinates



model coordinates



terrestrial  
photogrammetry



aerial  
photogrammetry

Internal and external orientation elements for terrestrial and aerial photogrammetry

# Coordinate systems



Image coordinate system label :  $x'$  ,  $y'$  , ( $z' = -f$ )

Model coordinate system label:  $x$  ,  $y$  ,  $z$

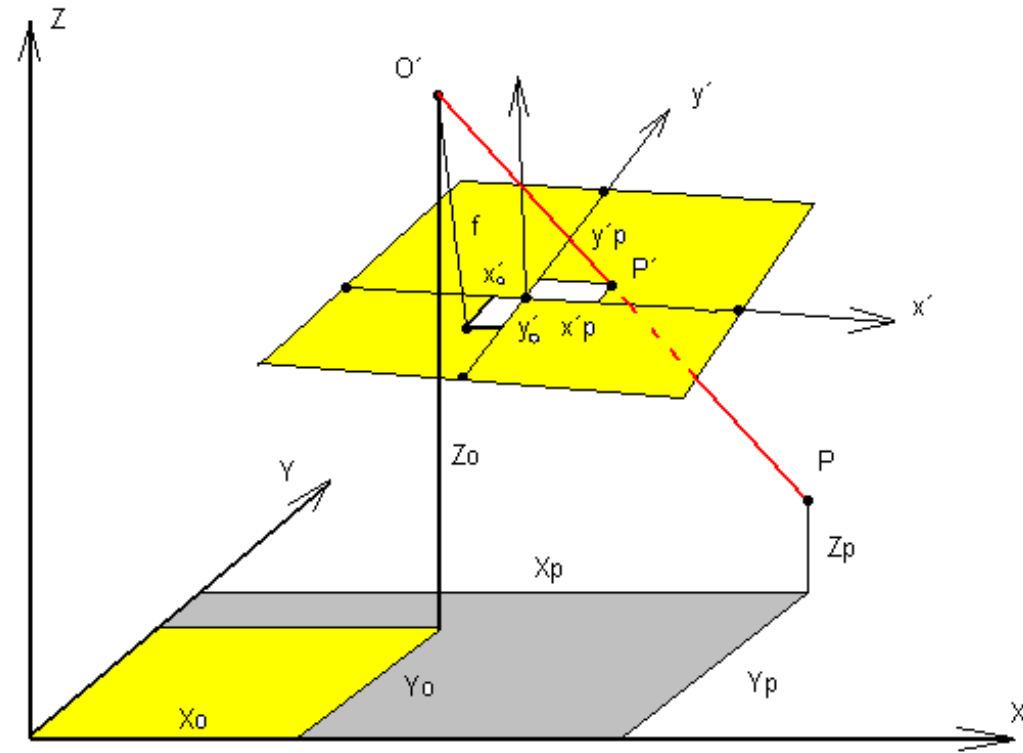
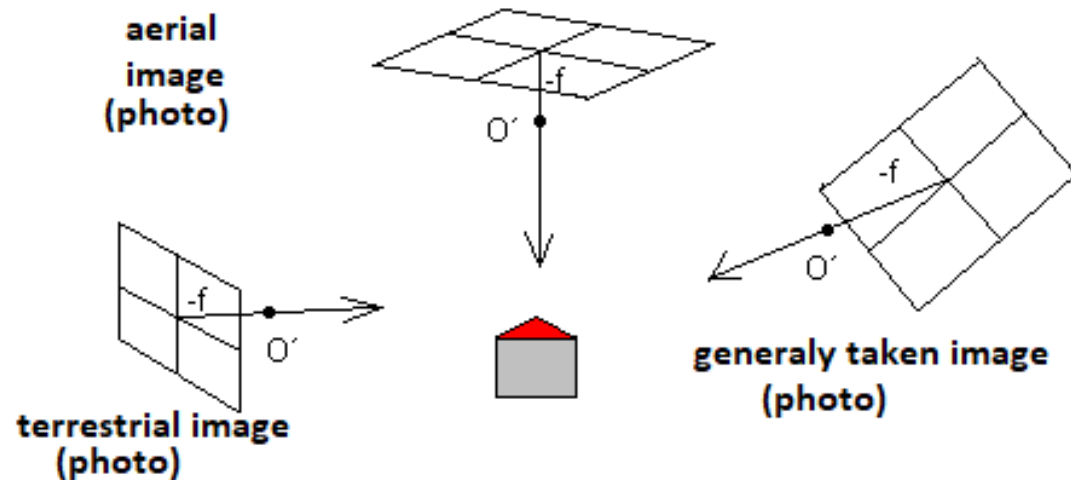
Geodetical system:  $X$  ,  $Y$  ,  $Z$

Auxiliary systems

Fictional image coordinate system :  $x'_F$  ,  $y'_F$  ,  $z'_F$

Vertical image coordinate system :  $x'_S$  ,  $y'_S$  ,  $z'_S$

Classic terrestrial , aerial  
and generally taken image



Coordinate systems in  
aerial photogrammetry

# Converting image information to geodetic systems



1) Restoration of internal orientation elements

2) External orientation

External orientations can be solved classically in two steps as:

1. **-relative orientation** (mutual orientation between the two stereo images, formation of an arbitrary spatially oriented stereo model)
2. **-absolute orientation** (rotation and displacement of the model into the geodetic reference system)
3. - in one step **using the Bundle Adjustment method** (*Bündelausgleichung*)

# Rotation matrix



Resulting rotation matrix  $R$

$$\mathbf{R}_{\omega\varphi} = \mathbf{R}_{\omega} \cdot \mathbf{R}_{\varphi}$$

$$\mathbf{R}_{\omega\varphi\kappa} = \mathbf{R}_{\omega\varphi} \cdot \mathbf{R}_{\kappa}$$

$$\mathbf{R}_{\omega\varphi\kappa} = \begin{pmatrix} \cos \varphi \cos \kappa & -\cos \varphi \sin \kappa & \sin \varphi \\ \sin \omega \sin \varphi \cos \kappa + \cos \omega \sin \kappa & -\sin \omega \sin \varphi \sin \kappa + \cos \omega \cos \kappa & -\sin \omega \cos \varphi \\ -\cos \omega \sin \varphi \cos \kappa + \sin \omega \sin \kappa & \cos \omega \sin \varphi \sin \kappa + \sin \omega \cos \kappa & \cos \omega \cos \varphi \end{pmatrix}$$

$$\tan \omega = -\frac{r_{23}}{r_{33}}, \sin \varphi = r_{13}, \tan \kappa = -\frac{r_{12}}{r_{11}}$$

$$\mathbf{R} = \begin{pmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{pmatrix}$$

Here it is important to note that  $r_{13} = \sin > 0$  in the 1st and 2nd quadrants and further that  $r_{13} = \sin < 0$  in the 3rd and 4th quadrants. Thus, the rotation is not uniquely determined. The quadrants of the other two rotations, are uniquely determined given the expressions from which we calculate them. **Thus we get a total of two sets of rotations, to a single rotation matrix  $R$ .**





# ***Derivation of mathematical relations***

# Direct relationship between image and geodetic coordinates



collinear frame-model relationship

$$\frac{x' - x'_0}{-f} = \frac{x - x_0}{z - z_0}, \quad \frac{y' - y'_0}{-f} = \frac{y - y_0}{z - z_0}$$

the model coordinate system can be converted to a geodetic system by rotations around three axes

$$\begin{pmatrix} X - X_0 \\ Y - Y_0 \\ Z - Z_0 \end{pmatrix} = \mathbf{R} \cdot \begin{pmatrix} x - x_0 \\ y - y_0 \\ z - z_0 \end{pmatrix}, \quad \mathbf{R} = \begin{pmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{pmatrix}$$
$$\begin{pmatrix} x - x_0 \\ y - y_0 \\ z - z_0 \end{pmatrix} = \mathbf{R}^T \cdot \begin{pmatrix} X - X_0 \\ Y - Y_0 \\ Z - Z_0 \end{pmatrix}$$

**the direct relationship between image and geodetic coordinates, which is the basis of all contemporary photogrammetry:**

$$x' = x'_0 - f \frac{r_{11}(X - X_0) + r_{21}(Y - Y_0) + r_{31}(Z - Z_0)}{r_{13}(X - X_0) + r_{23}(Y - Y_0) + r_{33}(Z - Z_0)}$$
$$y' = y'_0 - f \frac{r_{12}(X - X_0) + r_{22}(Y - Y_0) + r_{32}(Z - Z_0)}{r_{13}(X - X_0) + r_{23}(Y - Y_0) + r_{33}(Z - Z_0)}$$

# Photogrammetric series



Finally, these expressions need to be supplemented by the effect of translation

$$\Delta x' = -y'd\kappa' - \left( f + \frac{x'^2}{f} \right) d\varphi' + \frac{x'y'}{f} d\omega' + db'_x + \frac{x'}{f} db'_z$$

$$\Delta y' = x'd\kappa' - \frac{x'y'}{f} d\varphi' + \left( f + \frac{y'^2}{f} \right) d\omega' + db'_y + \frac{y'}{f} db'_z$$

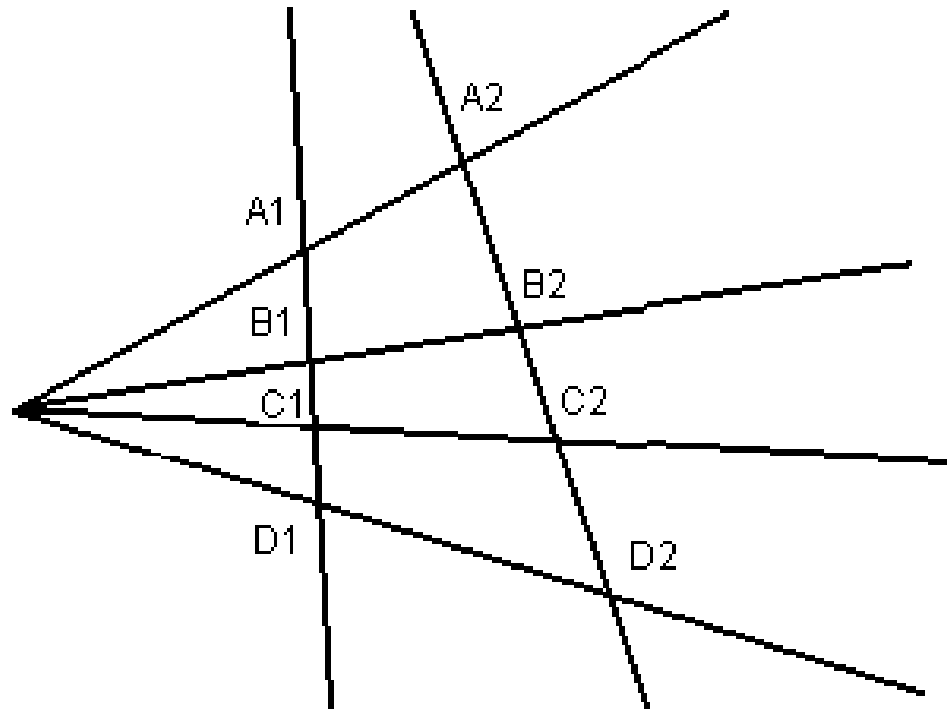
The term is called "**complete photogrammetric series**", or historically Gruber series, and is used in simplified theoretical derivations. The meaning and use of series was quite fundamental, especially in the era of analogue photogrammetry.

# ***Methods of photogrammetry***

# Single-shot photogrammetry



- *relationship between two planes*



Mathematical expression  
in fact, the **collinear transformation**

**Papp's theorem:**

*The point or ray quadrature  
binary ratio is preserved in the  
map and image planes.*

$$\frac{\frac{A_1 C_1}{B_1 C_1}}{\frac{A_1 D_1}{B_1 D_1}} = \frac{\frac{A_2 C_2}{B_2 C_2}}{\frac{A_2 D_2}{B_2 D_2}}$$

$$X = \frac{a_1 x' + a_2 y' + a_3}{c_1 x' + c_2 y' + 1}$$

$$Y = \frac{b_1 x' + b_2 y' + b_3}{c_1 x' + c_2 y' + 1}$$

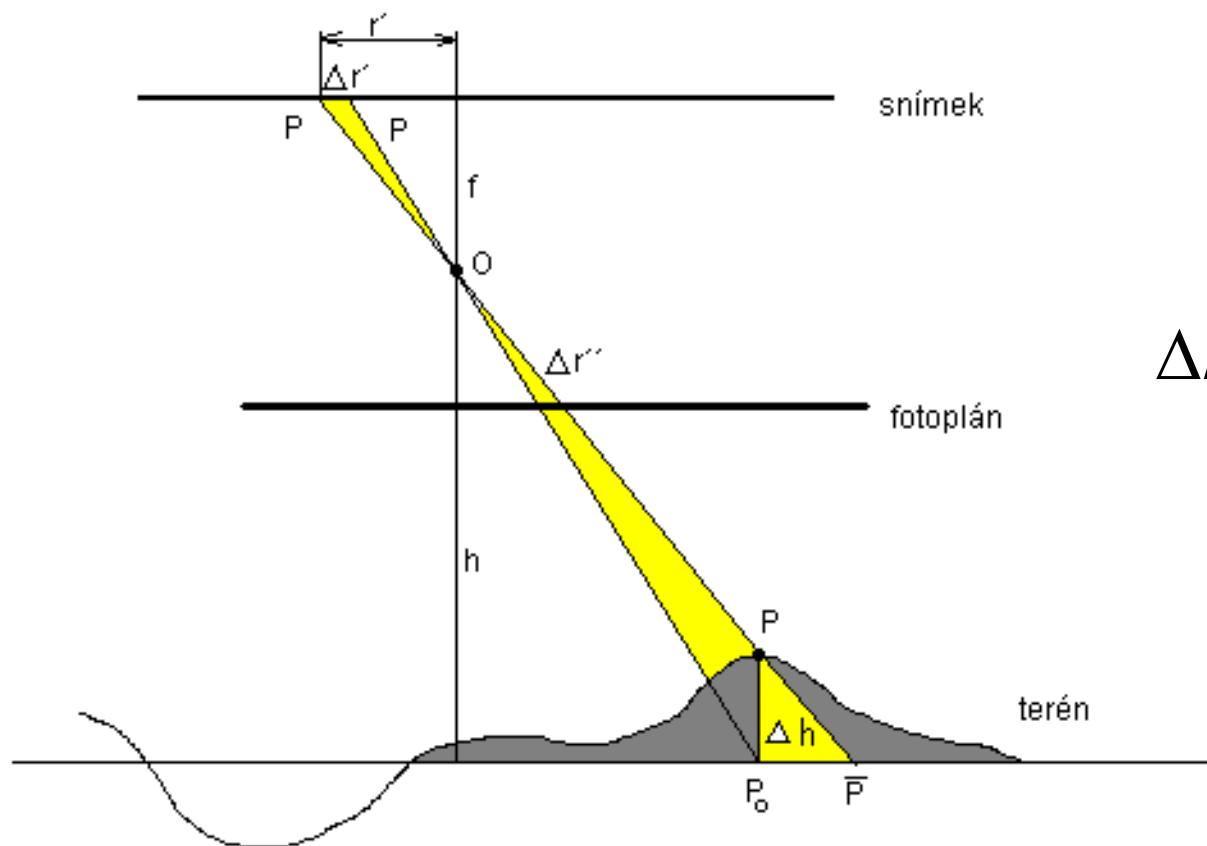




# Effect of height zoning



$$\Delta r'' = \frac{\Delta h \cdot r'}{f \cdot m_F}$$



$$\Delta h_{\max} = \frac{f \cdot m_F \cdot \Delta r''_{\max}}{r'}$$

# Digital redrawing



*Original image and photo plan, taken by the measuring camera (left),  
an image taken with an ordinary camera and its digitally redrawn form - an image vault,  
due to uncorrected radial distortion is clearly visible (right)*

# Solution



$$X = \frac{a_1 x' + a_2 y' + a_3}{c_1 x' + c_2 y' + 1}$$

$$Y = \frac{b_1 x' + b_2 y' + b_3}{c_1 x' + c_2 y' + 1}$$

$$X = a_1 x' + a_2 y' + a_3 - c_1 x' X - c_2 y' X$$

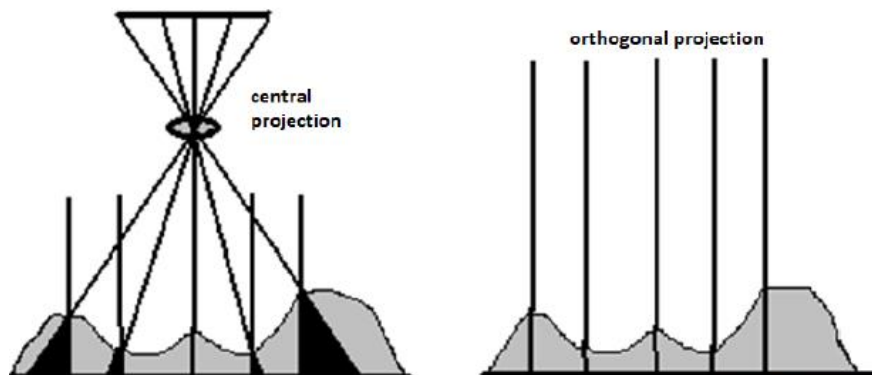
$$Y = b_1 x' + b_2 y' + b_3 - c_1 x' Y - c_2 y' Y$$

$$\begin{pmatrix} x'_1 & y'_1 & 1 & 0 & 0 & 0 & -x'_1 X_1 & -y'_1 X_1 \\ 0 & 0 & 0 & x'_1 & y'_1 & 1 & -x'_1 Y_1 & -y'_1 Y_1 \\ x'_2 & y'_2 & 1 & 0 & 0 & 0 & -x'_2 X_2 & -y'_2 X_2 \\ 0 & 0 & 0 & x'_2 & y'_2 & 1 & -x'_2 Y_2 & -y'_2 Y_2 \\ x'_3 & y'_3 & 1 & 0 & 0 & 0 & -x'_3 X_3 & -y'_3 X_3 \\ 0 & 0 & 0 & x'_3 & y'_3 & 1 & -x'_3 Y_3 & -y'_3 Y_3 \\ x'_4 & y'_4 & 1 & 0 & 0 & 0 & -x'_4 X_4 & -y'_4 X_4 \\ 0 & 0 & 0 & x'_4 & y'_4 & 1 & -x'_4 Y_4 & -y'_4 Y_4 \end{pmatrix} \cdot \begin{pmatrix} a_1 \\ a_2 \\ a_3 \\ b_1 \\ b_2 \\ b_3 \\ c_1 \\ c_2 \end{pmatrix} = \begin{pmatrix} X_1 \\ Y_1 \\ X_2 \\ Y_2 \\ X_3 \\ Y_3 \\ X_4 \\ Y_4 \end{pmatrix}$$

$$\mathbf{A} \cdot \mathbf{a} = \mathbf{X}$$

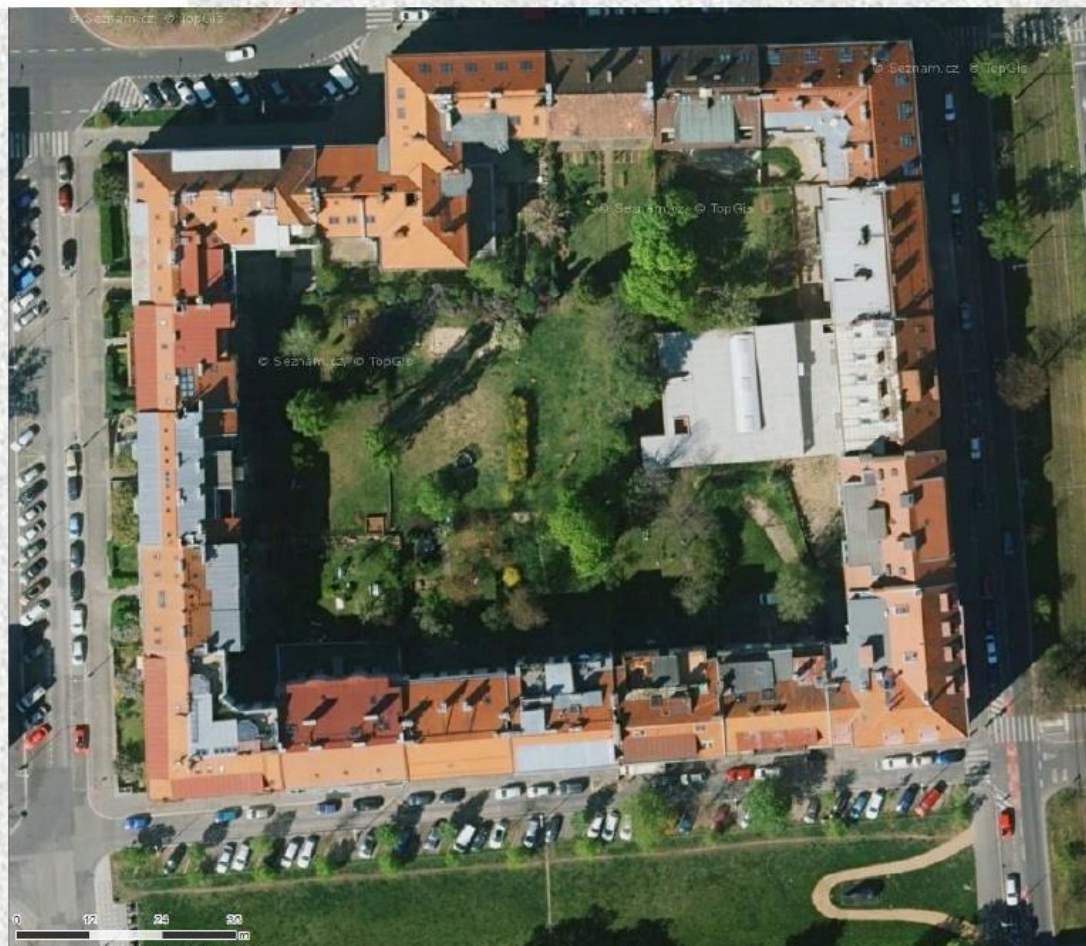
$$\mathbf{a} = \mathbf{A}^{-1} \cdot \mathbf{X}$$





# Digital orthophoto

Converting the central projection to orthogonal - to orthophoto - allows you to work with the image information as a map and insert it as a data layer in GIS.





# Digital orthophoto

*Digital orthophoto is a photogrammetric product - image conversion with central projection to orthogonal projection*



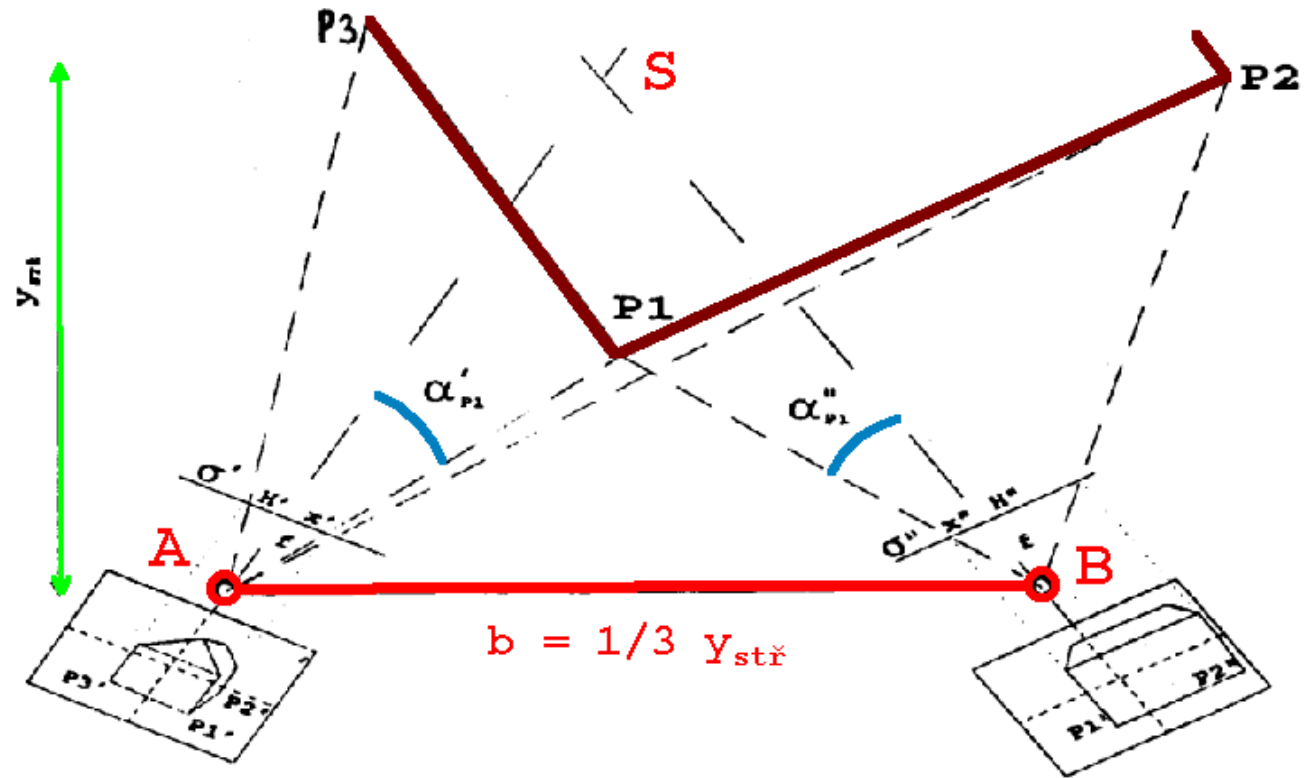
*For creation:  
Required image with known elements of  
internal and external orientation and DMT*

*Ortophoto and true ortophoto*

*The problem of mosaicking  
- seamless orthophoto*



# Multi-frame photogrammetry - cross-sectional



The oldest photogrammetric method  
- based on intersection of rays  
- today only in digital form

# Today's solution

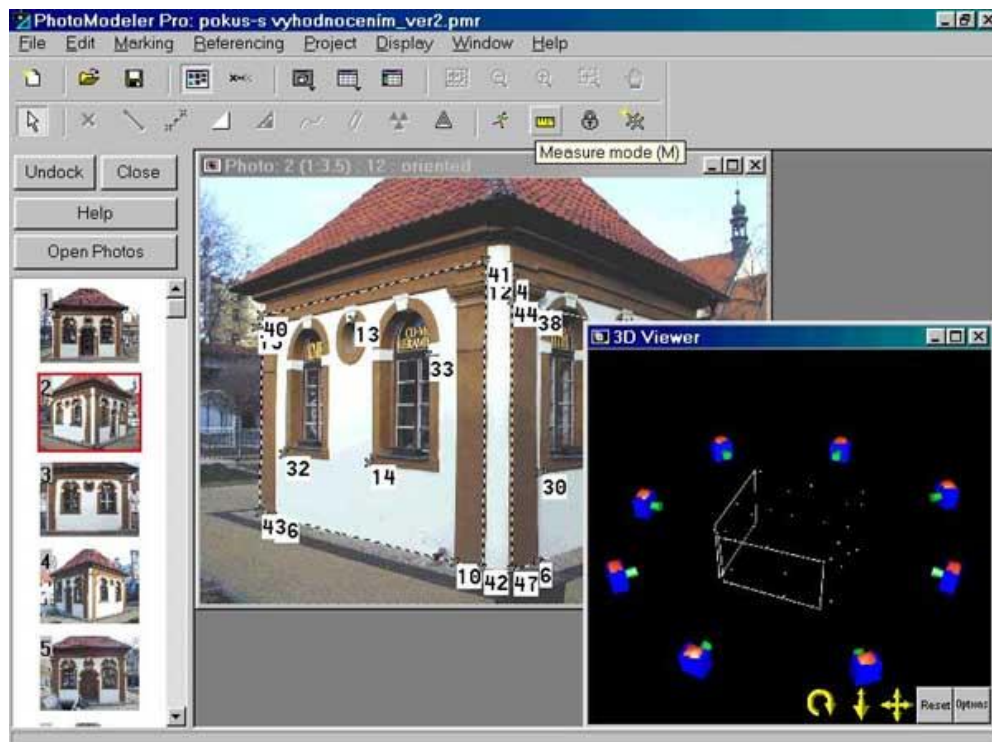
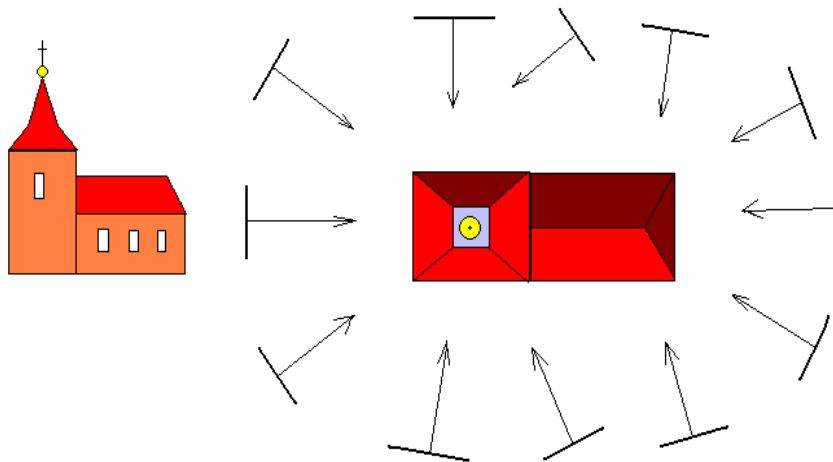


$$X = X_0 + (Z - Z_0) \frac{r_{11}(x' - x'_0) + r_{12}(y' - y'_0) - r_{13}f}{r_{31}(x' - x'_0) + r_{32}(y' - y'_0) - r_{33}f}$$

$$Y = Y_0 + (Z - Z_0) \frac{r_{21}(x' - x'_0) + r_{22}(y' - y'_0) - r_{23}f}{r_{31}(x' - x'_0) + r_{32}(y' - y'_0) - r_{33}f}$$

$$\begin{pmatrix} x' - x'_0 + \Delta x' \\ y' - y'_0 + \Delta y' \\ -f \end{pmatrix} = m \cdot \mathbf{R}^T \cdot \begin{pmatrix} X - X_0 \\ Y - Y_0 \\ Z - Z_0 \end{pmatrix}$$

# Cross-sectional photogrammetry



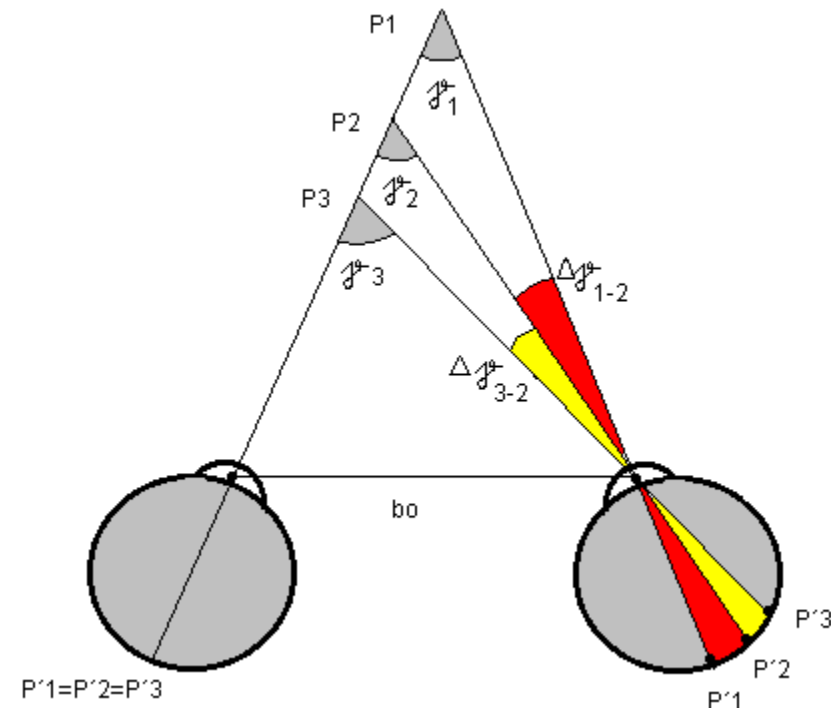
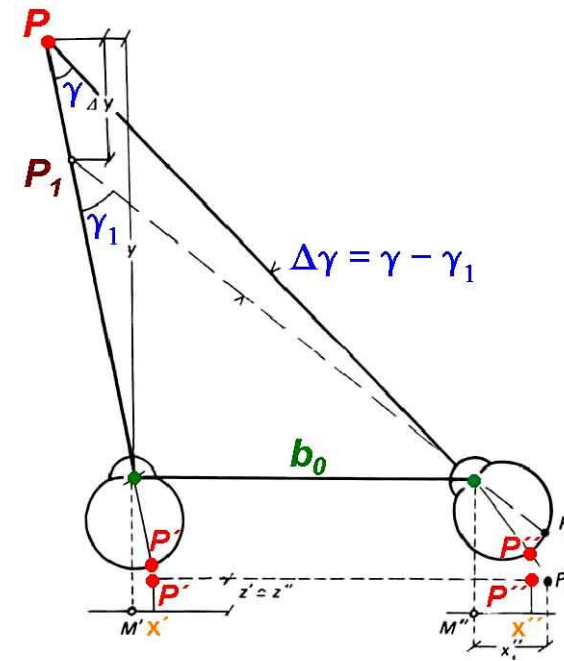
# Stereophotogrammetry

Stereophotogrammetric method introduced at the beginning of the 20th century (Pulfrich)

Evaluation based on stereoscopic perception also for non-signalized points

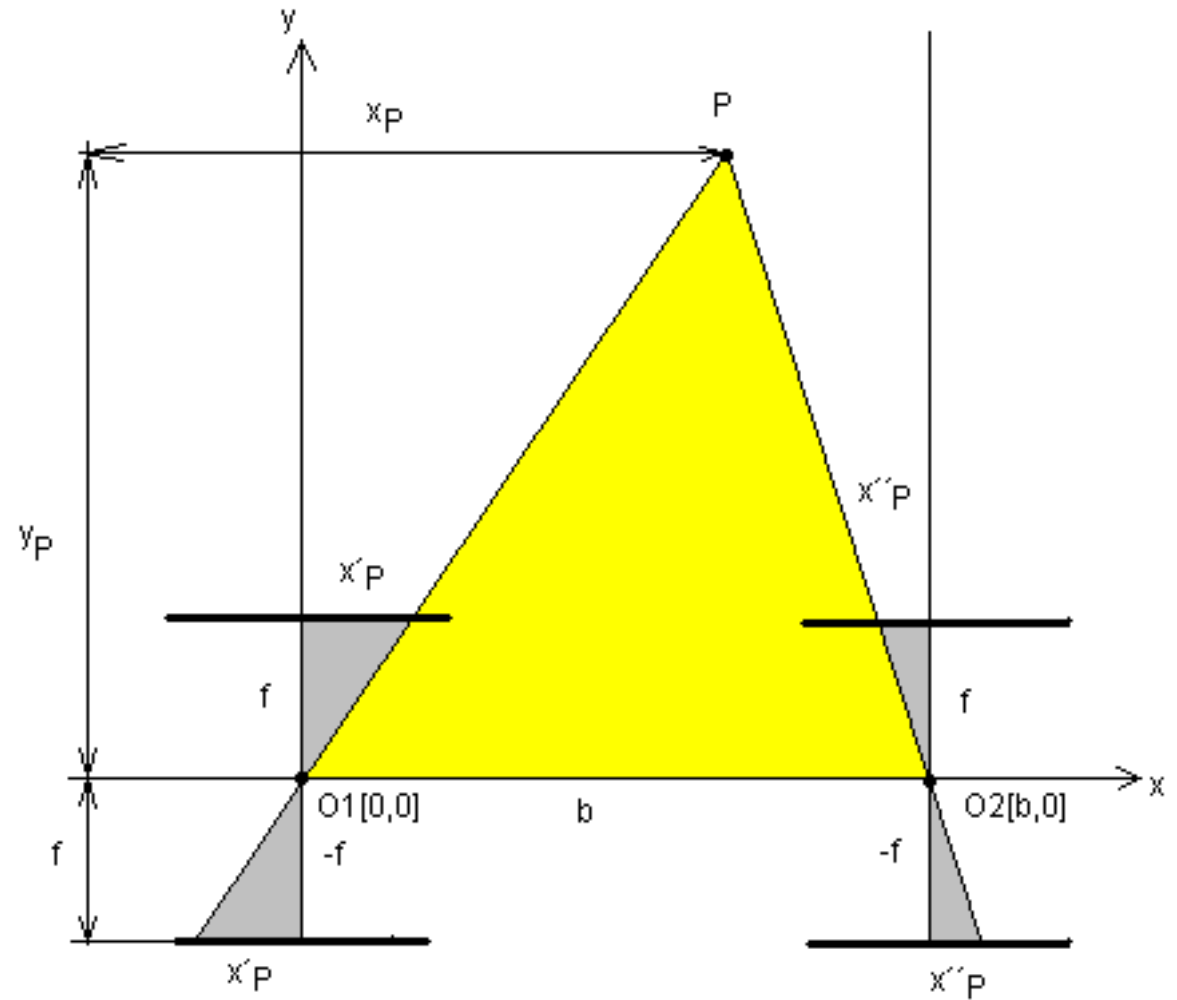
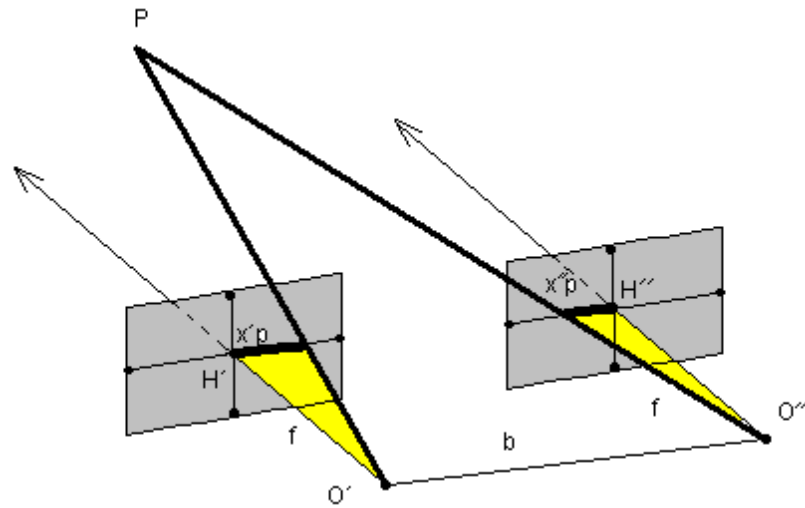
Photogrammetric stereoscopic observation and evaluation

- artificial stereoscopic perception based on the natural perception of healthy eyes





# Solution





# Terrestrial stereophotogrammetry - normal case

In terrestrial applications,  
standardization of the external  
orientation elements can be ensured

**R=E**

$$x = \frac{b \cdot x'}{p} \quad y = \frac{b \cdot f}{p} \quad z = \frac{b \cdot z'}{p}$$

**b (AB) base**

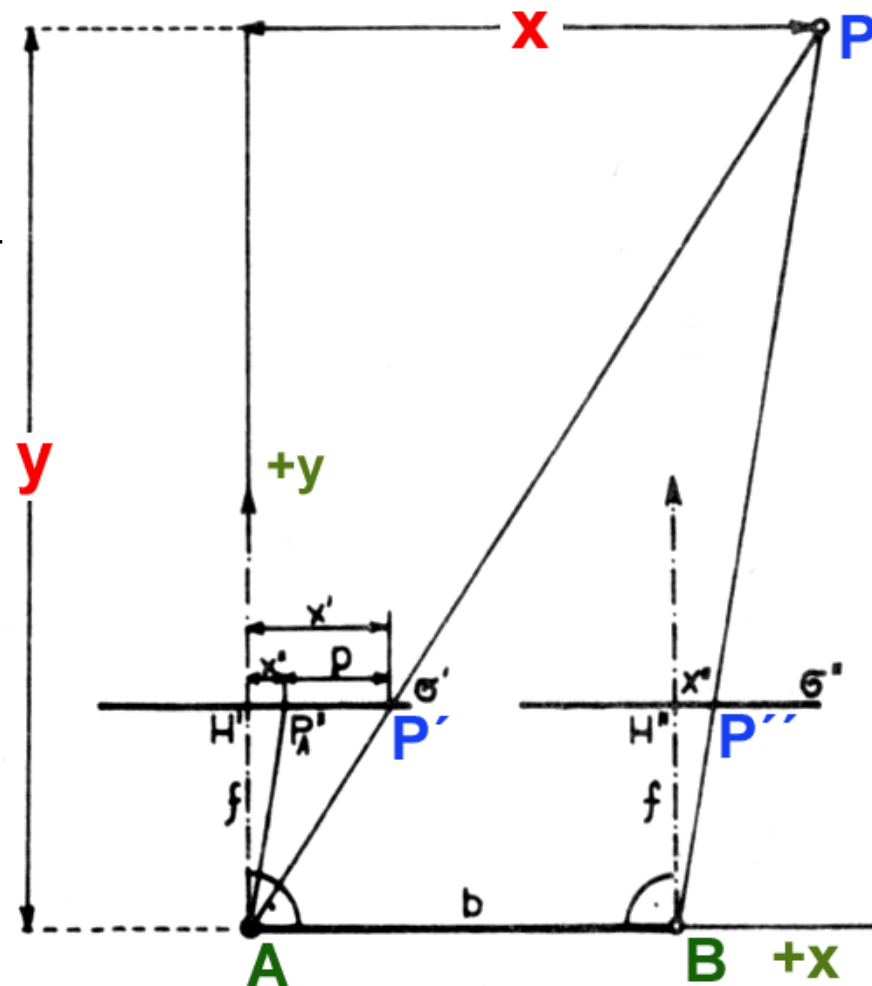
**x y (z) model system**

**', '' image planes**

**x', x'', z', z'' image coordinates**

**p parallax**

**f chamber constant**



# Accuracy of photogrammetry



$$\frac{y}{f} = \frac{b}{p}$$

$$x = \frac{b \cdot x'}{p} \quad y = \frac{b \cdot f}{p} \quad z = \frac{b \cdot z'}{p}$$

$$x = y \frac{x'}{f} \quad z = y \frac{z'}{f}$$

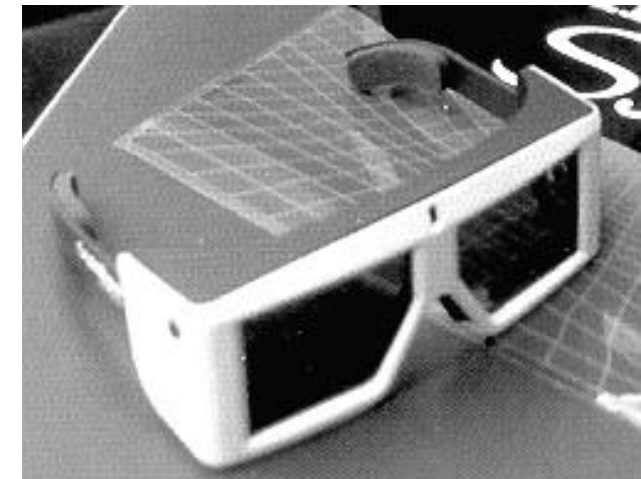
$$y = \frac{b \cdot f}{p}, \quad dy = \frac{f}{p} db + \frac{b}{p} df - \frac{bf}{p^2} dp$$

$$dy = -\frac{b \cdot f}{p^2} dp, \quad p^2 = \left( \frac{b \cdot f}{y} \right)^2$$

$$dy = -\frac{y \cdot y}{b \cdot f} dp$$

$$m_y = \pm \frac{y \cdot y}{b \cdot f} m_P$$

# *Device for stereoscopic perception*



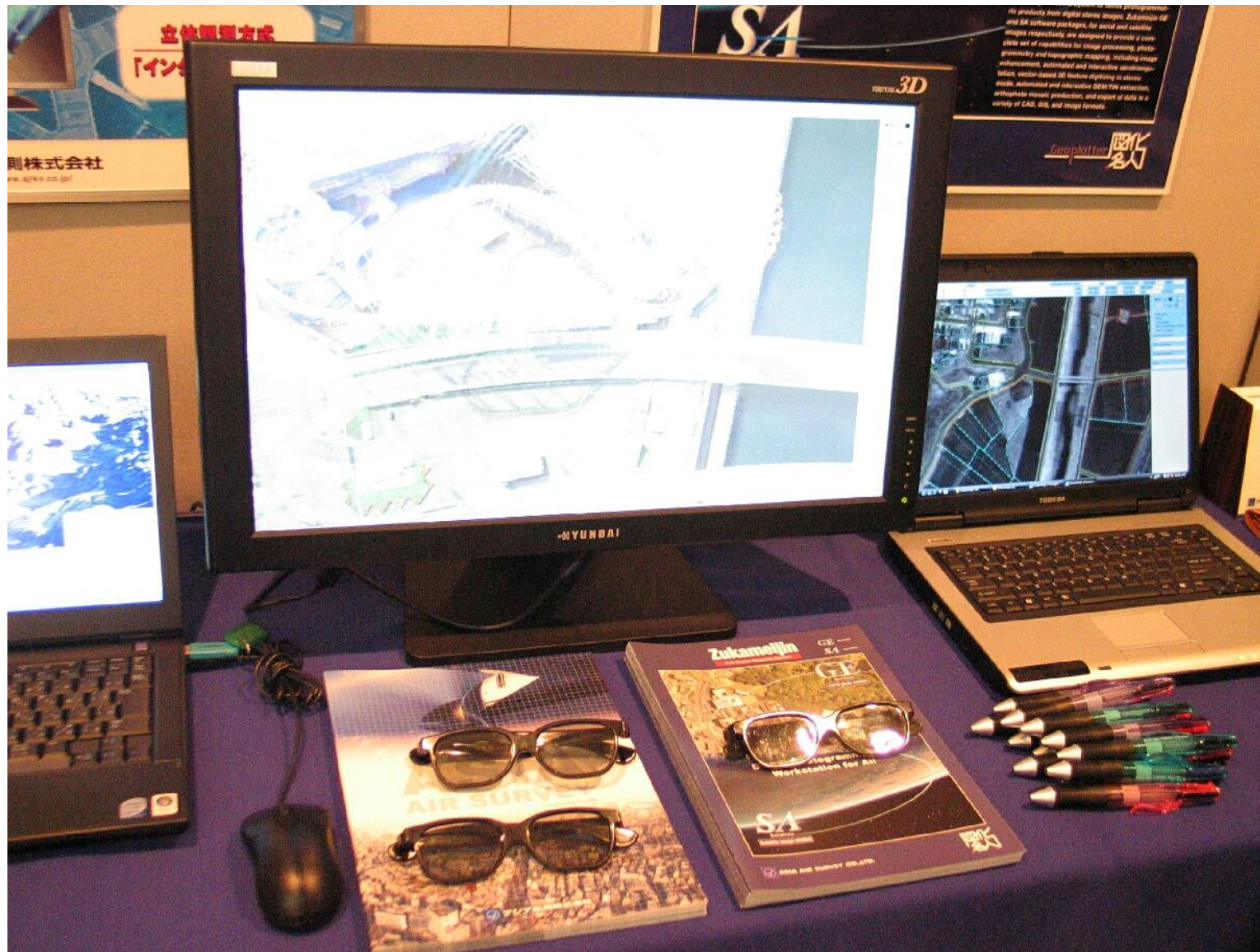


*new solutions*





# *new solutions*



# The emergence of the digital image

A **digital image** is an image in digital form (expressed in numbers). It is created either primarily by digital capture devices or by scanning analogue images. A digital image consists of individual pixels,

(from English *picture elements*) taking certain values which are not arbitrary (determined by technical possibilities of the computer and coding).

$$P[i, j] = f(i, j)$$

$f(i, j)$	$f(i, j+1)$	$f(i, j+2)$	$f(i, j+3)$	$f(i, j+4)$
$f(i+1, j)$	$f(i+1, j+1)$	$f(i+1, j+2)$	$f(i+1, j+3)$	$f(i+1, j+4)$
$f(i+2, j)$	$f(i+2, j+1)$	$f(i+2, j+2)$	$f(i+2, j+3)$	$f(i+2, j+4)$
.....				
.....				$f(m, n)$

$$M = m \cdot n \cdot e \text{ [byte]}$$

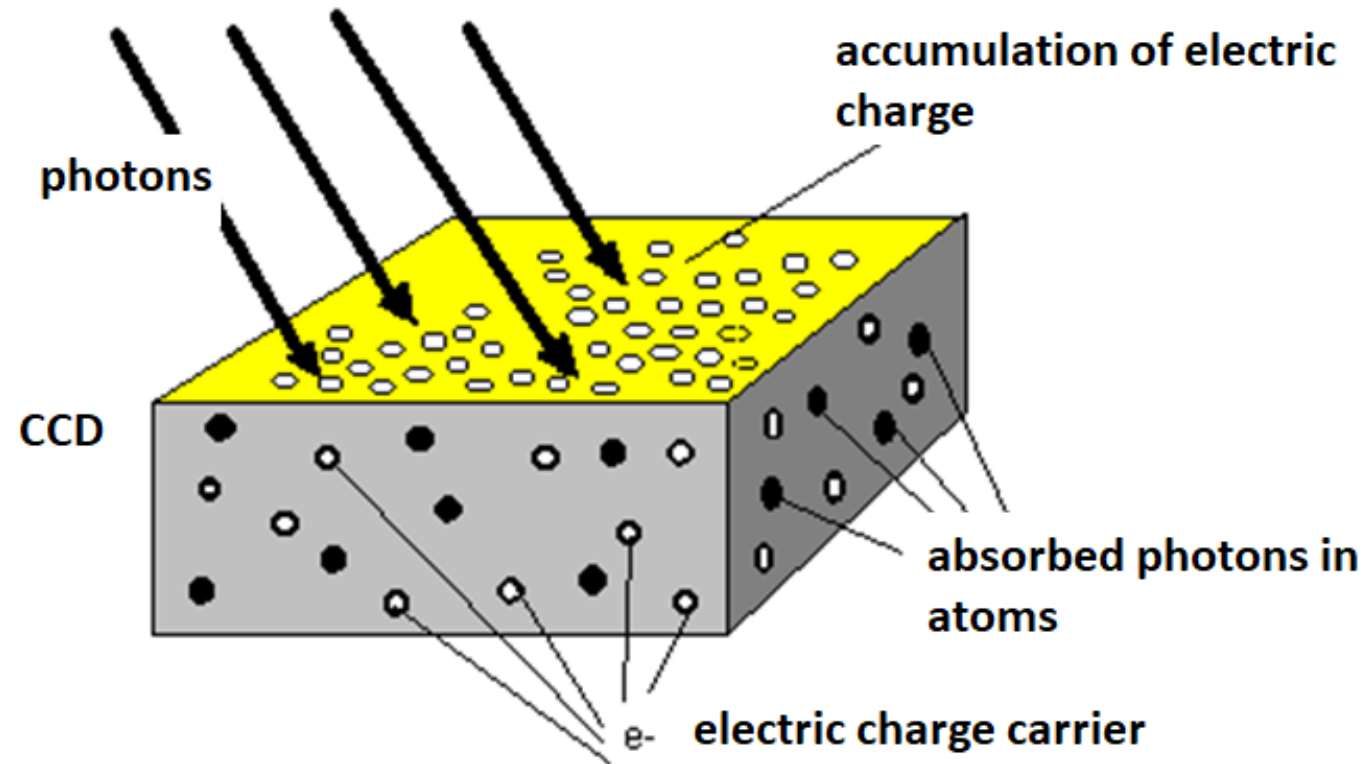


# ***The origin of the image***

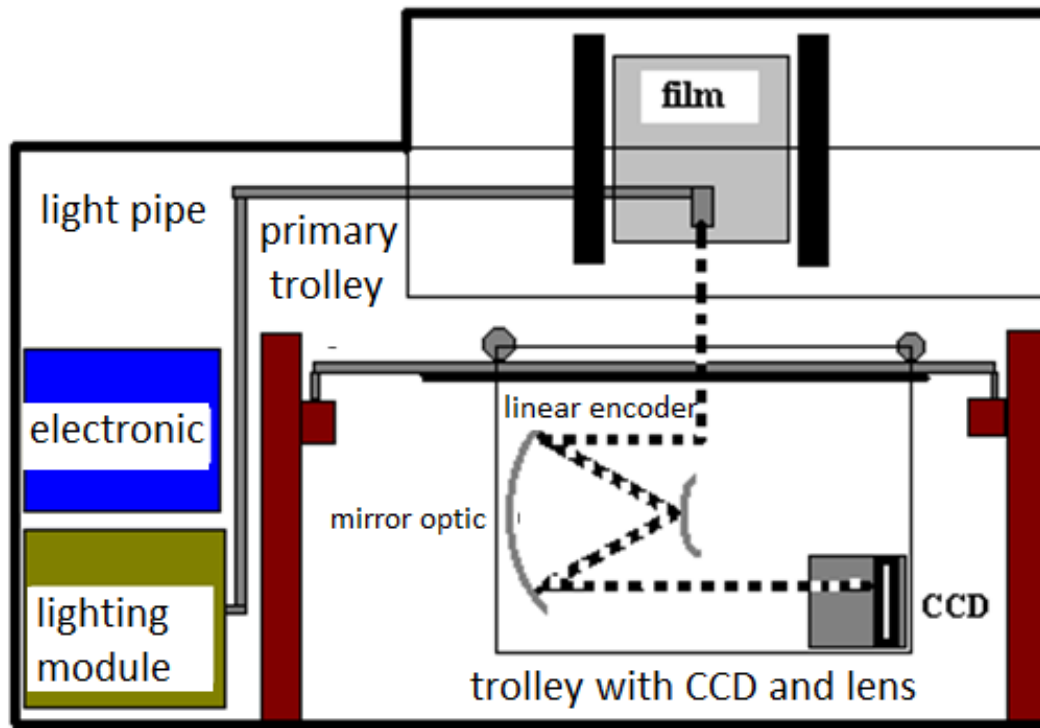
The most common type of detector is the CCD element. The name is derived from the name of the element in English "*Charge Coupled Device*".

CMOS (*Complementary Metal Oxide Semiconductor*) is a transistor-based electronic component. Compared to a CCD, it is simpler to manufacture, smaller, up to 80% cheaper, and consumes less power than a CCD (only 1%!).

Photocell - the principle of its function is generally the same with CCD detectors, differing mainly in size



# *Secondary digital image formation: by scanning*

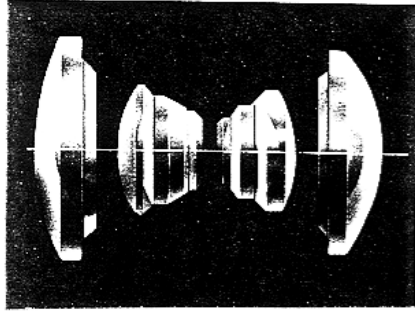


*Scanner PhotoScan2001*

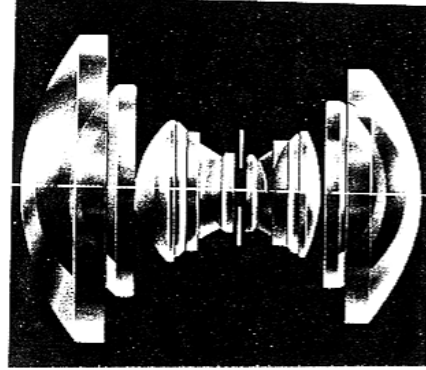


# ***Photogrammetric terrestrial cameras***

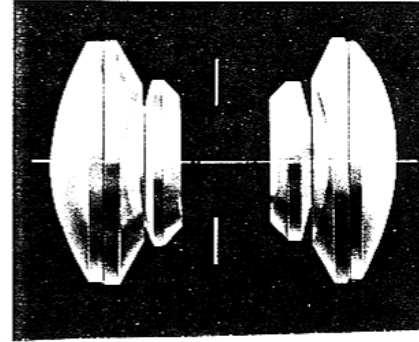
LAMEGON 8/100 B



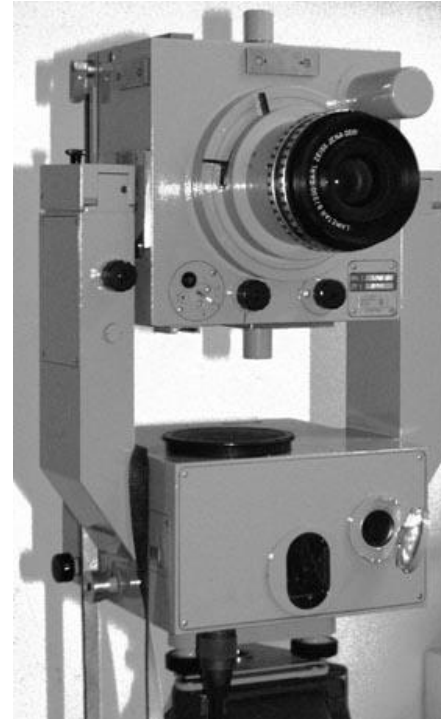
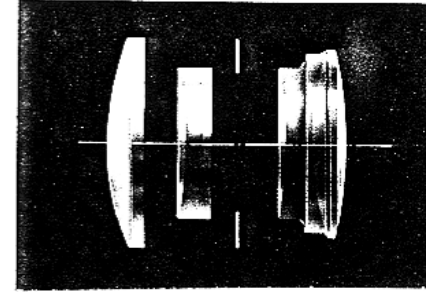
SUPERLAMEGON PI 5,6/64



LAMETAR 8/200



LAMETAR 11/300



*Photheo 13x18, UMK 201318 and Wild P31 chamber*

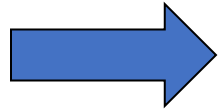
# *Photogrammetric cameras*



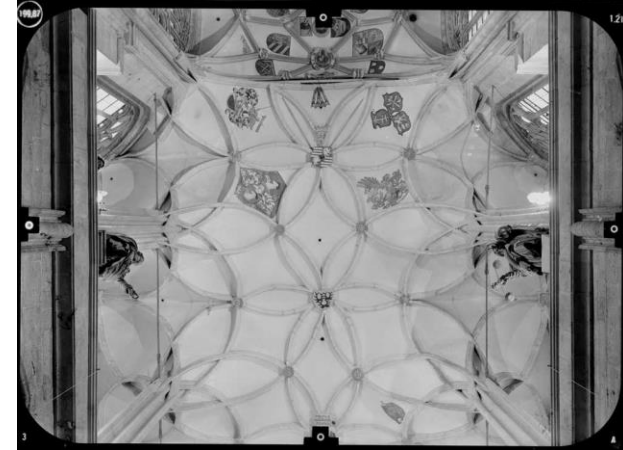
*Leica RC 30 camera  
Zeiss RMK-TOP camera and TAS gyrostabilised platform,  
LMK camera (Zeiss Jena)*



# *Classical photogrammetric records*



*frame marks*





2003, GSD 50 cm

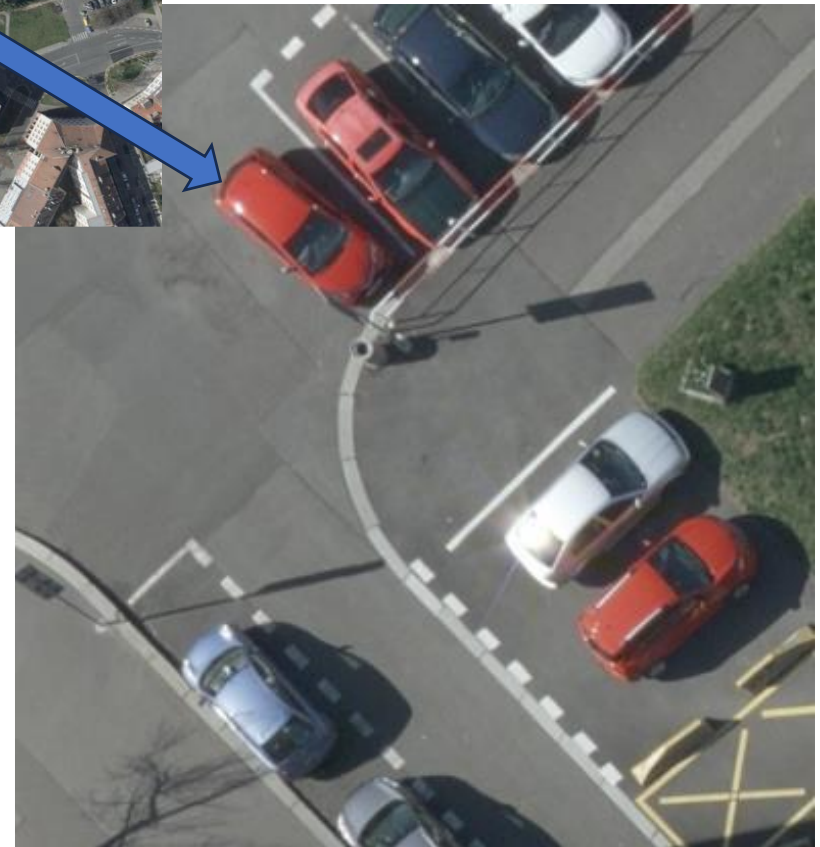
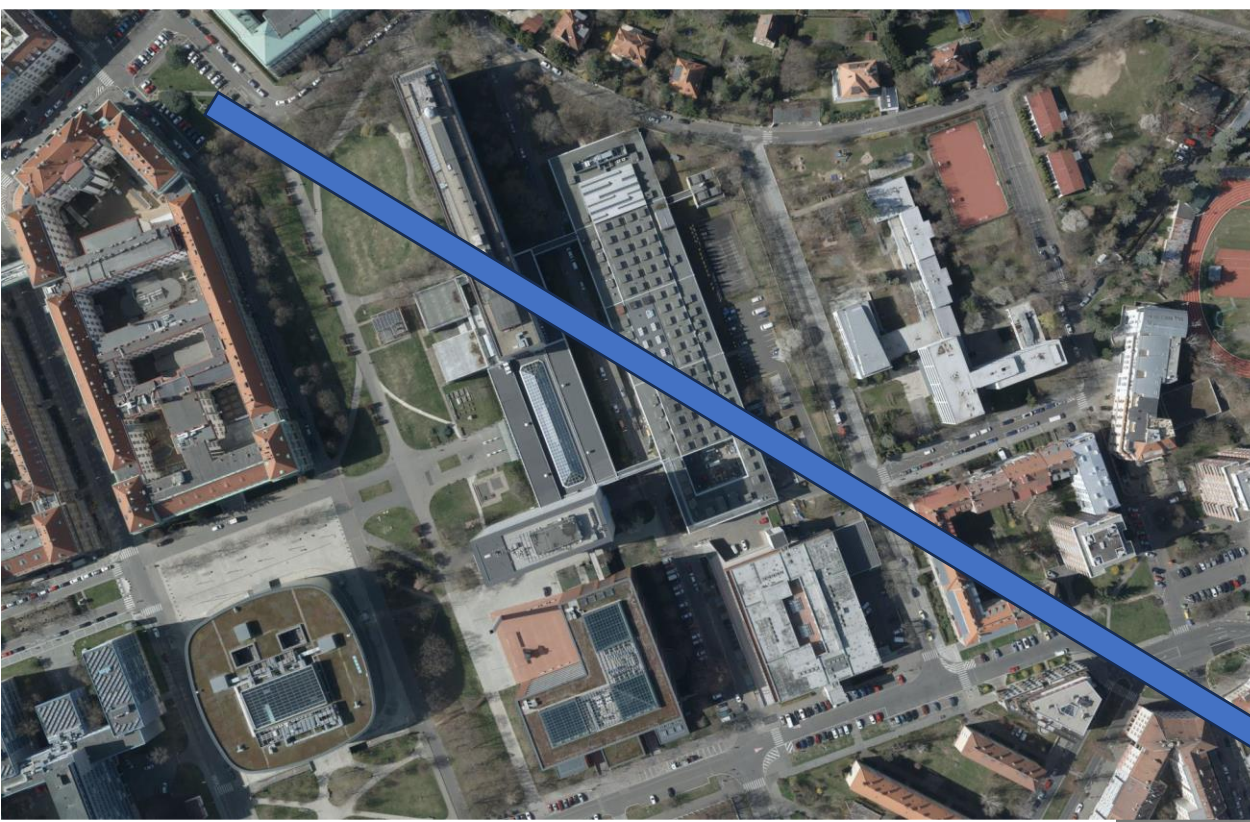


2015, GSD 15cm



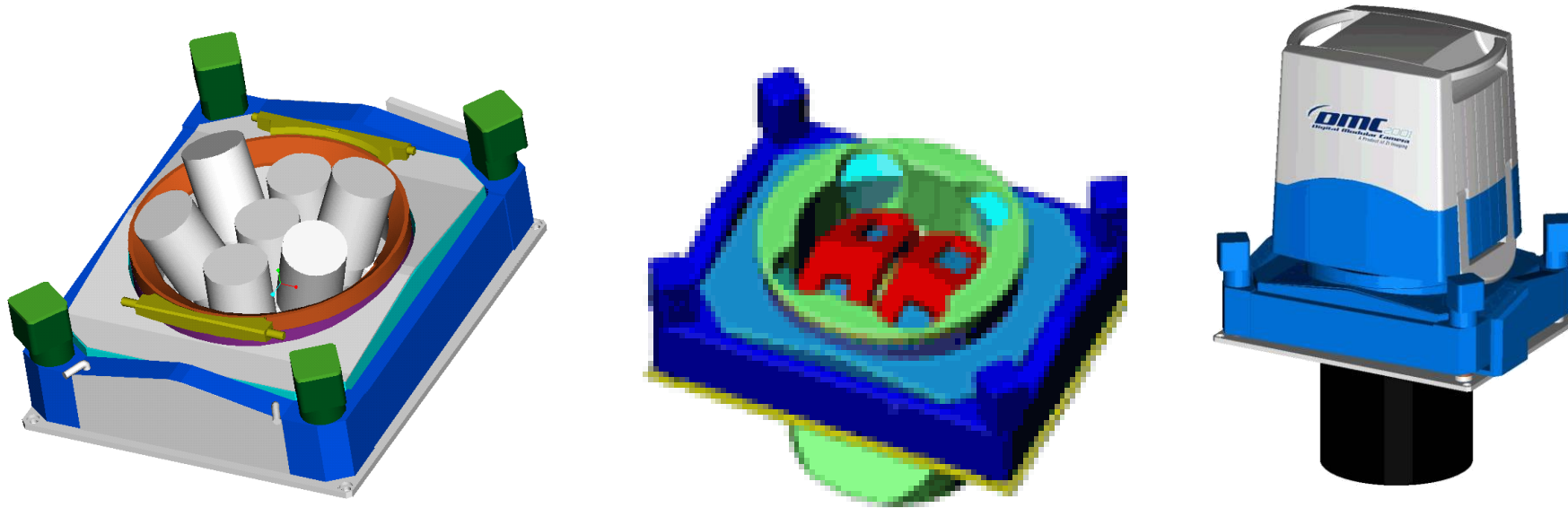
L-410FG



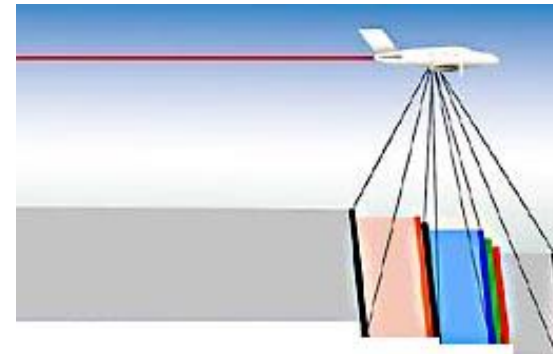
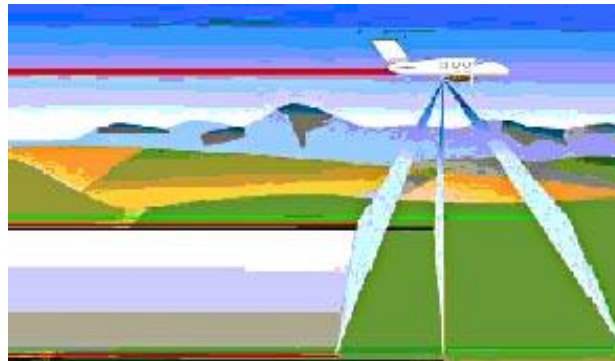


2021 GSD 2cm

# Digital air cameras



*View of the DMC camera (top), original schematic of the gyrostabilized sensor part (left), current schematic (right)*



*Sensor head ADS40 , ADS40, surface scanning principle*



# *satellite photogrammetry*



*Ikonos 1, 1999 (1m PAN, 4m MSS);  
today's civilian satellites 0.35-0.5m PAN*

# *Photogrammetric technologies for image content evaluation*

*Analog technology  
(obsolete, not used)*



*Numerical (analytical) technology  
- using analogue machines and partial  
counting steps (classical)*

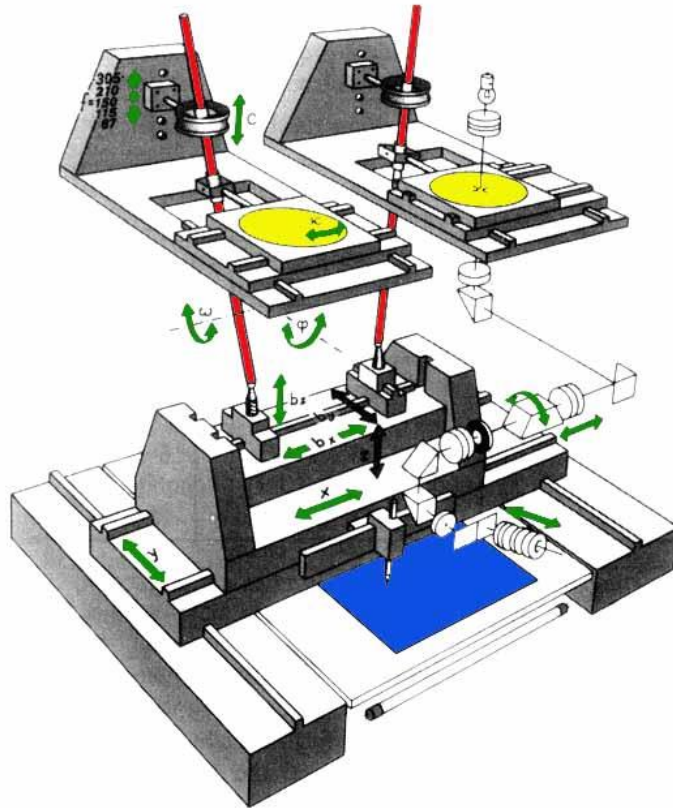


*Analytical technology  
- cannot be solved without a computer  
- present*

# *Spatial evaluation using streptophotogrammetric devices*

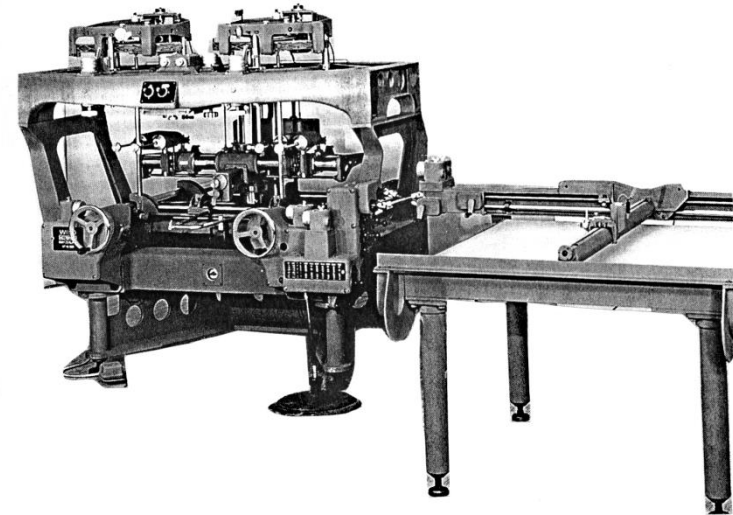
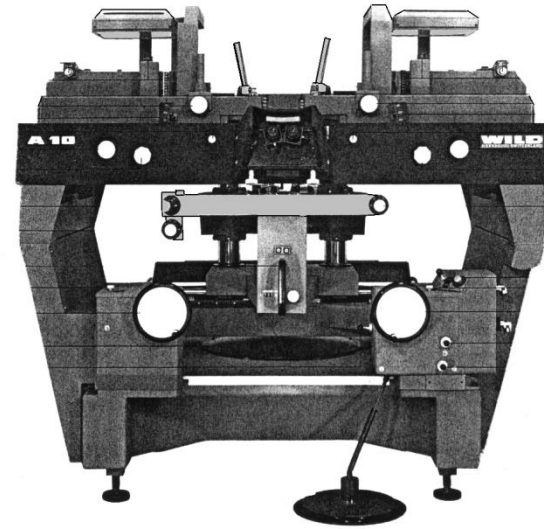
## *Analog plotters*

- produced until 1986 (Wild) and 1990 (Zeis Jena)*
- a complex and precise mechanical device, allowing the restoration of the elements of the external orientation*
- a realistic stereoscopic model is created by tilting and shifting the images*
- latest models with computer support*
- model coordinates are controlled*
- currently obsolete*





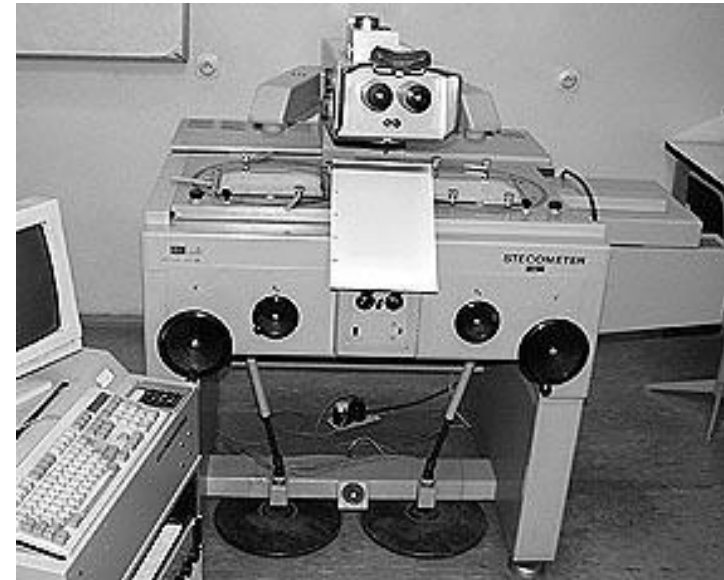
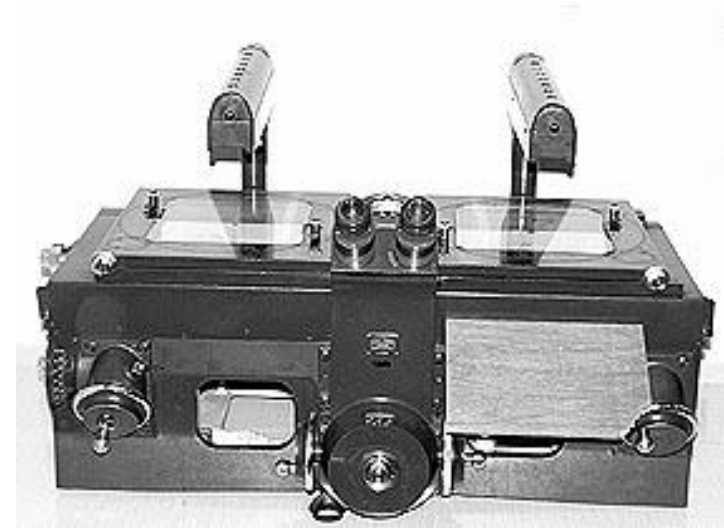
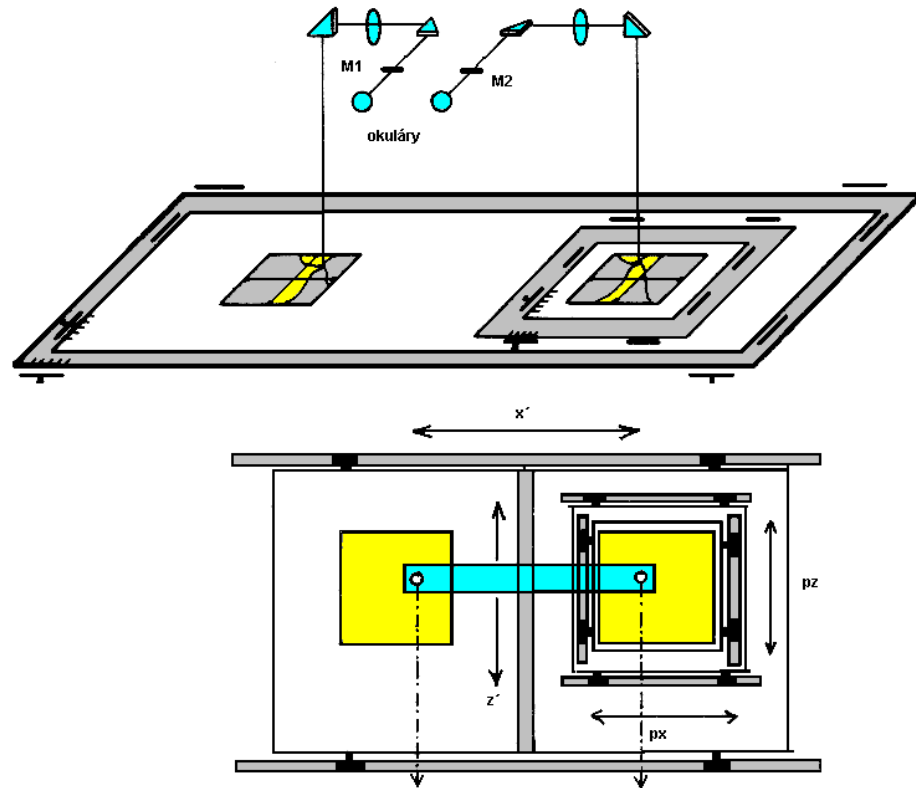
# *Analog plotters*



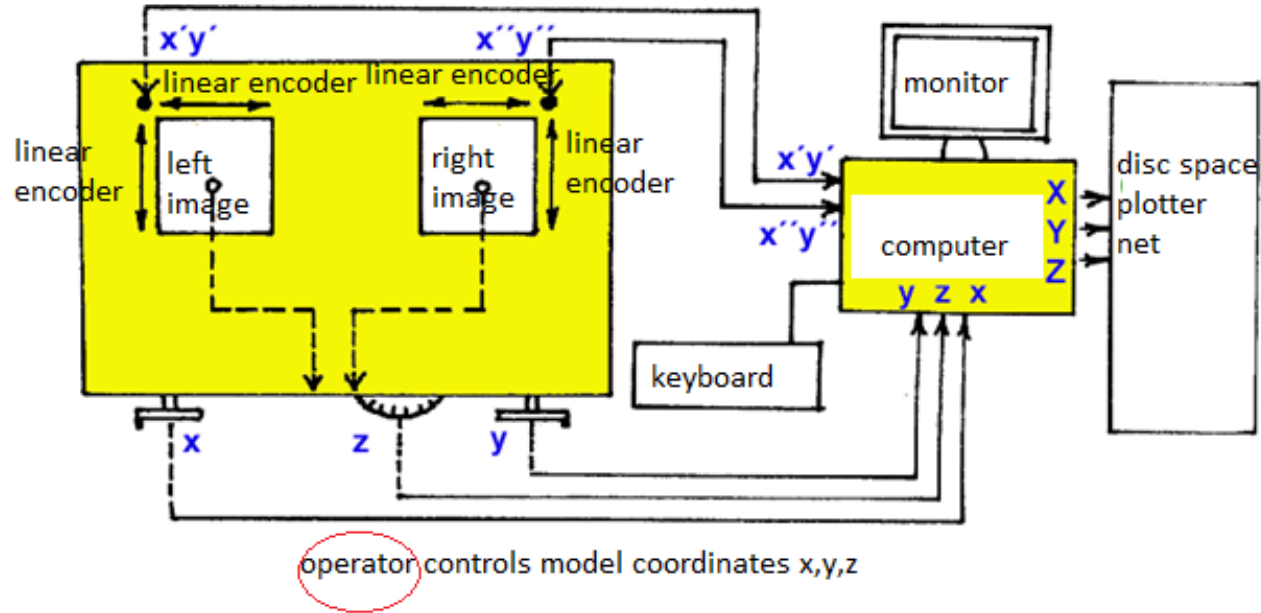
*Stereometrograph, Topocart (Zeiss Jena) A-10 and A-7 (Wild)*



# *analogue comparators*



# Analytical plotters

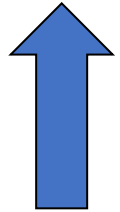


- measured on real images, computer required
- no real model is created
- the most accurate fm method
- model coordinates are controlled, converted to frame coordinates on the computer
- mobile image carriers are set to the calculated image coordinates

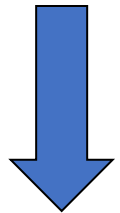


BC-1 (Wild, 1985) SD 2000 (Leica, 1995)

# Digital stations



*Imagestation Unix Imagestation SSK  
Helava (Leica) VSD*





# ***aerial photogrammetry***

## **Image orientation:**

- *internal orientation (elements of internal orientation)*
- *External orientation (coordinates of the centre of the entrance pupil  $X_0$ ,  $Y_0$ ,  $Z_0$ , then inclinations „)*

**For stereo-evaluation of photogrammetric images, the exterior orientation is defined as:**

- direct transformation relation based on complex solution - beam alignment
- older step-by-step procedure called:

- relative orientation** (relative orientation between the two stereo images, forming an arbitrary spatially oriented virtual stereo model)*
- absolute orientation** (scaling, rotation and shifting of the model to the geodetic reference system)*

# aerial photogrammetry

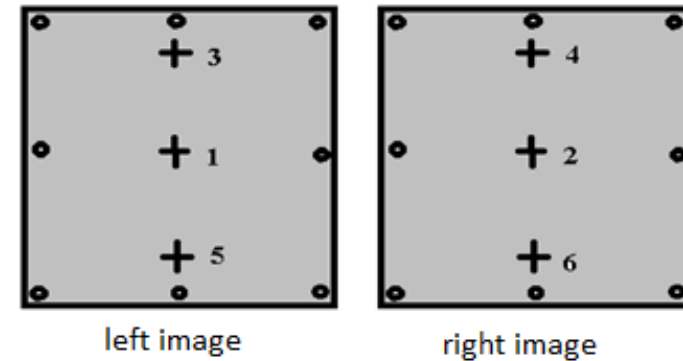
## Relative orientation of the independent pair

The rotation  $d, d, d, d, =d -d$  is chosen as the determinate unknowns. assumption yy

$$0 = q + x'd\kappa' - x'd\kappa'' - \frac{x'y'}{f}d\phi' + \frac{x'y'}{f}d\phi'' + \left(f + \frac{y'^2}{f}\right)\Delta\omega$$

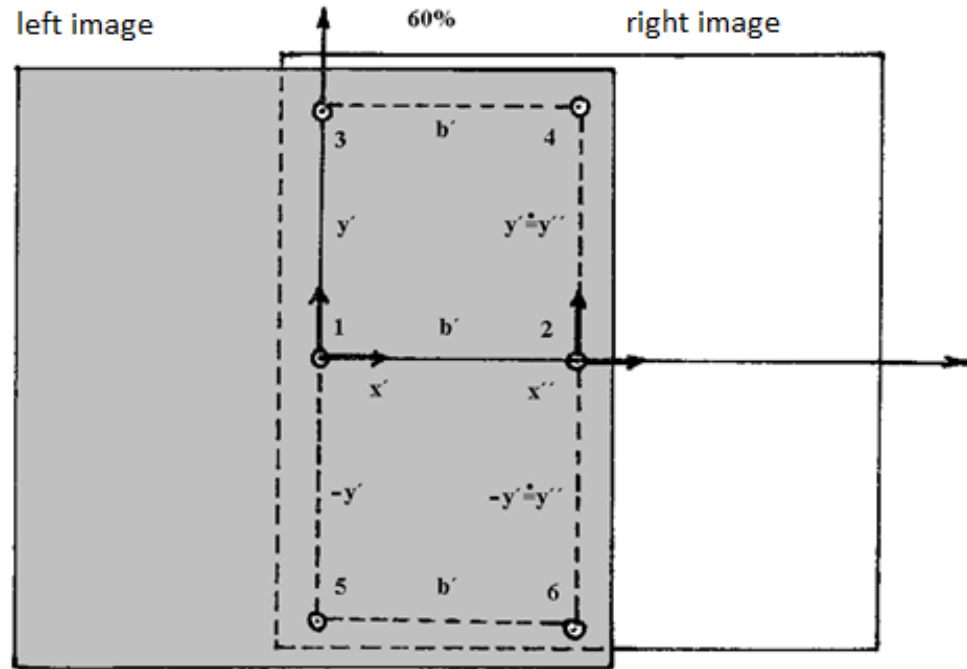
$$\left(f + \frac{y'^2}{f}\right)d\omega' - \left(f + \frac{y''^2}{f}\right)d\omega'' \cong \left(f + \frac{y'^2}{f}\right)(d\omega' - d\omega'') = \left(f + \frac{y'^2}{f}\right)\Delta\omega$$

orinthal point	left picture x	left frame y	right picture x	right image y
1	0	0	-b	0
2	+b	0	0	0
3	0	+y	-b	+y
4	+b	+y	0	+y
5	0	-y	-b	-y
6	+b	-y	0	-y





# aerial photogrammetry



$$0 = q_1 + b'd\kappa'' + f\Delta\omega$$

$$0 = q_2 + b'd\kappa' + f\Delta\omega$$

$$0 = q_3 + b'd\kappa'' - \frac{b'y'}{f}d\varphi'' + \left(f + \frac{y'^2}{f}\right)\Delta\omega$$

$$0 = q_4 + b'd\kappa' - \frac{b'y'}{f}d\varphi' + \left(f + \frac{y'^2}{f}\right)\Delta\omega$$

$$0 = q_5 + b'd\kappa'' + \frac{b'y'}{f}d\varphi'' + \left(f + \frac{y'^2}{f}\right)\Delta\omega$$

$$0 = q_6 + b'd\kappa' + \frac{b'y'}{f}d\varphi' + \left(f + \frac{y'^2}{f}\right)\Delta\omega$$

# aerial photogrammetry

## Relative orientation when attaching an image

The rotations  $d$ ,  $d$ ,  $db_y$ ,  $db_z$  are chosen as the determinate unknowns.

$$0 = q - x''d\kappa'' + \frac{x''y''}{f}d\phi'' - \left(f + \frac{y''^2}{f}\right)d\omega'' - db_y'' - \frac{y''}{f}db_z''$$

$$0 = q_1 + b'd\kappa'' - fd\omega'' - db_y''$$

$$0 = q_2 - fd\omega'' - db_y''$$

$$0 = q_3 + b'd\kappa'' - \frac{b'y''}{f}d\phi'' - fd\omega'' - \frac{y''^2}{f}d\omega'' - db_y'' - \frac{y''}{f}db_z''$$

$$0 = q_4 - fd\omega'' - \frac{y''^2}{f}d\omega'' - db_y'' - \frac{y''}{f}db_z''$$

$$0 = q_5 + b'd\kappa'' + \frac{b'y''}{f}d\phi'' - fd\omega'' - \frac{y''^2}{f}d\omega'' - db_y'' + \frac{y''}{f}db_z''$$

$$0 = q_6 - fd\omega'' - \frac{y''^2}{f}d\omega'' - db_y'' + \frac{y''}{f}db_z''$$

# ***aerial photogrammetry***

## ***Absolute orientation***

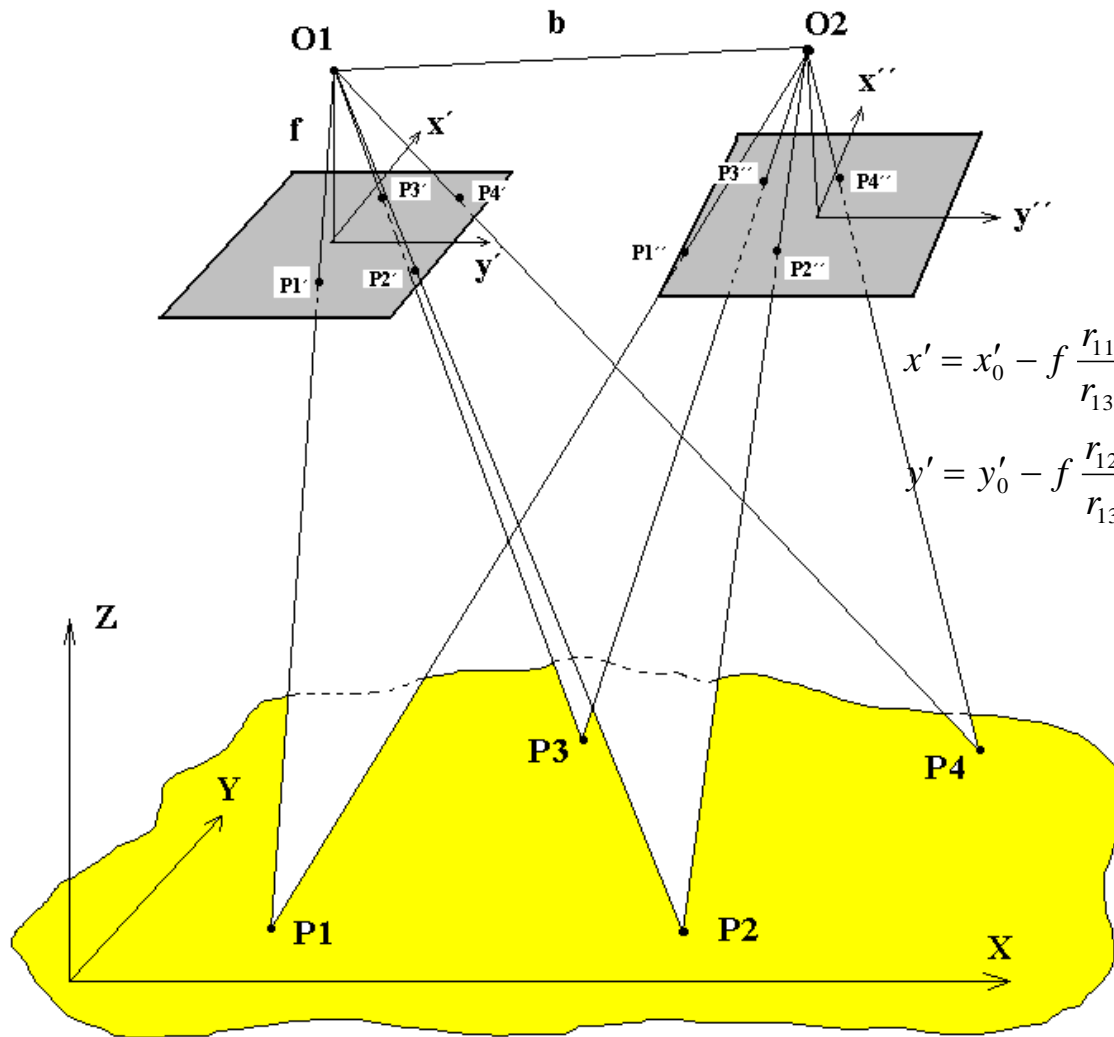
$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix} = \begin{pmatrix} X_0 \\ Y_0 \\ Z_0 \end{pmatrix} + m \cdot \mathbf{R} \cdot \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

where  $X, Y, Z$  are geodetic coordinates,  $X_0, Y_0, Z_0$  are the geodetic coordinates of the origin of the model coordinate system  $x, y, z$ ,  $m$  is the scale of the model and  $\mathbf{R}$  is the spatial rotation matrix of the model coordinate system in the geodetic coordinate system, containing the three angles  $\phi, \omega, \kappa$ . The relation (14.12) is a spatial similarity transformation with unknowns  $X_0, Y_0, Z_0, m, \phi, \omega, \kappa$ .

$$M = \begin{pmatrix} m_x & 0 & 0 \\ 0 & m_y & 0 \\ 0 & 0 & m_z \end{pmatrix}$$

# Analytical methods

Comprehensive solution



$$x' = x'_0 - f \frac{r_{11}(X - X_0) + r_{21}(Y - Y_0) + r_{31}(Z - Z_0)}{r_{13}(X - X_0) + r_{23}(Y - Y_0) + r_{33}(Z - Z_0)} = x'_0 - f \frac{\mathbf{R}_1 \cdot \mathbf{X}}{\mathbf{R}_3 \cdot \mathbf{X}}$$

$$y' = y'_0 - f \frac{r_{12}(X - X_0) + r_{22}(Y - Y_0) + r_{32}(Z - Z_0)}{r_{13}(X - X_0) + r_{23}(Y - Y_0) + r_{33}(Z - Z_0)} = y'_0 - f \frac{\mathbf{R}_2 \cdot \mathbf{X}}{\mathbf{R}_3 \cdot \mathbf{X}}$$

# Analytical methods

## Comprehensive solution

$$x'_{i1} = F_x(f, x'_0 = d'x, X_{01}, Y_{01}, Z_{01}, \omega_1, \varphi_1, \kappa_1, X_i, Y_i, Z_i)$$

$$y'_{i1} = F_y(f, y'_0 = d'y, X_{01}, Y_{01}, Z_{01}, \omega_1, \varphi_1, \kappa_1, X_i, Y_i, Z_i)$$

$$x''_{i2} = F_x(f, x''_0 = d'x, X_{02}, Y_{02}, Z_{02}, \omega_2, \varphi_2, \kappa_2, X_i, Y_i, Z_i)$$

$$y''_{i2} = F_y(f, y''_0 = d'y, X_{02}, Y_{02}, Z_{02}, \omega_2, \varphi_2, \kappa_2, X_i, Y_i, Z_i)$$

$$f(x_1, \dots, x_n) = f(x_1^0, \dots, x_n^0) + \left( \frac{\partial f}{\partial x_1} \right)^0 dx_1 + \dots + \left( \frac{\partial f}{\partial x_n} \right)^0 dx_n$$

$$\begin{aligned} v_{xij} = & \left( \frac{\partial x'}{\partial X_{0j}} \right)^0 dX_{0j} + \left( \frac{\partial x'}{\partial Y_{0j}} \right)^0 dY_{0j} + \left( \frac{\partial x'}{\partial Z_{0j}} \right)^0 dZ_{0j} + \\ & + \left( \frac{\partial x'}{\partial \omega_j} \right)^0 d\omega_j + \left( \frac{\partial x'}{\partial \varphi_j} \right)^0 d\varphi_j + \left( \frac{\partial x'}{\partial \kappa_j} \right)^0 d\kappa_j + \\ & + \left( \frac{\partial x'}{\partial X_i} \right)^0 dX_i + \left( \frac{\partial x'}{\partial Y_i} \right)^0 dY_i + \left( \frac{\partial x'}{\partial Z_i} \right)^0 dZ_i - (x'_{ij} - x'^0_{ij}) \end{aligned}$$



# Analytical methods

**Comprehensive solution**

$$\mathbf{v} = \mathbf{A}_1 \cdot \mathbf{x}_1 + \mathbf{A}_2 \cdot \mathbf{x}_2 - \mathbf{l} \quad \leftrightarrow \quad (\mathbf{v} = \mathbf{A} \cdot \mathbf{x} - \mathbf{l})$$

$$\mathbf{x} = (\mathbf{A}^T \mathbf{A})^{-1} \cdot \mathbf{A}^T \mathbf{l}$$

$$\mathbf{A}^T \mathbf{A} = \mathbf{N} \quad \mathbf{A}^T \cdot \mathbf{l} = \mathbf{n}$$

$$\mathbf{v} = \mathbf{A} \cdot \mathbf{x} - \mathbf{l}$$

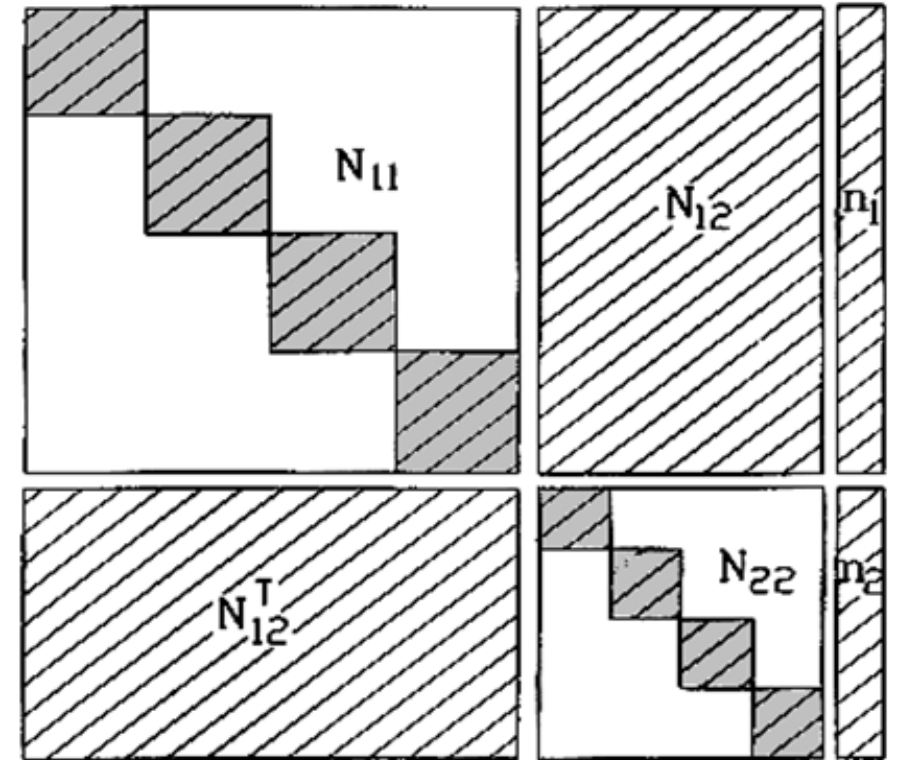


$$\mathbf{N} \cdot \mathbf{x} = \mathbf{n}$$

$$\begin{pmatrix} \mathbf{N}_{11} & \mathbf{N}_{12} \\ \mathbf{N}_{12}^T & \mathbf{N}_{22} \end{pmatrix} \cdot \begin{pmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \end{pmatrix} = \begin{pmatrix} \mathbf{n}_1 \\ \mathbf{n}_2 \end{pmatrix}$$

$$(\mathbf{N}_{11} - \mathbf{N}_{12} \cdot \mathbf{N}_{22}^{-1} \cdot \mathbf{N}_{12}^T) \mathbf{x}_1 = \mathbf{n}_1 - \mathbf{N}_{12} \cdot \mathbf{N}_{22}^{-1} \cdot \mathbf{n}_2$$

image1 image 2 image 3 image 4



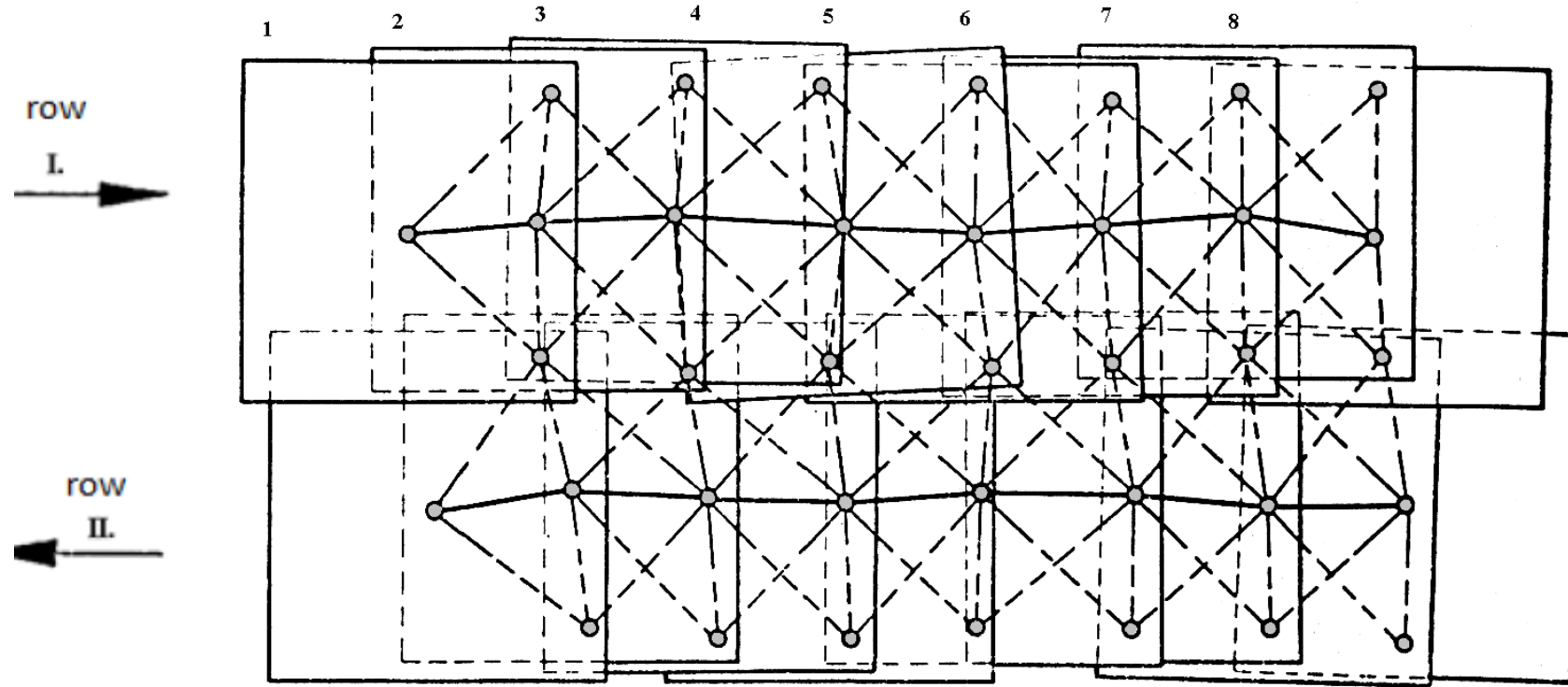
point 1  
point 2  
point 3  
point 4

# ***Image triangulation***

The goal of today's analytical aerotriangulation is:

- - ***obtaining germination points for detailed evaluation***
  - - ***Alignment of a set of images or models to ensure continuous evaluation***
  - - ***accurate calculation of exterior orientation elements for all images***
- 
- *Historically, there are radial, analogue, semi-analytical and analytical technology of aerotriangulation*
  - *Today only automated (digital) aerotriangulation is used (**AAT**)*

# *Image triangulation*



Full triangular radial mesh and normal image block in radial triangulation

# digital photogrammetry

## *Theory of image correlation*

$$\rho(A, B) = \frac{\text{cov}(A, B)}{\rho(A) \cdot \rho(B)}$$

If we want to calculate the correlation coefficient for two equally sized digital images (or their cuts), we will use to calculate the pixel value  $p(A)_{i,j}$  for image **A** and  $p(B)_{i,j}$  for image **B**. We obtain the expression:

$$r(A, B) = \frac{C(A, B)}{\sqrt{C(A) \cdot C(B)}}$$

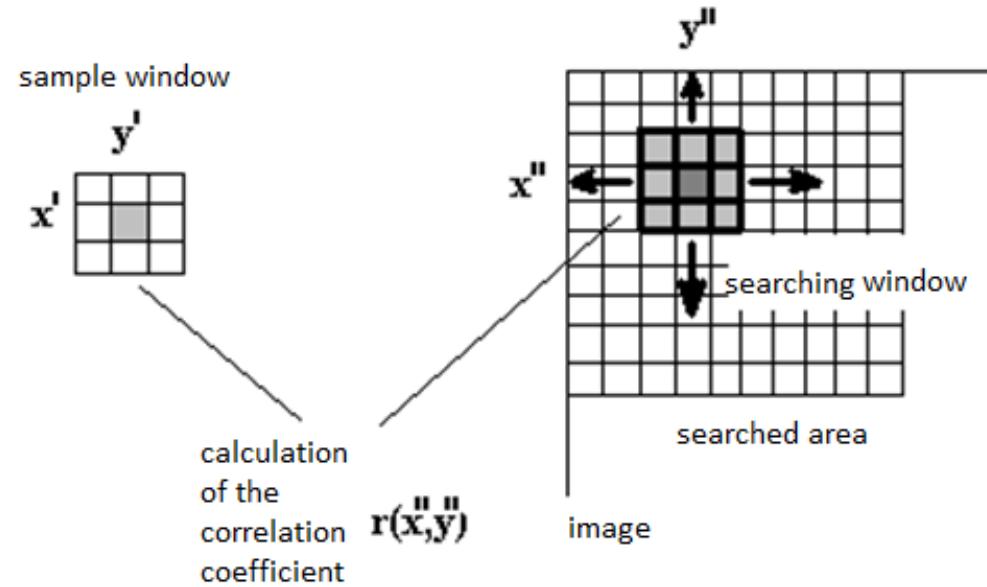
where the individual expressions are ( $n$  is the number of pixels in the side of the square window)

$$C(A, B) = \frac{1}{n^2 - 1} \sum_{i=1}^n \sum_{j=1}^n \left( p(A)_{i,j} - \bar{p}(A) \right) \cdot \left( p(B)_{i,j} - \bar{p}(B) \right)$$

$$C(A) = \frac{1}{n^2 - 1} \sum_{i=1}^n \sum_{j=1}^n \left( p(A)_{i,j} - \bar{p}(A) \right)^2, \quad \bar{p}(A) = \frac{1}{n^2} \sum_{i=1}^n \sum_{j=1}^n \left( p(A)_{i,j} \right)$$

$$C(B) = \frac{1}{n^2 - 1} \sum_{i=1}^n \sum_{j=1}^n \left( p(B)_{i,j} - \bar{p}(B) \right)^2, \quad \bar{p}(B) = \frac{1}{n^2} \sum_{i=1}^n \sum_{j=1}^n \left( p(B)_{i,j} \right)$$

# digital photogrammetry



We are looking for its maximum with subpixel precision. Since it reaches its maximum only in a limited region, we can replace the discrete correlation function by a continuous function and describe it by, for example, a second degree polynomial:

$$r = \bar{r} + v = a_0 + a_1x + a_2y + a_3xy + a_4x^2 + a_5y^2$$

where  $x_i, y_i$  is the position of the search window for the calculated value of the correlation coefficient  $r_i$ . if we have a matrix of 3x3 correlation coefficients, we get 9 values. We need a total of 6 to calculate the coefficients  $a_i$  and



# digital photogrammetry

## *Subpixel transformation*

$$p_B(x) = p_A(x + a_1)$$

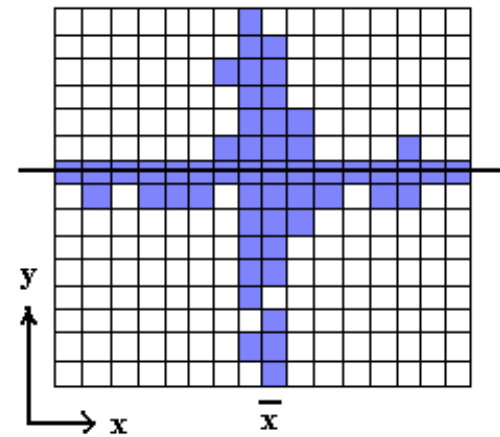
$$p_B(y) = p_A(y + a_2)$$

$$v_x + p_B(x) = p_A(x + a_1)a_3 + a_5$$

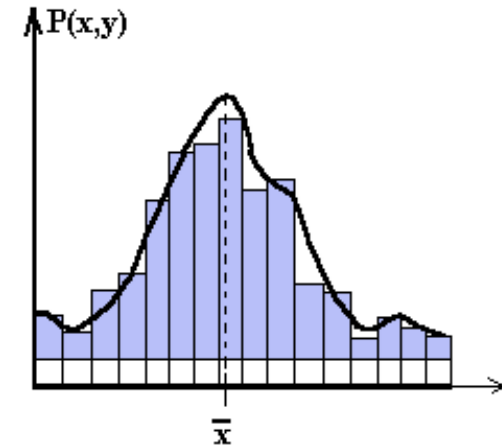
$$v_y + p_B(y) = p_A(y + a_2)a_4 + a_6$$

$$v_x + p_B(x) = p_A \cdot a_3(x) + p'_A \cdot a_3 a_1(x) + a_5$$

$$v_y + p_B(y) = p_A \cdot a_4(y) + p'_A \cdot a_4 a_2(y) + a_6$$



a detail of displayed cross  
(for example fiducial mark)



its probable centre

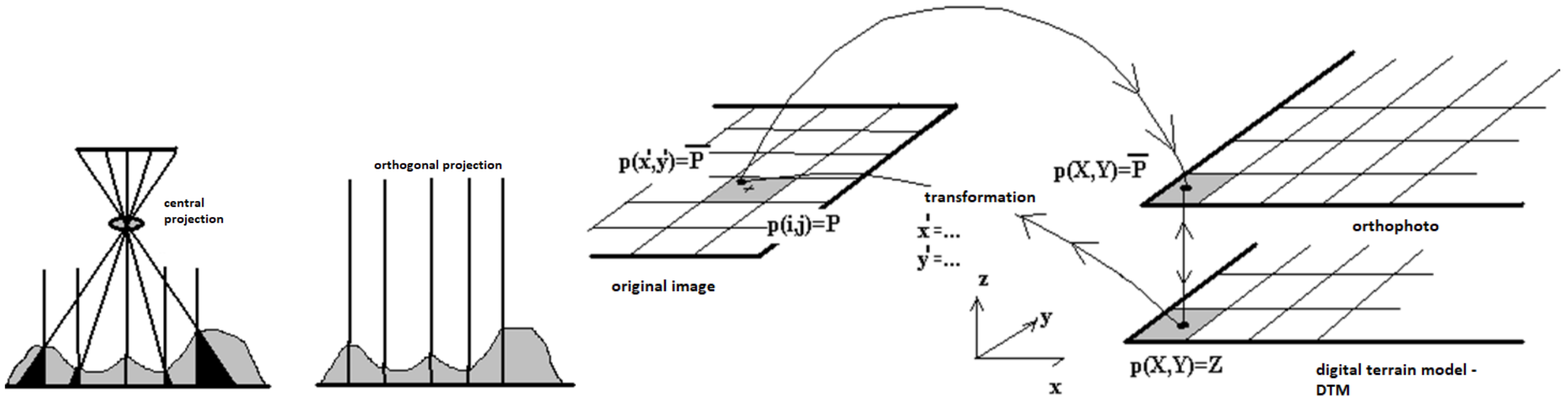
# digital photogrammetry

## Digital orthophoto

*What is necessary for an orthophoto creating?*

- images,
- known interior and exterior orientation,
- digital terrain model (DRM, DEM or DSM),
- software

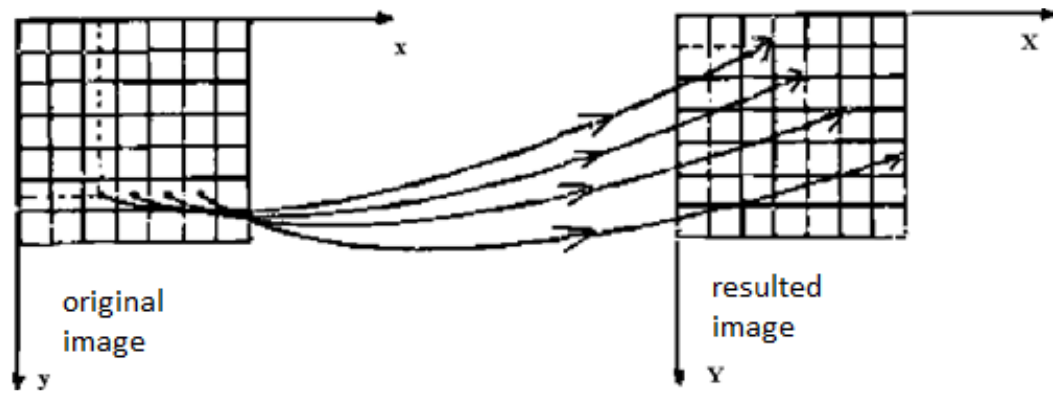
$$x' = x'_0 - f \frac{r_{11}(X - X_0) + r_{21}(Y - Y_0) + r_{31}(Z - Z_0)}{r_{13}(X - X_0) + r_{23}(Y - Y_0) + r_{33}(Z - Z_0)}$$
$$y' = y'_0 - f \frac{r_{12}(X - X_0) + r_{22}(Y - Y_0) + r_{32}(Z - Z_0)}{r_{13}(X - X_0) + r_{23}(Y - Y_0) + r_{33}(Z - Z_0)}$$



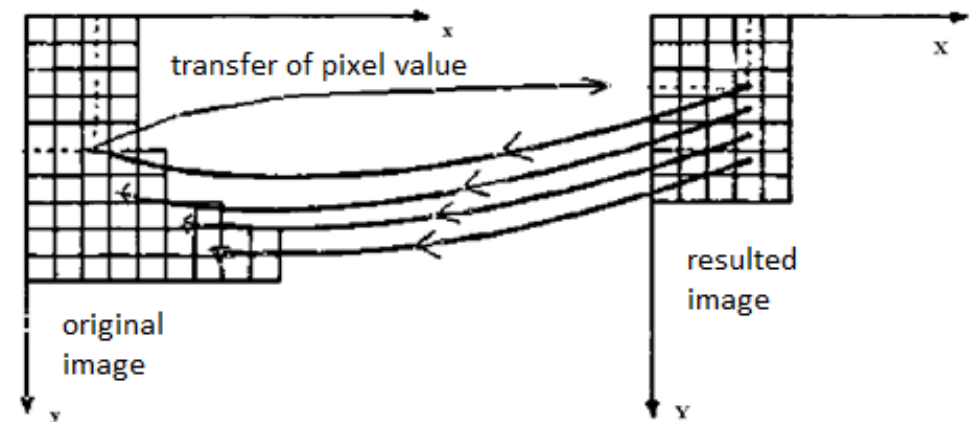
# Geometric transformation

The aim of geometric transformation is either to remove image distortion caused by the instability of geometric conditions during measurement and to convert the data into a suitable projection (especially in DPZ) or to create a new image (e.g. orthophoto) based on transformation relations. Geometric correction can be performed in three different ways:

- *data transformation based on precisely known carrier trajectory parameters*
- *direct geometric transformation based on embedding points or vectors*
  - *direct geometric transformation based on embedding points or vectors*



- data transfer from the original image matrix to the corrected matrix
  - Nearest Neighbour Method*
- *Bilinear transformation*
- *Bicubic Convolution*



***End of photogrammetry***

# 3D scanning

- Direct 3D detailed point coordinate technology
- 1)terrestrial scanning (laser scanners, triangulation scanners, optical correlation systems)-applications in construction or conservation, documentation of technological units
- 2)aerial scanning-applications for photogrammetry and GIS (creation of DTM, DRM, DSM)

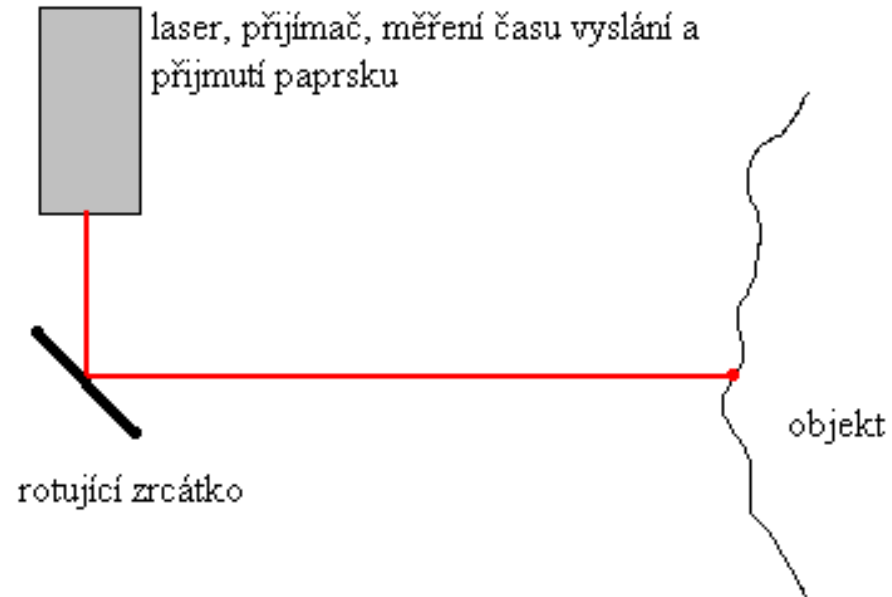


## The use of 3D scanners and their accuracy

- since about 2000, aerial applications earlier (1995)- Laser scanners (range m to hundreds of m, accuracy 4-8mm)
- triangulation scanners (range cm to approx. 20 m, accuracy from fractions of mm to mm)
- optical correlation scanners or systems (range cm to approx. 20m, accuracy from fractions of mm to cm)

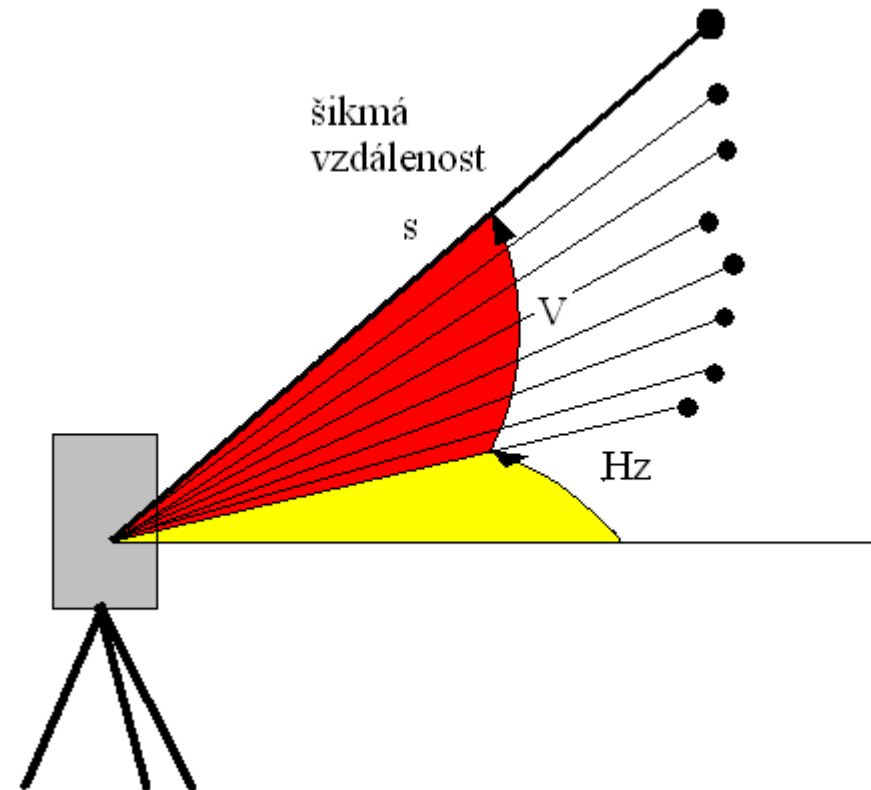
# Laser scanning

## principle



## Laser scanners ToF (time of flight)

### Terrestrial laser scanner



# Laser scanning (comparing 2002 and 2020





Callidus



Optech



Leica



Trimble



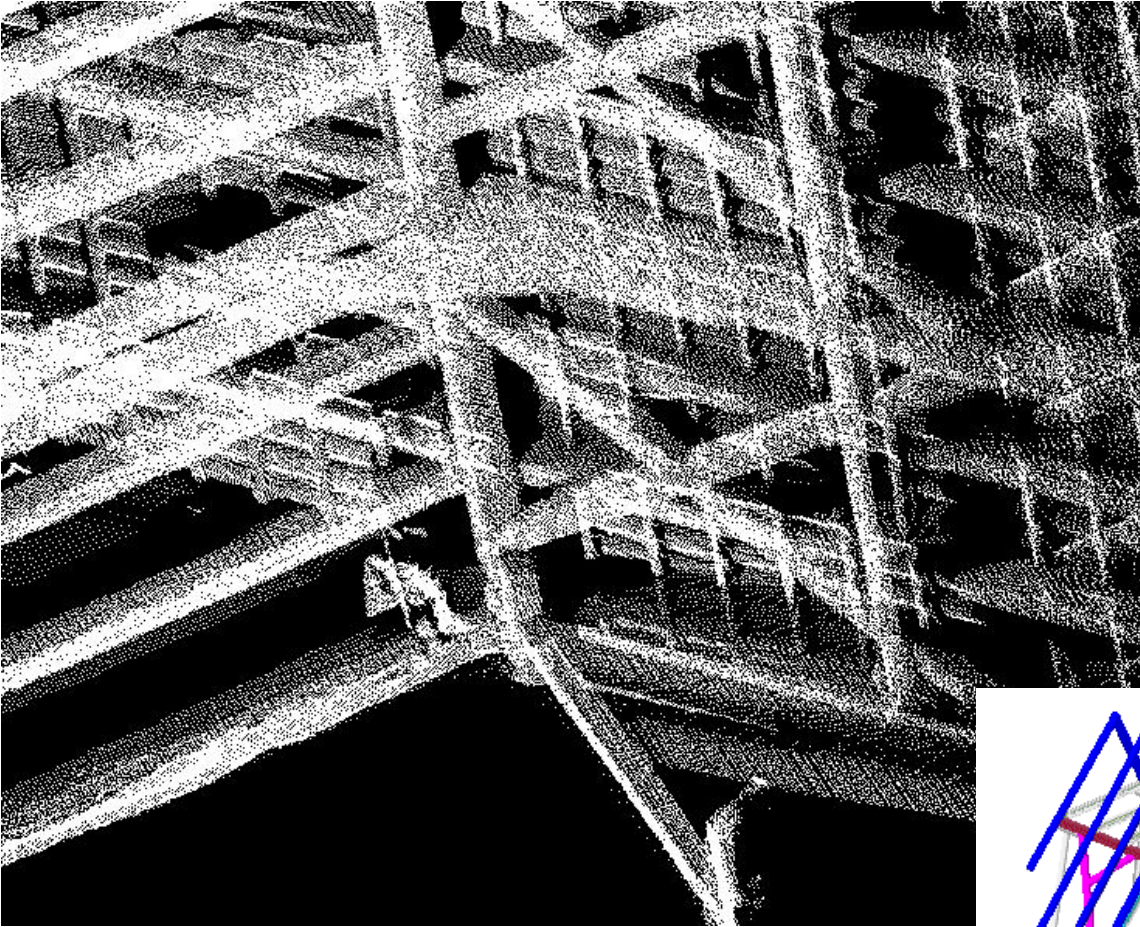
Surphaser



Faro



# *Laser scanning*

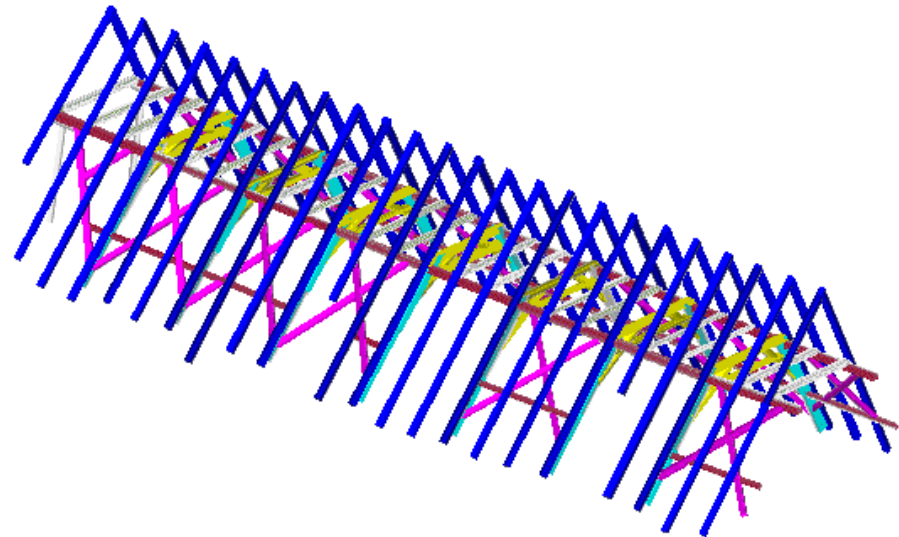


*Documentation of the board*

- point cloud

- evaluation into the model in  
*AUTOCAD*

- *Callidus laser scanner, 2004*



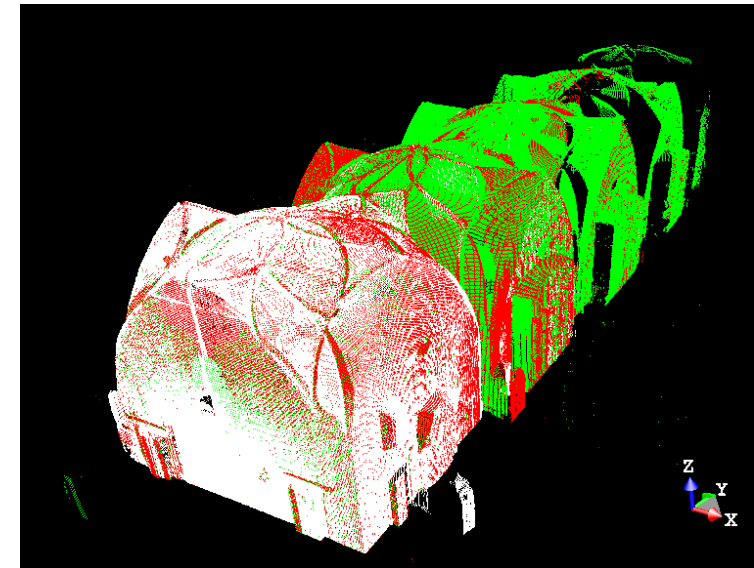
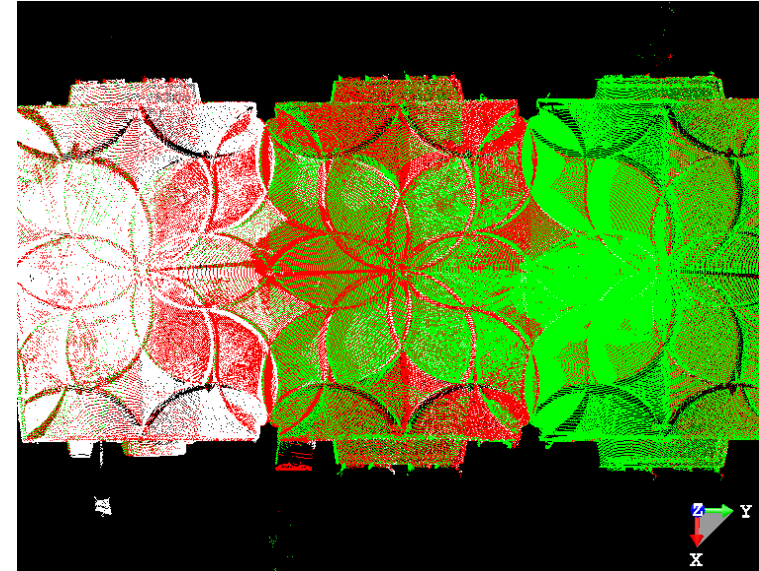


# Laser scanning

*Documentation of monumental objects*

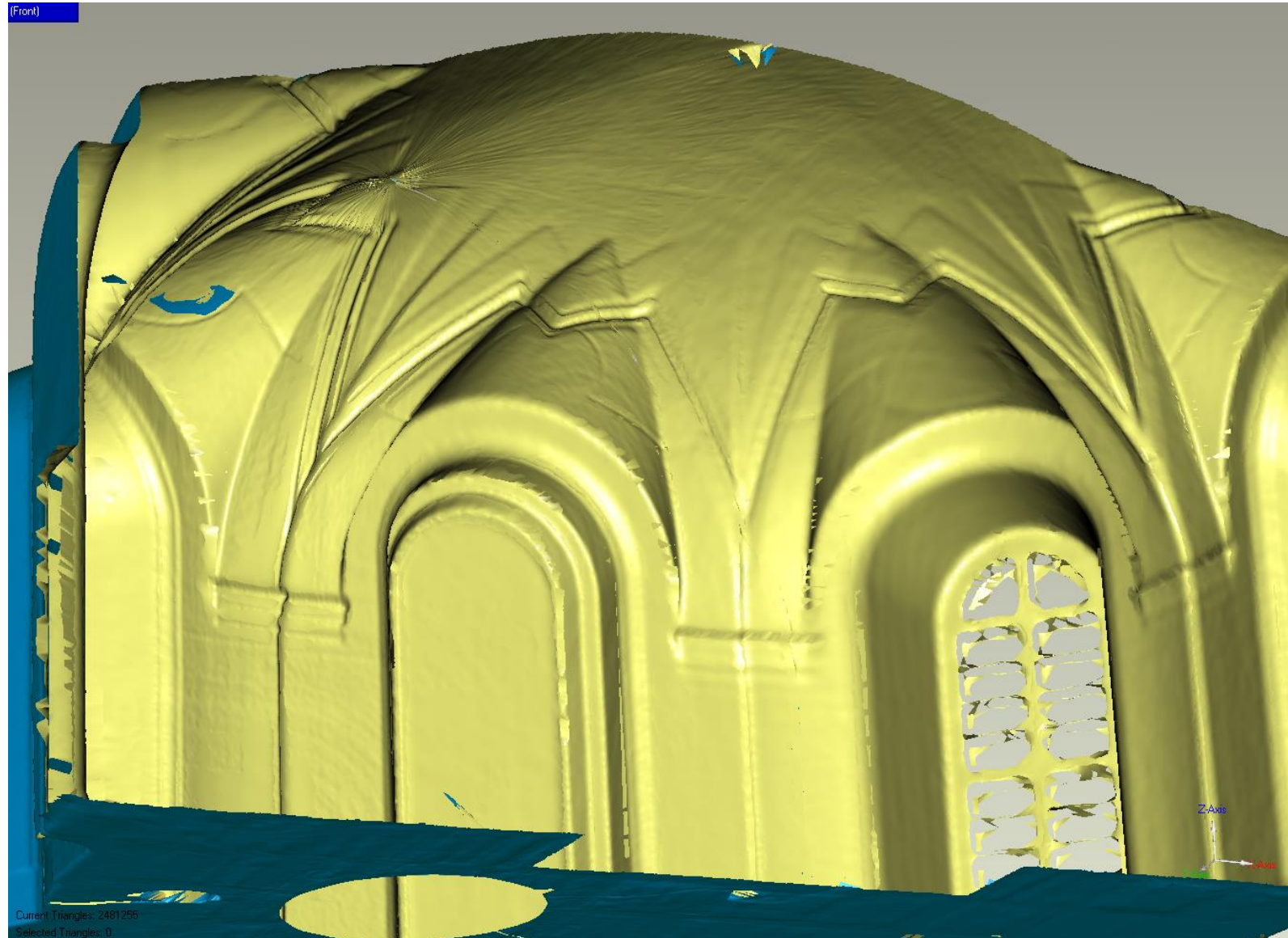
*Vladislav Hall, Prague Castle*

*Callidus laser scanner, 2005*

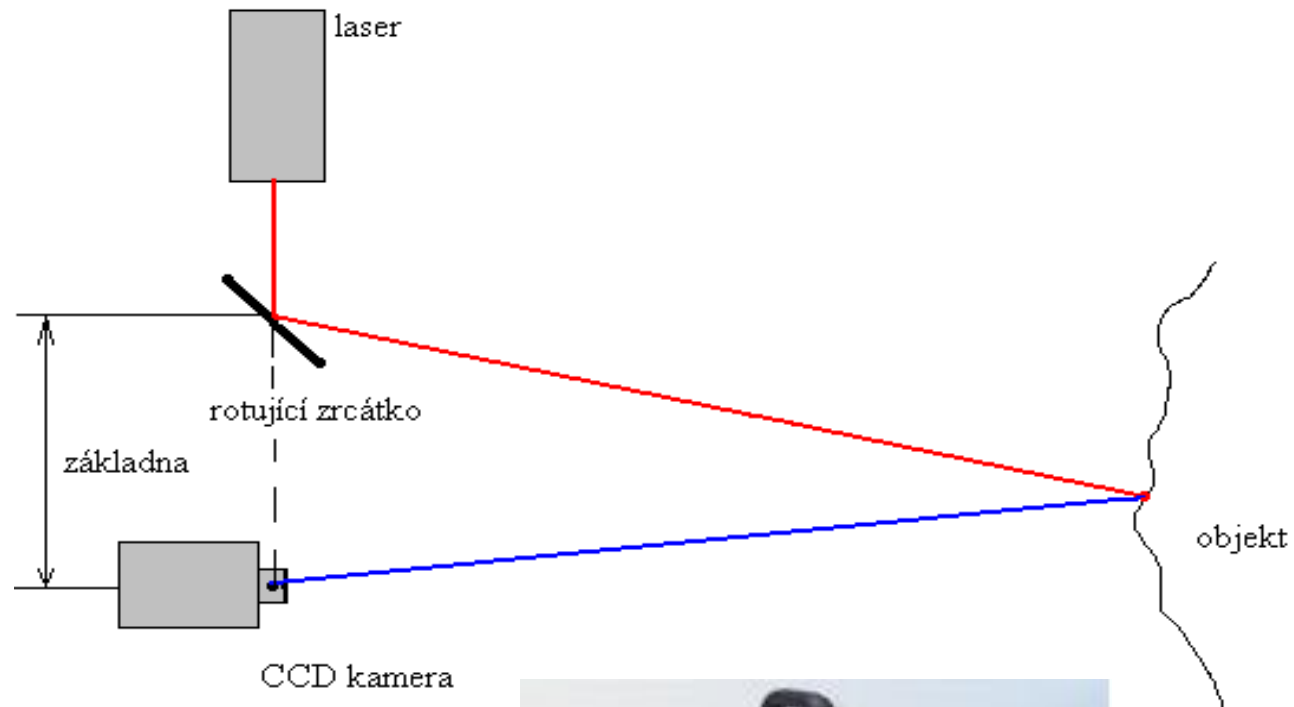




# Plasy: laser scanner Callidus, 2006



# Triangulation principle



# Laser scanning

Mensi/Trimble S25



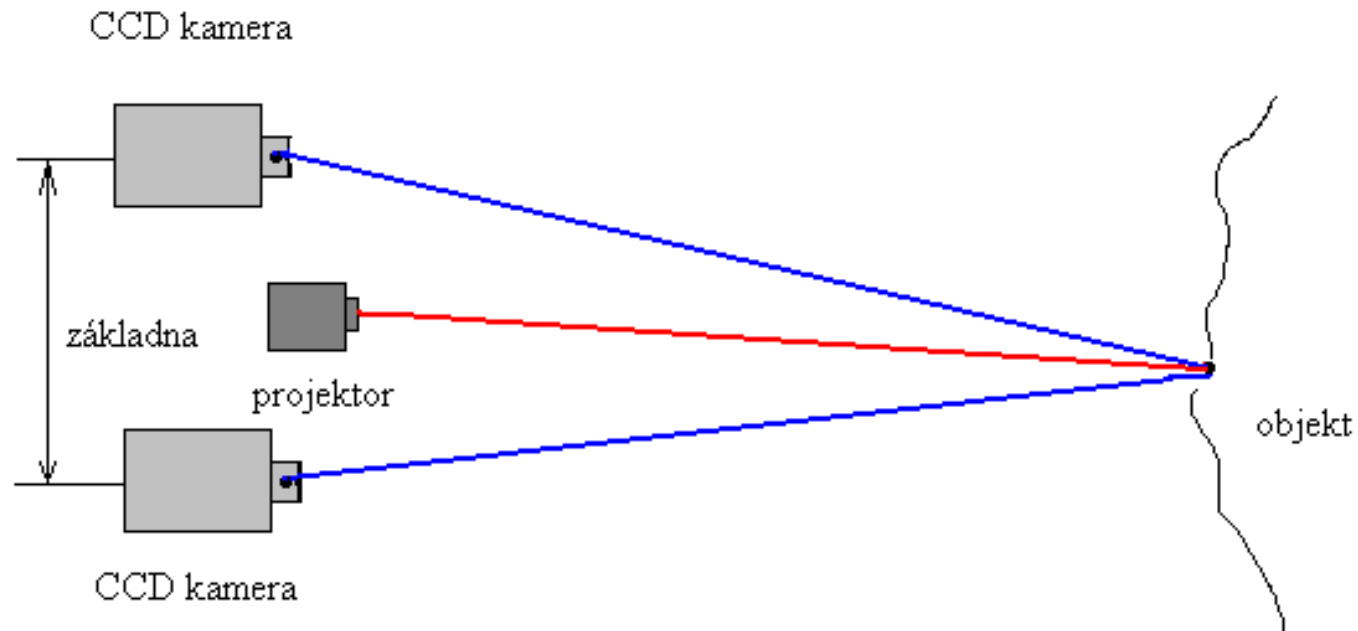
Atos



•Part of the documentation of the Mausoleum of Maximilian I, triangulation scanner Atos II, Mensi S25; scanning time 4 days, 50GB of data (i3mainz, [Böhler](http://www.i3mainz.fh-mainz.de/Article240.html), <http://www.i3mainz.fh-mainz.de/Article240.html>)



# Principle of using two cameras



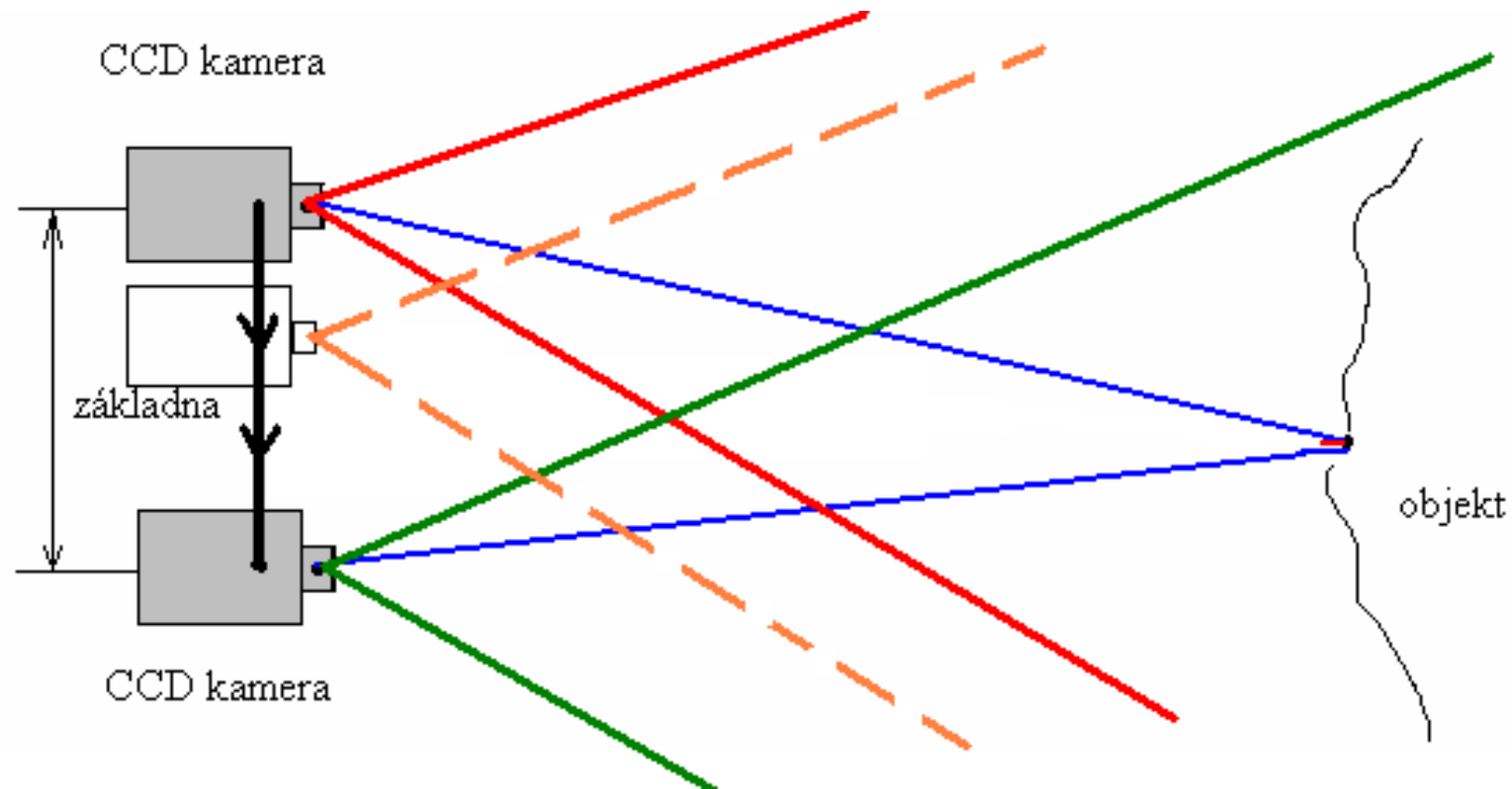
InduSCAN



Scanner Atos

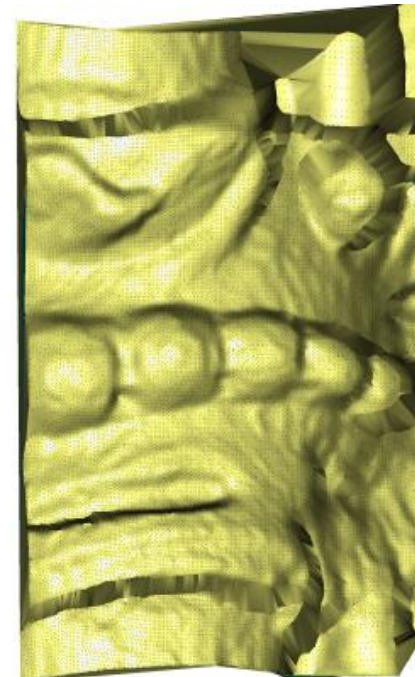


# Using of image correlation





scanner OKS, own student scanner, 2011





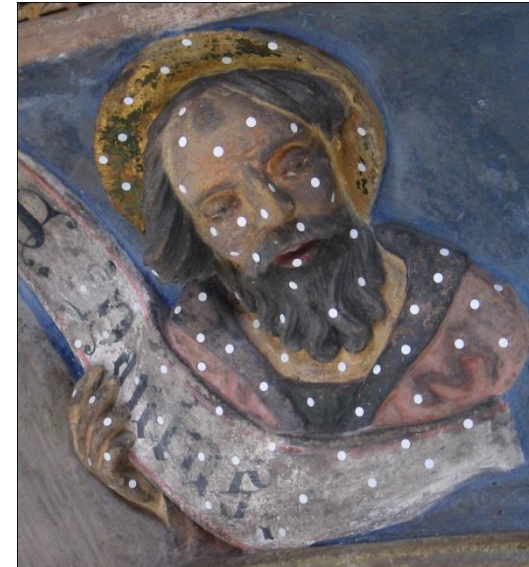
OKS



# Hand-held scanners

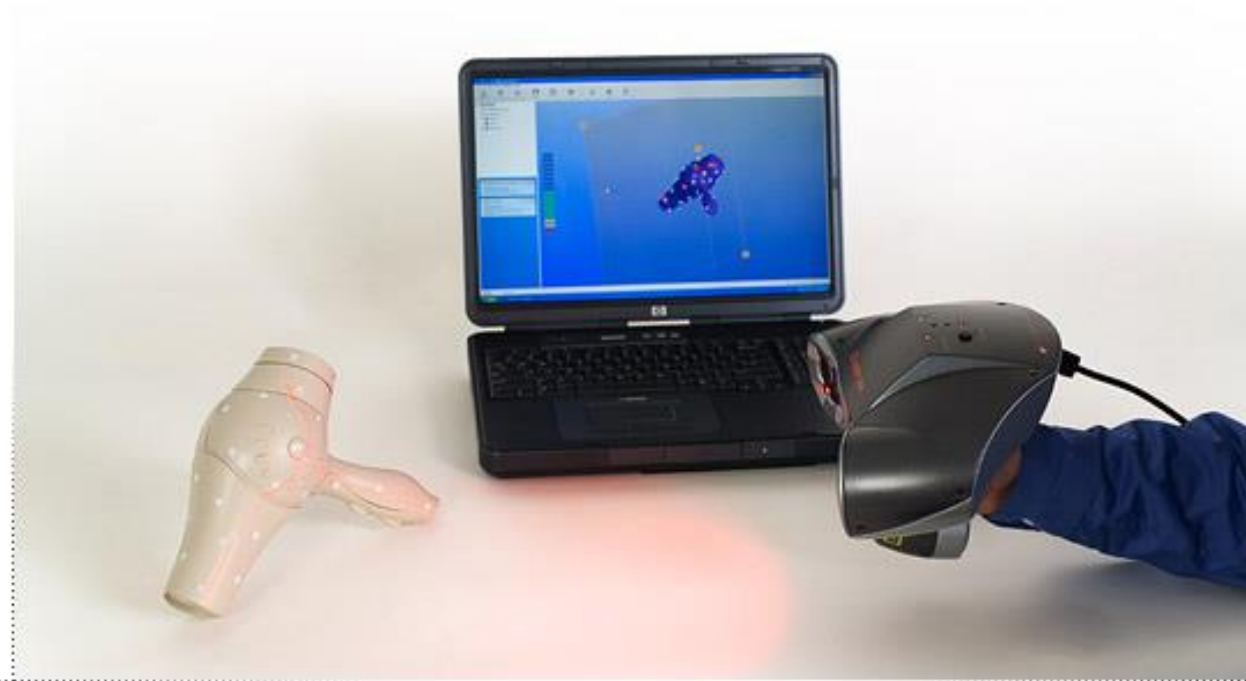


- *Original and final model*
- *(Zscanner 700 handheld scanner),*
- *Geovap and CTU*





# Zscanner 700





# Leica T-ScanTS 50



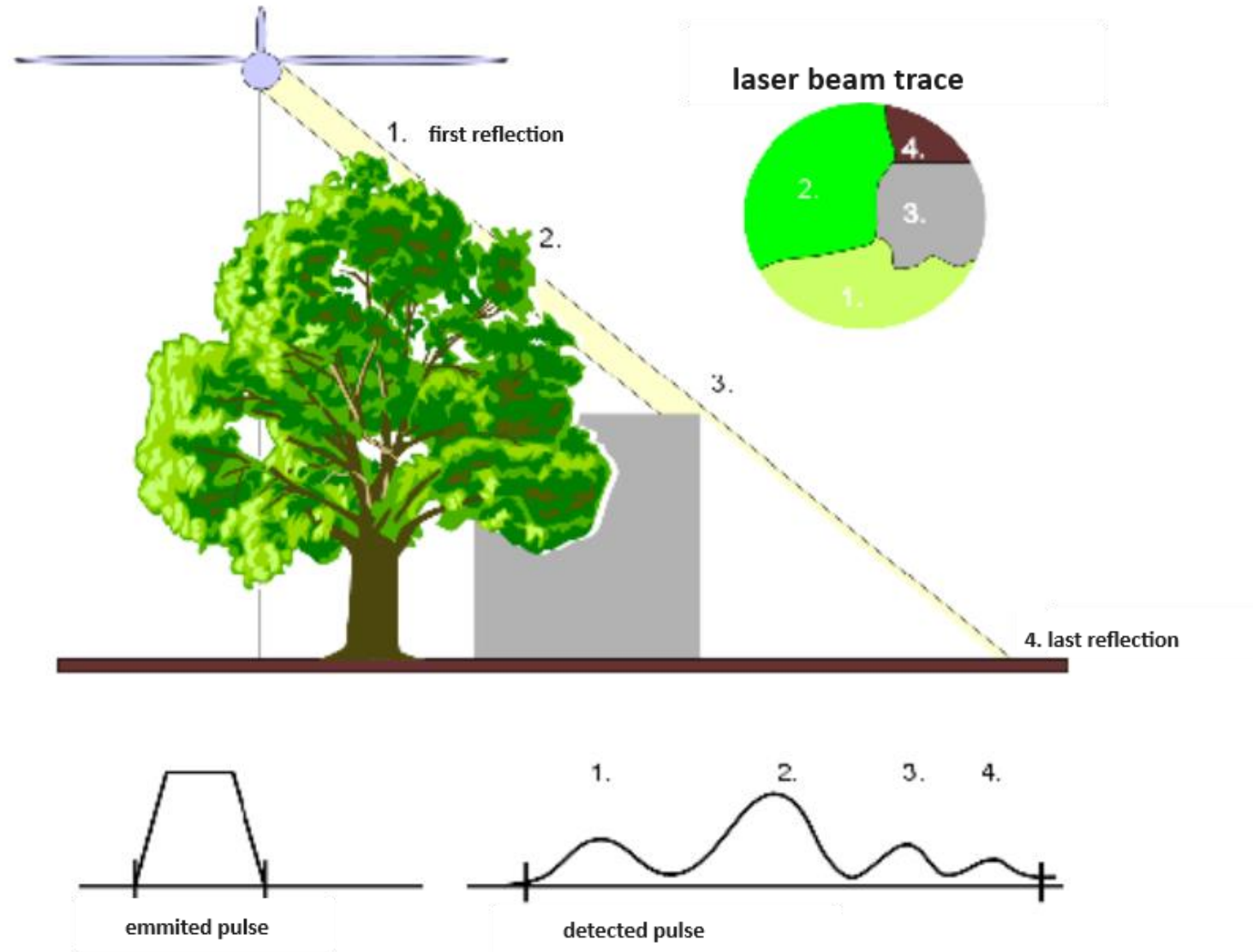
Technician using, very- high precission



ALS  
(airborne laser scanning)

# ALS

## The principle of laser airborne scanning



# ALS Technology - hardware



**Lidar Leica ALS 80**



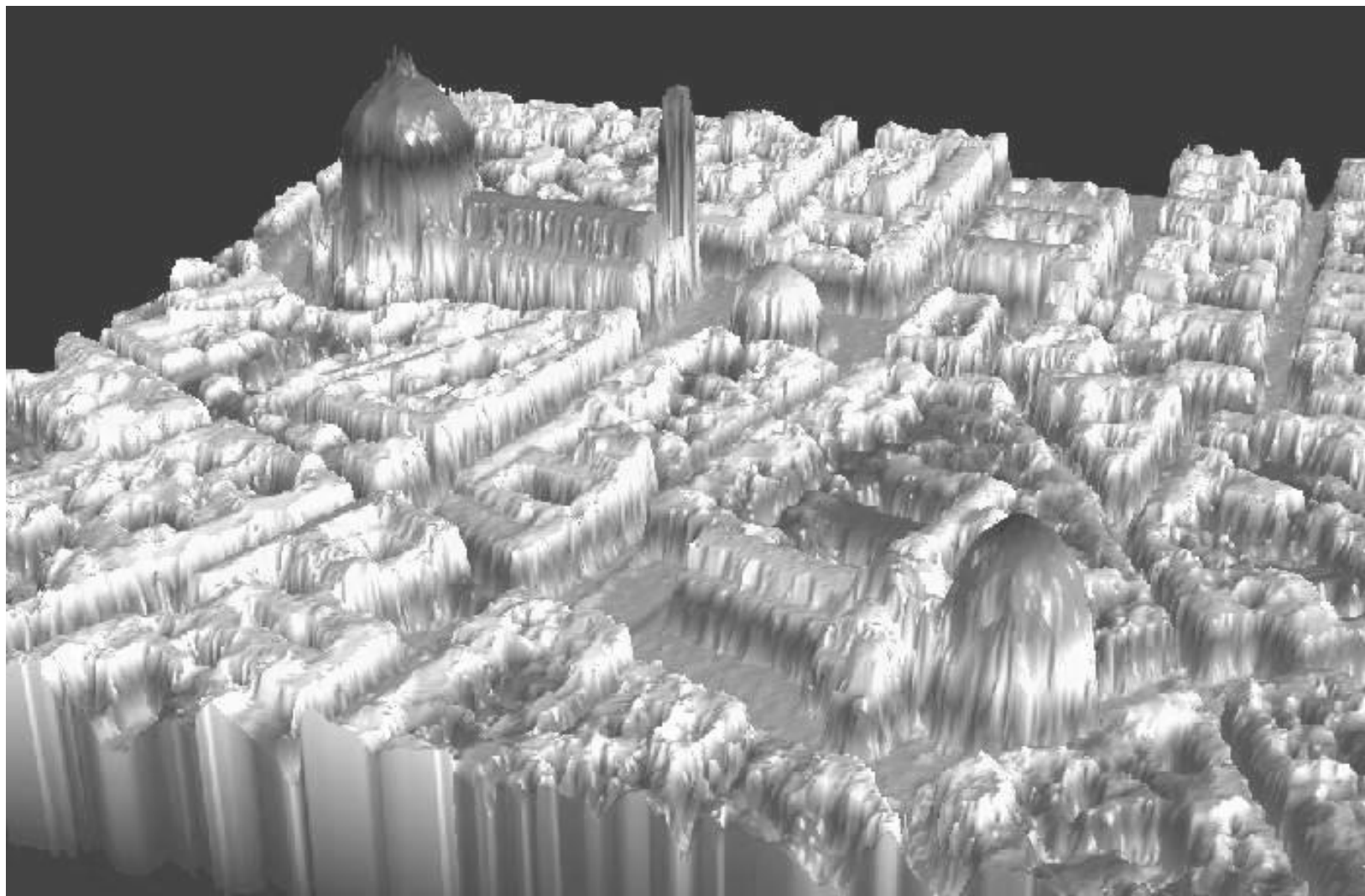
**LMS Q56 a data recorder  
DR-560**

**Lidar Falcon III.**



**ALTM 3100 (Optech)**

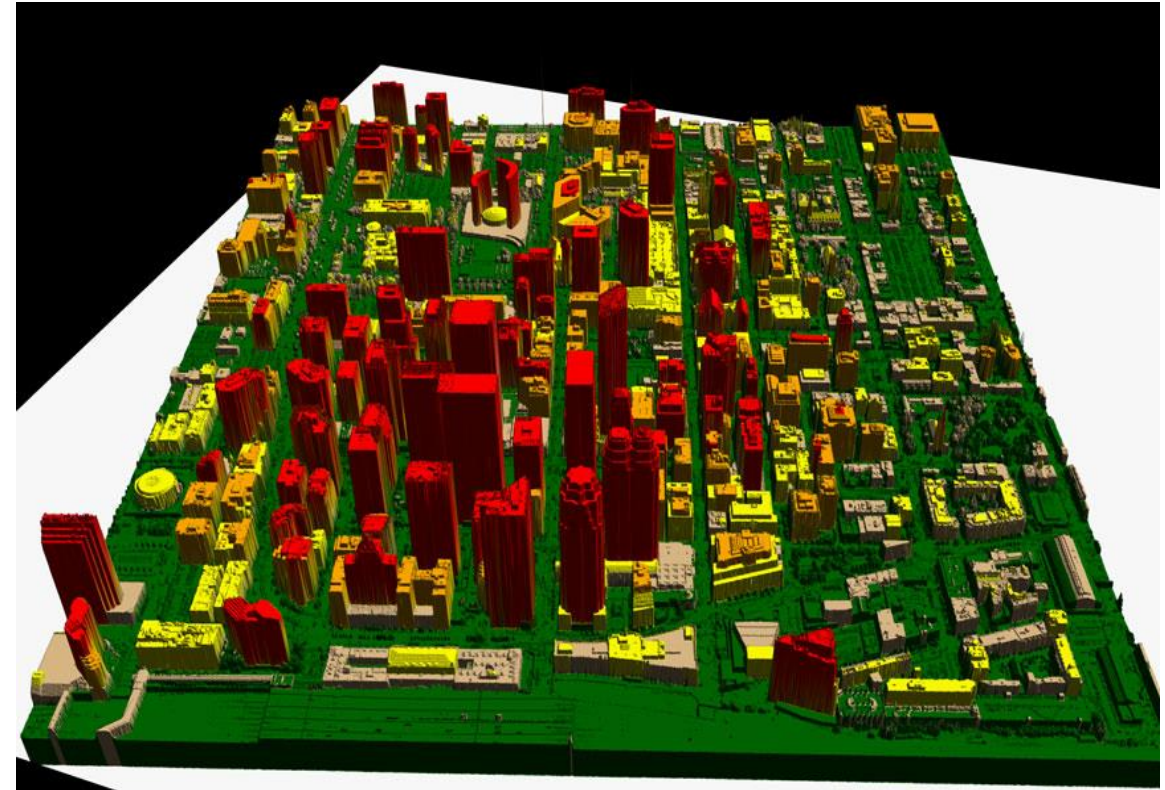
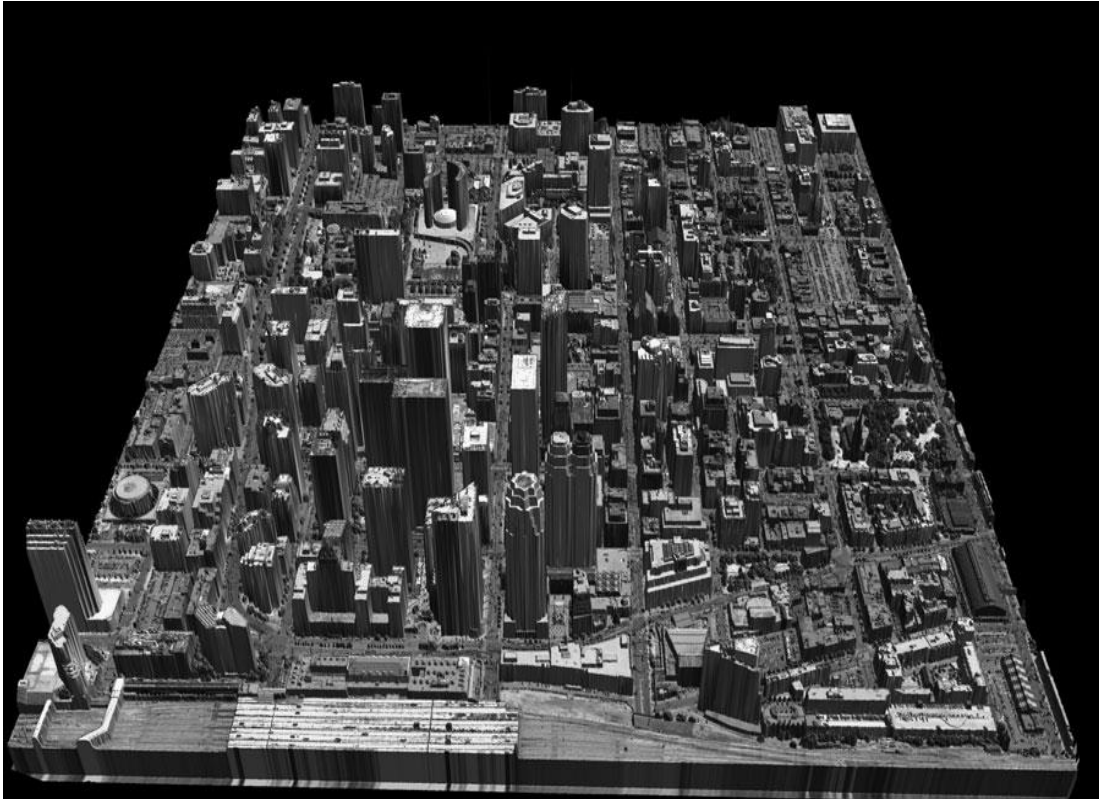
# ALS



- Older unfiltered 3D model of the city (1990s)

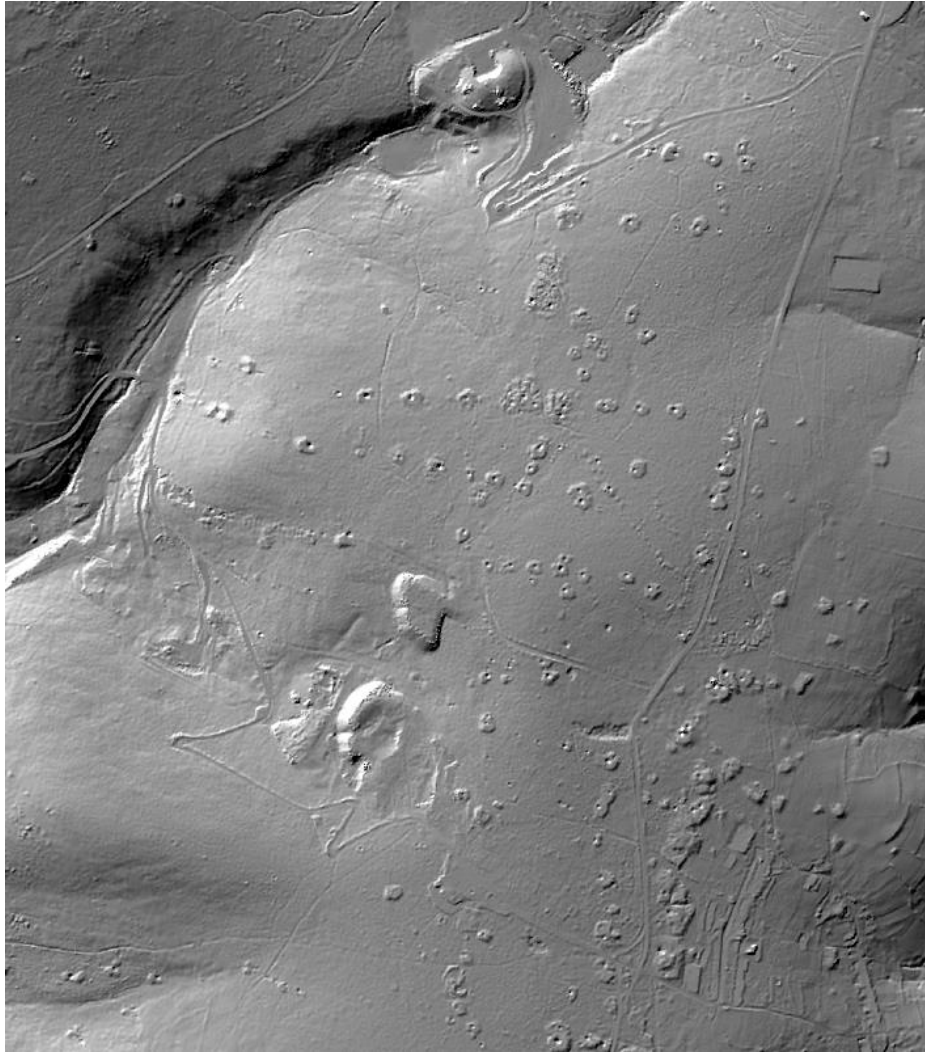


*Digital surface model and laser "image": ALTM sensor, flight height 850m, area 1400x1300m, measurement time 37min, processing 4h, density (raster) 60x60cm (Optech material, 2008)*





Aerial laser scanning: medieval silver mines and uranium mines  
of the last century. 2013.

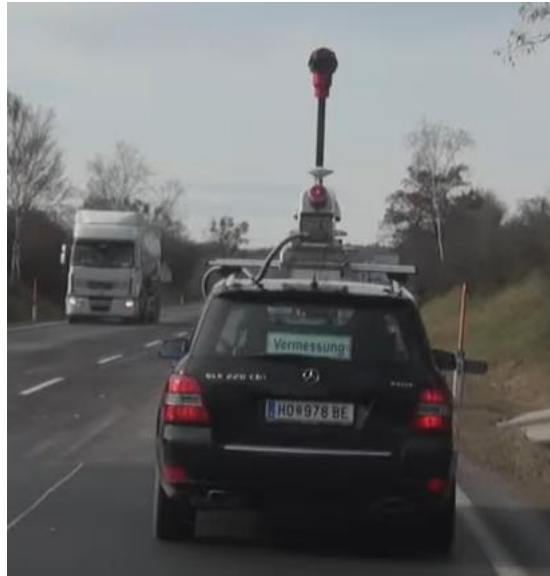


# L410 Turbolet FG (CZ)

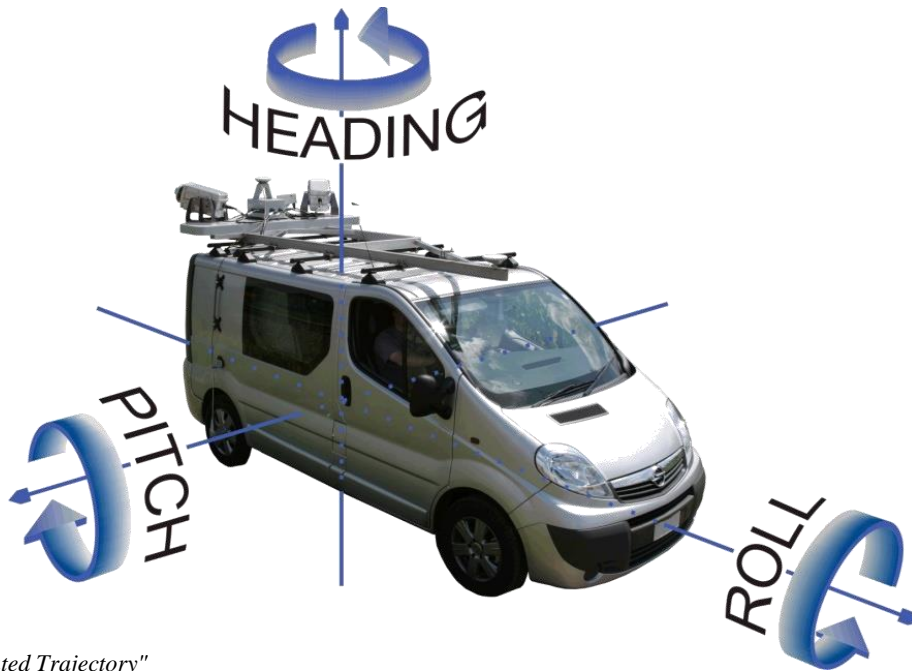




**New technologies: mobile mapping devices - carried by a person, in a car or other vehicle.**



# Mobile laser scanning



•SBET "Smoothed Best Estimated Trajectory"

•Real-time vehicle trajectory

•200 records per second

•Vehicle position (x, y, z) + roll and yaw

	with GNSS	1 min without GNSS
X,Y (m)	0.020	0.100
Z (m)	0.050	0.120
Tilts (°)	0.005	0.020
Angular Bending (°)	0.020	0.020

•Applanix POSLV 420

•2 GPS receivers

•Trimble Zephyr

•1 DMI (Distance Measuring Indicator)

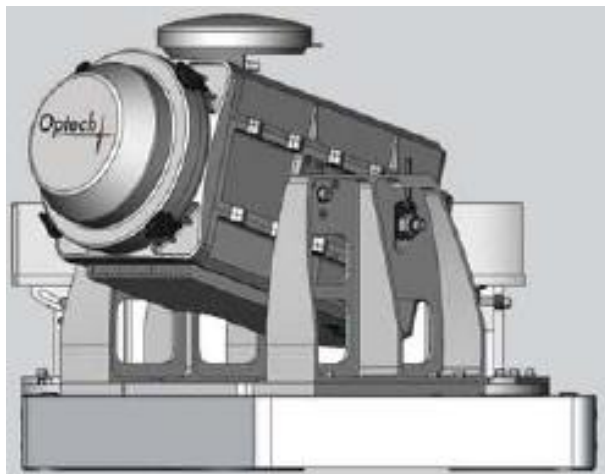
•1 IMU (Inertial Measuring Unit)

•Northrop Grumman LN-200

•3 gyroscopes

•3 accelerometers

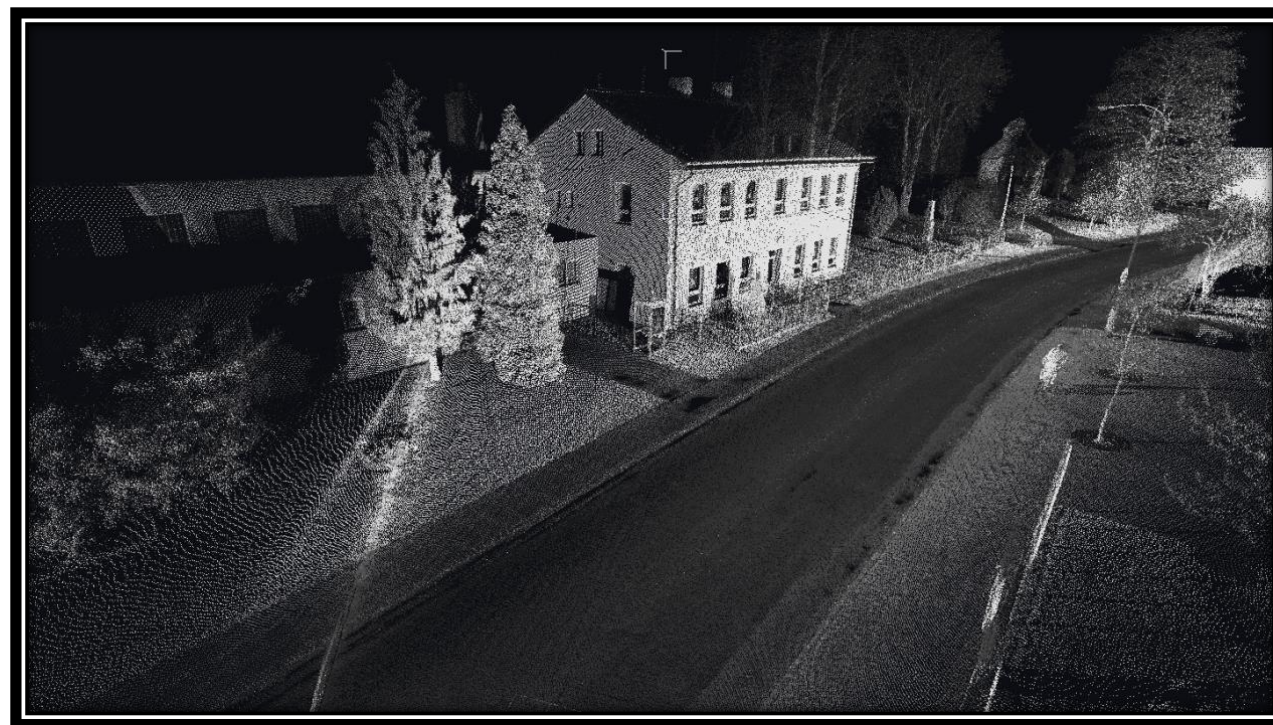


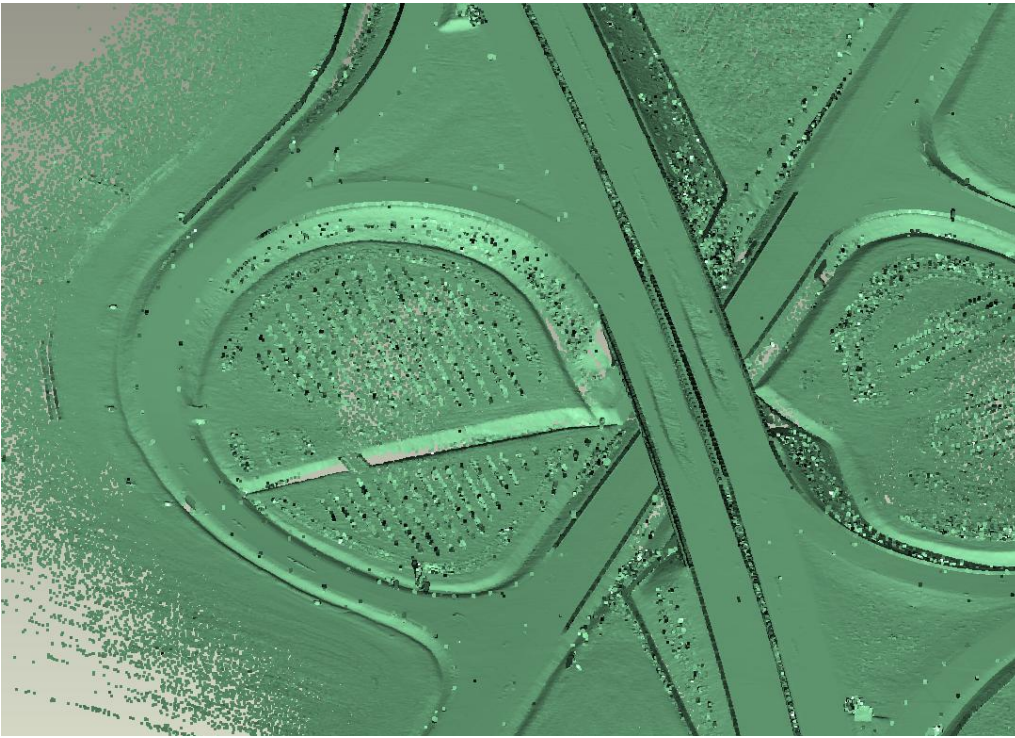


# Mobile laser scanning

• *Sample data - absolute accuracy of points  
+/- 5 cm (Geovap Pardubice)*

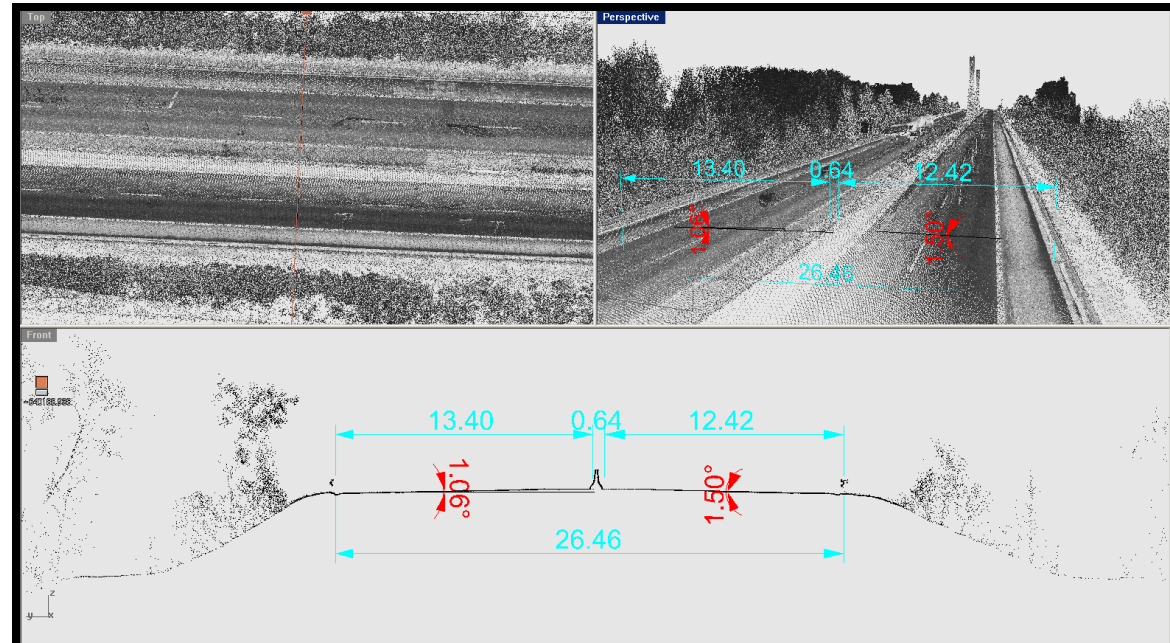
- *LYNX system - laser head*
- LYNX scanner heads
- 360° coverage
- Rotation speed: 9000 rpm
- Output: 200,000 pulses/sec
- Measuring up to 4 reflections/pulse
- Class 1 laser radiation safety
- Invisible beam
- Range up to 200 m
- >> targeting a 400 m wide swath





# Mobile laser scanning

- *Easy and fast use of measured data - no need for new types of software*





# *PLS: mobile - personal - handheld - laser scanner*

- *Designed mainly for data conversion to BIM, hand carried, no GNSS,*
- *SLAM technology is used for orientation in confined spaces*

## *Geoslam go*



## *Daro Orbis*



***End of laser scanning***